PROJ coordinate transformation software library

Release 6.1.1

PROJ contributors

September 2019
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## Using PROJ

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PROJ is a generic coordinate transformation software that transforms geospatial coordinates from one coordinate reference system (CRS) to another. This includes cartographic projections as well as geodetic transformations.

PROJ includes command line applications for easy conversion of coordinates from text files or directly from user input. In addition to the command line utilities PROJ also exposes an application programming interface, or API in short. The API lets developers use the functionality of PROJ in their own software without having to implement similar functionality themselves.

PROJ started purely as a cartography application letting users convert geodetic coordinates into projected coordinates using a number of different cartographic projections. Over the years, as the need has become apparent, support for datum shifts has slowly worked its way into PROJ as well. Today PROJ supports more than a hundred different map projections and can transform coordinates between datums using all but the most obscure geodetic techniques.

1.1 Citation

To cite PROJ in publications use:


A BibTeX entry for LaTeX users is

```latex
@Manual{,
  title = {{PROJ} coordinate transformation software library},
  author = {{PROJ contributors}},
  organization = {Open Source Geospatial Foundation},
  year = {2019},
  url = {https://proj.org/},
}
```
1.2 License

PROJ uses the MIT license. The software was initially released by the USGS in the public domain. When Frank Warmerdam took over the development of PROJ it was moved under the MIT license. The license is as follows:

Copyright (c) 2000, Frank Warmerdam

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2.1 6.1.1 Release Notes

July 1st 2019

2.1.1 Updates

• Update EPSG registry to version 9.6.3 (#1485)

2.1.2 Bug Fixes

• Take the passed authority into account when identifying objects (#1466)
• Avoid exception when transforming from NAD83 to projected CRS using NAD83(2011) (#1477)
• Avoid off-by-one reading of name argument if name of resource file has length 1 (#11489)
• Do not include PROJ_LIB in proj_info().searchpath when context search path is set (#1498)
• Use correct delimiter for the current platform when parsing PROJ_LIB (#1497)
• Do not confuse ‘ID74’ CRS with WKT2 ID[] node (#1506)
• WKT1 importer: do case insensitive comparison for axis direction (#1509)
• Avoid compile errors on GCC 4.9.3 (#1512)
• Make sure that pipelines including +proj=ob_tran can be created (#1526)

2.2 6.1.0 Release Notes

May 15th 2019
2.2.1 Updates

- Include custom ellipsoid definitions from QGIS (#1137)
- Add -k ellipsoid option to projinfo (#1338)
- Make cs2cs support 4D coordinates (#1355)
- WK2 parser: update to OGC 18-010r6 (#1360 #1366)
- Update internal version of googletest to v1.8.1 (#1361)
- Database update: EPSG v9.6.2 (#1462), IGNF v3.0.3, ESRI 10.7.0 and add operation_version column (#1368)
- Add proj_normalize_for_visualization() that attempts to apply axis ordering as used by most GIS applications and PROJ <6 (#1387)
- Added noop operation (#1391)
- Paths set by user take priority over PROJ_LIB for search paths (#1398)
- Reduced database size (#1438)
- add support for compoundCRS and concatenatedOperation named from their components (#1441)

2.2.2 Bug fixes

- Have gie return non-zero code when file can’t be opened (#1312)
- CMake cross-compilation fix (#1316)
- Use 1st eccentricity instead of 2nd eccentricity in Molodensky (#1324)
- Make sure to include grids when doing Geocentric to CompoundCRS with nadgrids+geoidgrids transformations (#1326)
- Handle coordinates outside of bbox better (#1333)
- Enable system error messages in command line automatically in builds (#1336)
- Make sure to install projinfo man page with CMake (#1347)
- Add data dir to pkg-config file proj.pc (#1348)
- Fix GCC 9 warning about useless std::move() (#1352)
- Grid related fixes (#1369)
- Make sure that ISO19111 C++ code sets pj_errno on errors (#1405)
- vgridshift: handle longitude wrap-around for grids with 360deg longitude extent (#1429)
- proj/cs2cs: validate value of -f parameter to avoid potential crashes (#1434)
- Many division by zero and similar bug fixes found by OSS Fuzz.
2.3 6.0.0 Release Notes

March 1st 2019

PROJ 6 has undergone extensive changes to increase its functional scope from a cartographic projection engine with so-called “early-binding” geodetic datum transformation capabilities to a more complete library supporting coordinate transformations and coordinate reference systems.

As a foundation for other enhancements, PROJ now includes a C++ implementation of the modelisation proposed by the ISO-19111:2019 standard / OGC Abstract Specification Topic 2: “Referencing By Coordinates”, for geodetic reference frames (datums), coordinate reference systems and coordinate operations. Construction and query of those geodetic objects is available through a new C++ API, and also accessible for the most part from bindings in the C API.

Those geodetic objects can be imported and exported from and into the OGC Well-Known Text format (WKT) in its different variants: ESRI WKT, GDAL WKT 1, WKT2:2015 (ISO 19162:2015) and WKT2:2018 (ISO 19162:2018). Import and export of CRS objects from and into PROJ strings is also supported. This functionality was previously available in the GDAL software library (except WKT2 support which is a new feature), and is now an integral part of PROJ.

A unified database of geodetic objects, coordinate reference systems and their metadata, and coordinate operations between those CRS is now available in a SQLite3 database file, proj.db. This includes definitions imported from the IOGP EPSG dataset (v9.6.0 release), the IGNF (French national mapping agency) geodetic registry and the ESRI projection engine database. PROJ is now the reference software in the “OSGeo C stack” for this CRS and coordinate operation database, whereas previously this functionality was spread over PROJ, GDAL and libgeotiff, and used CSV or other adhoc text-based formats.

Late-binding coordinate operation capabilities, that takes metadata such as area of use and accuracy into account, has been added. This can avoid in a number of situations the past requirement of using WGS84 as a pivot system, which could cause unneeded accuracy loss, or was not doable at all sometimes when transformation to WGS84 was not available. Those late-binding capabilities are now used by the proj_create_crs_to_crs() function and the cs2cs utility.

A new command line utility, projinfo, has been added to query information about a geodetic object of the database, import and export geodetic objects from/into WKT and PROJ strings, and display coordinate operations available between two CRSs.

2.3.1 UPDATES

- Removed projects.h as a public interface (#835)
- Deprecated the proj_api.h interface. The header file is still available but will be removed with the next major version release of PROJ. It is now required to define ACCEPT_USE_OF_DEPRECATED_PROJ_API_H before the interface can be used (#836)
- Removed support for the nmake build system (#838)
- Removed support for the proj_def.dat defaults file (#201)
- C++11 required for building PROJ (#1203)
- Added build dependency on SQLite 3.7 (#1175)
- Added projinfo command line application (#1189)
- Added many functions to proj.h for handling ISO19111 functionality (#1175)
- Added C++ API exposing ISO19111 functionality (#1175)
- Updated cs2cs to use late-binding features (#1182)
- Removed the nad2bin application. Now available in the proj-datumgrid git repository (#1236)
• Removed support for Chebyshev polynomials in proj (#1226)
• Removed proj_geocentric_latitude() from proj.h API (#1170)
• Changed behaviour of proj: Now only allow initialization of projections (#1162)
• Changed behaviour of tmesc: Now defaults to the Extended Transverse Mercator algorithm (etmerc). Old implementation available by adding +approx (#404)
• Chaged behaviour: Default ellipsoid now set to GRS80 (was WGS84) (#1210)
• Allow multiple directories in PROJ_LIB environment variable (#1281)
• Added Lambert Conic Conformal (2SP Michigan) projection (#1142)
• Added Bertin1953 projection (#1133)
• Added Tobler-Mercator projection (#1153)
• Added Molodensky-Badekas transform (#1160)
• Added push and pop coordinate operations (#1250)
• Removed +t_obs parameter from helmert and deformation (#1264)
• Added +dt parameter to deformation as replacement for removed +t_obs (#1264)

2.3.2 BUG FIXES

• Read +towgs84 values correctly on locales not using dot as comma separator (#1136)
• Fixed file offset for reading of shift values in NTv1 files (#1144)
• Avoid problems with PTHREAD_MUTEX_RECURSIVE when using CMake (#1158)
• Avoid raising errors when setting ellipsoid flattening to zero (#1191)
• Fixed lower square calculations in rHealpix projection (#1206)
• Allow Molodensky transform parameters to be zero (#1194)
• Fixed wrong parameter in ITRF2000 init file (#1240)
• Fixed use of grid paths including spaces (#1152)
• Robinson: fix wrong values for forward path for latitudes >= 87.5, and fix inaccurate inverse method (#1172)

2.4 PROJ 5.2.0

September 15th 2018
2.4.1 UPDATES

- Added support for deg, rad and grad in unitconvert (#1054)
- Assume \texttt{t\_epoch} as time input when not otherwise specified (#1065)
- Added inverse Lagrange projection (#1058)
- Added \texttt{multiplier} option to vgridshift (#1072)
- Added Equal Earth projection (#1085)
- Added “require\_grid” option to gie (#1088)
- Replace \texttt{transpose} option of Helmert transform with \texttt{convention}. From now on the convention used should be explicitly written. An error will be returned when using the \texttt{transpose} option (#1091)
- Improved numerical precision of inverse spherical Mercator projection (#1105)
- \texttt{cct} will now forward text after coordinate input to output stream (#1111)

2.4.2 BUG FIXES

- Do not pivot over WGS84 when doing cs2cs-emulation with geocent (#1026)
- Do not scan past the end of the read data in \texttt{pj\_ctx\_fgets()} (#1042)
- Make sure \texttt{proj\_errno\_string()} is available in DLL (#1050)
- Respect \texttt{to\_meter} setting when doing cs2cs-emulation (#1053)
- Fixed unit conversion factors for \texttt{geod} (#1075)
- Fixed test failures related to GCC 8 (#1084)
- Improved handling of \texttt{geoc} flag (#1093)
- Calculate correct projection factors for Webmercator (#1095)
- \texttt{cs2cs} now always outputs degrees when transformed coordinates are in angular units (#1112)

2.5 PROJ 5.1.0

June 1st 2018

2.5.1 UPDATES

- Function \texttt{proj\_errno\_string()} added to \texttt{proj.h} API (#847)
- Validate units between pipeline steps and ensure transformation sanity (#906)
- Print help when calling \texttt{cct} and \texttt{gie} without arguments (#907)
- \texttt{CITATION} file added to source distribution (#914)
- Webmercator operation added (#925)
- Enhanced numerical precision of forward spherical Mercator near the Equator (#928)
- Added \texttt{--skip\_lines} option to \texttt{cct} (#923)
- Consistently return \texttt{NaN} values on \texttt{NaN} input (#949)
• Removed unused `src/org_proj4_Projections.h` file (#956)
• Java Native Interface bindings updated (#957, #969)
• Horizontal and vertical gridshift operations extended to the temporal domain (#1015)

### 2.5.2 BUG FIXES

- Handle NaN float cast overflow in `PJ_robin.c` and `nad_intr.c` (#887)
- Avoid overflow when Horner order is unreasonably large (#893)
- Avoid unwanted NaN conversions in etmerc (#899)
- Avoid memory failure in `gie` when not specifying x,y,z in gie files (#902)
- Avoid memory failure when `+sweep` is initialized incorrectly in geos (#908)
- Return `HUGE_VAL` on erroneous input in ortho (#912)
- Handle commented lines correctly in cct (#933)
- Avoid segmentation fault when transformation coordinates outside grid area in deformation (#934)
- Avoid doing false easting/northing adjustments on cartesian coordinates (#936)
- Thread-safe creation of proj mutex (#954)
- Avoid errors when setting up geos with `+lat_0!=0` (#986)
- Reset errno when running `proj` in verbose mode (#988)
- Do not interpolate node values at nodata value in vertical grid shifts (#1004)
- Restrict Horner degrees to positive integer values to avoid memory allocation issues (#1005)

### 2.6 PROJ 5.0.1

**March 1st 2018**

#### 2.6.1 Bug fixes

- Handle ellipsoid change correctly in pipelines when `+towgs84=0,0,0` is set (#881)
- Handle the case where `nad_cetable2_init` returns NULL (#883)
- Avoid shadowed declaration errors with old gcc (#880)
- Expand `+datum` properly in pipelines (#872)
- Fail gracefully when incorrect headers are encountered in grid files (#875)
- Improve roundtrip stability in pipelines using `+towgs84` (#871)
- Fixed typo in gie error codes (#861)
- Numerical stability fixes to the geodesic package (#826 & #843)
- Make sure that transient errors are returned correctly (#857)
- Make sure that locally installed header files are not used when building PROJ (#849)
- Fix inconsistent parameter names in `proj.h/proj_4D_api.c` (#842)
• Make sure `+vunits` is applied (#833)
• Fix incorrect Web Mercator transformations (#834)

2.7 PROJ 5.0.0

February 1st 2018

This version of PROJ introduces some significant extensions and improvements to (primarily) the geodetic functionality of the system.

The main driver for introducing the new features is the emergence of dynamic reference frames, the increasing use of high accuracy GNSS, and the related growing demand for accurate coordinate transformations. While older versions of PROJ included some geodetic functionality, the new framework lays the foundation for turning PROJ into a generic geospatial coordinate transformation engine.

The core of the library is still the well established projection code. The new functionality is primarily exposed in a new programming interface and a new command line utility, `cct` (for “Coordinate Conversion and Transformation”). The old programming interface is still available and can - to some extent - use the new geodetic transformation features.

The internal architecture has also seen many changes and much improvement. So far, these improvements respect the existing programming interface. But the process has revealed a need to simplify and reduce the code base, in order to support sustained active development.

Therefore we have scheduled regular releases over the coming years which will gradually remove the old programming interface.

This will cause breaking changes with the next two major version releases, which will affect all projects that depend on PROJ (cf. section “deprecations” below).

The decision to break the existing API has not been easy, but has ultimately been deemed necessary to ensure the long term survival of the project. Not only by improving the maintainability immensely, but also by extending the potential user (and hence developer) community.

The end goal is to deliver a generic coordinate transformation software package with a clean and concise code base appealing to both users and developers.

2.7.1 Versioning and naming

For the first time in more than 25 years the major version number of the software is changed. The decision to do this is based on the many new features and new API. While backwards compatibility remains - except in a few rare corner cases - the addition of a new and improved programming interface warrants a new major release.

The new major version number unfortunately leaves the project in a bit of a conundrum regarding the name. For the majority of the life-time of the product it has been known as PROJ.4, but since we have now reached version 5 the name is no longer aligned with the version number.

Hence we have decided to decouple the name from the version number and from this version and onwards the product will simply be called PROJ.

In recognition of the history of the software we are keeping PROJ.4 as the name of the organizing project. The same project team also produces the datum-grid package.

In summary:

• The PROJ.4 project provides the product PROJ, which is now at version 5.0.0.
• The foundational component of PROJ is the library libproj.
Other PROJ components include the application proj, which provides a command line interface to libproj.

The PROJ.4 project also distributes the datum-grid package, which at the time of writing is at version 1.6.0.

### 2.7.2 Updates

- Introduced new API in `proj.h`.
  - The new API is orthogonal to the existing `proj_api.h` API and the internally used `projects.h` API.
  - The new API adds the ability to transform spatiotemporal (4D) coordinates.
  - Functions in the new API use the `proj_` namespace.
  - Data types in the new API use the `PJ_` namespace.
- Introduced the concept of “transformation pipelines” that makes possible to do complex geodetic transformations of coordinates by daisy chaining simple coordinate operations.
- Introduced `cct`, the Coordinate Conversion and Transformation application.
- Introduced `gie`, the Geospatial Integrity Investigation Environment.
  - Selftest invoked by `-C` flag in `proj` has been removed
  - Ported approx. 1300 built-in selftests to `gie` format
  - Ported approx. 1000 tests from the gigs test framework
  - Added approx. 200 new tests
- Adopted terminology from the OGC/ISO-19100 geospatial standards series. Key definitions are:
  - At the most generic level, a coordinate operation is a change of coordinates, based on a one-to-one relationship, from one coordinate reference system to another.
  - A transformation is a coordinate operation in which the two coordinate reference systems are based on different datums, e.g. a change from a global reference frame to a regional frame.
  - A conversion is a coordinate operation in which both coordinate reference systems are based on the same datum, e.g. change of units of coordinates.
  - A projection is a coordinate conversion from an ellipsoidal coordinate system to a plane. Although projections are simply conversions according to the standard, they are treated as separate entities in PROJ as they make up the vast majority of operations in the library.
- New operations
  - The pipeline operator (pipeline)
  - Transformations
    * Helmert transform (`helmert`)
    * Horner real and complex polynomial evaluation (`horner`)
    * Horizontal gridshift (`hgridshift`)
    * Vertical gridshift (`vgridshift`)
    * Molodensky transform (`molodensky`)
    * Kinematic gridshift with deformation model (`deformation`)
  - Conversions
    * Unit conversion (`unitconvert`)
2.7.3 Bug fixes

• Fixed incorrect convergence calculation in Lambert Conformal Conic. (#16)
• Handle ellipsoid parameters correctly when using +nadgrids=@null. (#22)
• Return correct latitude when using negative northings in Transverse Mercator. (#138)
• Return correct result at origin in inverse Mod. Stereographic of Alaska. (#161)
• Return correct result at origin in inverse Mod. Stereographic of 48 U.S. (#162)
• Return correct result at origin in inverse Mod. Stereographic of 50 U.S. (#163)
• Return correct result at origin in inverse Lee Oblated Stereographic. (#164)
• Return correct result at origin in inverse Miller Oblated Stereographic. (#165)
• Fixed scaling and wrap-around issues in Oblique Cylindrical Equal Area. (#166)
• Corrected a coefficient error in inverse Transverse Mercator. (#174)
• Respect —r flag when calling proj with —V. (#184)
• Remove multiplication by 2 at the equator error in Stereographic projection. (#194)
• Allow +alpha=0 and +gamma=0 when using Oblique Mercator. (#195)
• Return correct result of inverse Oblique Mercator when alpha is between 90 and 270. (#331)
• Avoid segmentation fault when accessing point outside grid. (#396)
• Avoid segmentation fault on NaN input in Robin inverse. (#463)
• Very verbose use of proj (—V) on Windows is fixed. (#484)
• Fixed memory leak in General Oblique Transformation. (#497)
• Equations for meridian convergence and partial derivatives have been corrected for non-conformal projections. (#526)
• Fixed scaling of cartesian coordinates in pj_transform(). (#726)
• Additional bug fixes courtesy of Google’s OSS-Fuzz program
Download

Here you can download current and previous releases of PROJ. We only supply a distribution of the source code and various resource file archives. See Installation for information on how to get pre-built packages of PROJ.

3.1 Current Release

- 2019-07-01 proj-6.1.1.tar.gz (md5)
- 2018-09-15 proj-datumgrid-1.8.zip
- 2019-03-01 proj-datumgrid-europe-1.3.zip
- 2019-03-01 proj-datumgrid-north-america-1.2.zip
- 2018-03-01 proj-datumgrid-oceania-1.0.zip
- 2019-03-01 proj-datumgrid-world-1.0.zip

3.2 Past Releases

- 2019-05-15 proj-6.1.0.tar.gz
- 2019-03-01 proj-6.0.0.tar.gz
- 2018-09-15 proj-5.2.0.tar.gz
- 2018-06-01 proj-5.1.0.tar.gz
- 2018-04-01 proj-5.0.1.tar.gz
- 2018-03-01 proj-5.0.0.tar.gz
- 2016-09-02 proj-4.9.3.tar.gz
- 2015-09-13 proj-4.9.2.tar.gz
- 2015-03-04 proj-4.9.1.tar.gz
- 2018-03-01 proj-datumgrid-1.7.zip
- 2016-09-11 proj-datumgrid-1.6.zip
- 2019-03-01 proj-datumgrid-europe-1.2.zip
- 2018-09-15 proj-datumgrid-europe-1.1.zip
- 2018-09-15 proj-datumgrid-north-america-1.1.zip
• 2018-03-01 proj-datumgrid-europe-1.0.zip
• 2018-03-01 proj-datumgrid-north-america-1.0.zip
These pages describe how to install PROJ on your computer without compiling it yourself. Below are guides for installing on Windows, Linux and Mac OS X. This is a good place to get started if this is your first time using PROJ. More advanced users may want to compile the software themselves.

### 4.1 Installation from package management systems

#### 4.1.1 Cross platform

PROJ is also available via cross platform package managers.

##### 4.1.1.1 Conda

The conda package manager includes several PROJ packages. We recommend installing from the conda-forge channel:

```
conda install -c conda-forge proj4
```

##### 4.1.1.2 Docker

A Docker image with just PROJ binaries and a full compliment of grid shift files is available on DockerHub. Get the package with:

```
docker pull osgeo/proj
```

#### 4.1.2 Windows

The simplest way to install PROJ on Windows is to use the OSGeo4W software distribution. OSGeo4W provides easy access to many popular open source geospatial software packages. After installation you can use PROJ from the OSGeo4W shell. To install PROJ do the following:

**Note:** If you have already installed software via OSGeo4W on your computer it is likely that PROJ is already installed.

1. Download either the 32 bit or 64 bit installer.
2. Run the OSGeo4W setup program.
4. Select “Install from Internet” and press Next.
5. Select a installation directory. The default suggestion is fine in most cases. Press Next.
6. Select “Local package directory”. The default suggestion is fine in most cases. Press Next.
7. Select “Direct connection” and press Next.
8. Choose the download.osgeo.org server and press Next.
9. Find “proj” under “Commandline_Utilities” and click the package in the “New” column until the version you want to install appears.
10. Press next to install PROJ.

You should now have a “OSGeo” menu in your start menu. Within that menu you can find the “OSGeo4W Shell” where you have access to all the OSGeo4W applications, including proj.

For those who are more inclined to the command line, steps 2–10 above can be accomplished by executing the following command:

```
C:\temp\osgeo4w-setup-x86-64.exe -q -k -r -A -s http://download.osgeo.org/osgeo4w/ -a -x86_64 -P proj
```

### 4.1.3 Linux

How to install PROJ on Linux depends on which distribution you are using. Below is a few examples for some of the more common Linux distributions:

#### 4.1.3.1 Debian

On Debian and similar systems (e.g. Ubuntu) the APT package manager is used:

```
sudo apt-get install proj-bin
```

#### 4.1.3.2 Red Hat

On Red Hat based system packages are installed with yum:

```
sudo yum install proj
```

### 4.1.4 Mac OS X

On OS X PROJ can be installed via the Homebrew package manager:

```
brew install proj
```

PROJ is also available from the MacPorts system:

```
sudo ports install proj
```
4.2 Compilation and installation from source code

The classical way of installing PROJ is via the source code distribution. The most recent version is available from the download page.

PROJ requires C and C++11 compilers. It also requires SQLite3 (headers, library and executable).

You will need that and at least the standard proj-datumgrid package for a successful installation.

The following guides show how to compile and install the software using the Autotools and CMake build systems.

### 4.2.1 Autotools

FSF’s configuration procedure is used to ease installation of the PROJ system.

Note: The Autotools build system is only available on UNIX-like systems. Follow the CMake installation guide if you are not using a UNIX-like operating system.

The default destination path prefix for installed files is /usr/local. Results from the installation script will be placed into subdirectories bin, include, lib, man/man1 and man/man3. If this default path prefix is proper, then execute:

```
./configure
```

If another path prefix is required, then execute:

```
./configure --prefix=/my/path
```

In either case, the directory of the prefix path must exist and be writable by the installer.

Before proceeding with the installation we need to add the datum grids. Unzip the contents of the proj-datumgrid package into data/:

```
unzip proj-datumgrid-1.7.zip -d proj-5.0.1/data/
```

The installation will automatically move the grid files to the correct location. Alternatively the grids can be installed manually in the directory pointed to by the PROJ_LIB environment variable. The default location is /usr/local/share/proj.

With the grid files in place we can now build and install PROJ:

```
make
make install
```

The install target will create, if necessary, all required sub-directories.

Tests are run with:

```
make check
```

The test suite requires that the proj-datumgrid package is installed in PROJ_LIB.
4.2.2 CMake

With the CMake build system you can compile and install PROJ on more or less any platform. After unpacking the source distribution archive step into the source-tree:

```
cd proj-5.0.1
```

Create a build directory and step into it:

```
mkdir build
cd build
```

From the build directory you can now configure CMake and build the binaries:

```
cmake ..
cmake --build .
```

On Windows, one may need to specify generator:

```
cmake -G "Visual Studio 15 2017" ..
```

If the SQLite3 dependency is installed in a custom location, specify the paths to the include directory and the library:

```
cmake -DSQLITE3_INCLUDE_DIR=/opt/SQLite/include -DSQLITE3_LIBRARY=/opt/SQLite/lib/
        -lsqlite3.so ..
```

Alternatively, the custom prefix for SQLite3 can be specified:

```
cmake -DCMAKE_PREFIX_PATH=/opt/SQLite ..
```

Tests are run with:

```
test
```

The test suite requires that the proj-datumgrid package is installed in `PROJ_LIB`. 
The main purpose of PROJ is to transform coordinates from one coordinate reference system to another. This can be achieved either with the included command line applications or the C API that is a part of the software package.

## 5.1 Quick start

Coordinate transformations are defined by, what in PROJ terminology is known as, “proj-strings”. A proj-string describes any transformation regardless of how simple or complicated it might be. The simplest case is projection of geodetic coordinates. This section focuses on the simpler cases and introduces the basic anatomy of the proj-string. The complex cases are discussed in *Geodetic transformation*.

A proj-strings holds the parameters of a given coordinate transformation, e.g.

```plaintext
+proj=merc +lat_ts=56.5 +ellps=GRS80
```

I.e. a proj-string consists of a projection specifier, +proj, a number of parameters that applies to the projection and, if needed, a description of a datum shift. In the example above geodetic coordinates are transformed to projected space with the Mercator projection with the latitude of true scale at 56.5 degrees north on the GRS80 ellipsoid. Every projection in PROJ is identified by a shorthand such as merc in the above example.

By using the above projection definition as parameters for the command line utility proj we can convert the geodetic coordinates to projected space:

```bash
$ proj +proj=merc +lat_ts=56.5 +ellps=GRS80
```

If called as above proj will be in interactive mode, letting you type the input data manually and getting a response presented on screen. proj works as any UNIX filter though, which means that you can also pipe data to the utility, for instance by using the echo command:

```bash
$ echo 55.2 12.2 | proj +proj=merc +lat_ts=56.5 +ellps=GRS80
3399483.80 752085.60
```

PROJ also comes bundled with the cs2cs utility which is used to transform from one coordinate reference system to another. Say we want to convert the above Mercator coordinates to UTM, we can do that with cs2cs:

```bash
$ echo 3399483.80 752085.60 | cs2cs +proj=merc +lat_ts=56.5 +ellps=GRS80 +to +proj=utm +zone=32
6103992.36 1924052.47 0.00
```

Notice the +to parameter that separates the source and destination projection definitions.

If you happen to know the EPSG identifiers for the two coordinates reference systems you are transforming between you can use those with cs2cs:
\$ echo 56 12 | cs2cs +init=epsg:4326 +to +init=epsg:25832

231950.54 1920310.71 0.00

In the above example we transform geodetic coordinates in the WGS84 reference frame to UTM zone 32N coordinates in the ETRS89 reference frame. UTM coordinates

### 5.2 Cartographic projection

The foundation of PROJ is the large number of *projections* available in the library. This section is devoted to the generic parameters that can be used on any projection in the PROJ library.

Below is a list of PROJ parameters which can be applied to most coordinate system definitions. This table does not attempt to describe the parameters particular to particular projection types. These can be found on the pages documenting the individual *projections*.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>+a</td>
<td>Semimajor radius of the ellipsoid axis</td>
</tr>
<tr>
<td>+axis</td>
<td>Axis orientation</td>
</tr>
<tr>
<td>+b</td>
<td>Semiminor radius of the ellipsoid axis</td>
</tr>
<tr>
<td>+ellps</td>
<td>Ellipsoid name (see <code>proj -le</code>)</td>
</tr>
<tr>
<td>+k</td>
<td>Scaling factor (deprecated)</td>
</tr>
<tr>
<td>+k_0</td>
<td>Scaling factor</td>
</tr>
<tr>
<td>+lat_0</td>
<td>Latitude of origin</td>
</tr>
<tr>
<td>+lon_0</td>
<td>Central meridian</td>
</tr>
<tr>
<td>+lon_wrap</td>
<td>Center longitude to use for wrapping (see below)</td>
</tr>
<tr>
<td>+over</td>
<td>Allow longitude output outside -180 to 180 range, disables wrapping (see below)</td>
</tr>
<tr>
<td>+pm</td>
<td>Alternate prime meridian (typically a city name, see below)</td>
</tr>
<tr>
<td>+proj</td>
<td>Projection name (see <code>proj -l</code>)</td>
</tr>
<tr>
<td>+units</td>
<td>meters, US survey feet, etc.</td>
</tr>
<tr>
<td>+vunits</td>
<td>vertical units.</td>
</tr>
<tr>
<td>+x_0</td>
<td>False easting</td>
</tr>
<tr>
<td>+y_0</td>
<td>False northing</td>
</tr>
</tbody>
</table>

In the sections below most of the parameters are explained in details.

#### 5.2.1 Units

Horizontal units can be specified using the `+units` keyword with a symbolic name for a unit (ie. `us-ft`). Alternatively the translation to meters can be specified with the `+to_meter` keyword (ie. 0.304800609601219 for US feet). The `-lu` argument to `cs2cs` or `proj` can be used to list symbolic unit names. The default unit for projected coordinates is the meter. A few special projections deviate from this behaviour, most notably the latlong pseudo-projection that returns degrees.

Vertical (Z) units can be specified using the `+vunits` keyword with a symbolic name for a unit (ie. `us-ft`). Alternatively the translation to meters can be specified with the `+vto_meter` keyword (ie. 0.304800609601219 for US feet). The `-lu` argument to `cs2cs` or `proj` can be used to list symbolic unit names. If no vertical units are specified, the vertical units will default to be the same as the horizontal coordinates.

**Note:** `proj` do not handle vertical units at all and hence the `+vto_meter` argument will be ignored.
Scaling of output units can be done by applying the \( +k_0 \) argument. The returned coordinates are scaled by the value assigned with the \( +k_0 \) parameter.

5.2.2 False Easting/Northing

Virtually all coordinate systems allow for the presence of a false easting (\( +x_0 \)) and northing (\( +y_0 \)). Note that these values are always expressed in meters even if the coordinate system is some other units. Some coordinate systems (such as UTM) have implicit false easting and northing values.

5.2.3 Longitude Wrapping

By default PROJ wraps output longitudes in the range -180 to 180. The \( +\text{over} \) switch can be used to disable the default wrapping which is done at a low level in \( \text{pj\_inv}() \). This is particularly useful with projections like the equidistant cylindrical where it would be desirable for X values past -20000000 (roughly) to continue past -180 instead of wrapping to +180.

The \( +\text{lon\_wrap} \) option can be used to provide an alternative means of doing longitude wrapping within \( \text{pj\_transform()} \). The argument to this option is a center longitude. So \( +\text{lon\_wrap}=180 \) means wrap longitudes in the range 0 to 360. Note that \( +\text{over} \) does not disable \( +\text{lon\_wrap} \).

5.2.4 Prime Meridian

A prime meridian may be declared indicating the offset between the prime meridian of the declared coordinate system and that of greenwich. A prime meridian is declared using the “pm” parameter, and may be assigned a symbolic name, or the longitude of the alternative prime meridian relative to greenwich.

Currently prime meridian declarations are only utilized by the \( \text{pj\_transform()} \) API call, not the \( \text{pj\_inv()} \) and \( \text{pj\_fwd()} \) calls. Consequently the user utility \( \text{cs2cs} \) does honour prime meridians but the \( \text{proj} \) user utility ignores them.

The following predeclared prime meridian names are supported. These can be listed using with \( \text{cs2cs -lm} \).

<table>
<thead>
<tr>
<th>Meridian</th>
<th>Longitude</th>
</tr>
</thead>
<tbody>
<tr>
<td>greenwich</td>
<td>0°E</td>
</tr>
<tr>
<td>lisbon</td>
<td>9°07'54.862°W</td>
</tr>
<tr>
<td>paris</td>
<td>2°20'14.025°E</td>
</tr>
<tr>
<td>bogota</td>
<td>7°40'51.3°E</td>
</tr>
<tr>
<td>madrid</td>
<td>3°41'16.48°W</td>
</tr>
<tr>
<td>rome</td>
<td>12°27'8.4°E</td>
</tr>
<tr>
<td>bern</td>
<td>7°26'22.5°E</td>
</tr>
<tr>
<td>jakarta</td>
<td>10°6'48'27.79°E</td>
</tr>
<tr>
<td>ferro</td>
<td>17°40°W</td>
</tr>
<tr>
<td>brussels</td>
<td>4°22'4.71°E</td>
</tr>
<tr>
<td>stockholm</td>
<td>18°3'29.8°E</td>
</tr>
<tr>
<td>athens</td>
<td>23°42'58.815°E</td>
</tr>
<tr>
<td>oslo</td>
<td>10°43'22.5°E</td>
</tr>
</tbody>
</table>

Example of use. The location \( \text{long}=0, \text{lat}=0 \) in the greenwich based lat/long coordinates is translated to lat/long coordinates with Madrid as the prime meridian.
5.2.5 Axis orientation

Starting in PROJ 4.8.0, the +axis argument can be used to control the axis orientation of the coordinate system. The default orientation is “easting, northing, up” but directions can be flipped, or axes flipped using combinations of the axes in the +axis switch. The values are:

- “e” - Easting
- “w” - Westing
- “n” - Northing
- “s” - Southing
- “u” - Up
- “d” - Down

They can be combined in +axis in forms like:

- +axis=enu - the default easting, northing, elevation.
- +axis=neu - northing, easting, up - useful for “lat/long” geographic coordinates, or south orientated transverse mercator.
- +axis=wnu - westing, northing, up - some planetary coordinate systems have “west positive” coordinate systems

**Note:** The +axis argument does not work with the proj command line utility.

5.3 Geodetic transformation

PROJ can do everything from the most simple projection to very complex transformations across many reference frames. While originally developed as a tool for cartographic projections, PROJ has over time evolved into a powerful generic coordinate transformation engine that makes it possible to do both large scale cartographic projections as well as coordinate transformation at a geodetic high precision level. This chapter delves into the details of how geodetic transformations of varying complexity can be performed.

In PROJ, two frameworks for geodetic transformations exists, the cs2cs framework and the transformation pipelines framework. The first is the original, and limited, framework for doing geodetic transforms in PROJ The latter is a newer addition that aims to be a more complete transformation framework. Both are described in the sections below. Large portions of the text are based on [EversKnudsen2017].

Before describing the details of the two frameworks, let us first remark that most cases of geodetic transformations can be expressed as a series of elementary operations, the output of one operation being the input of the next. E.g. when going from UTM zone 32, datum ED50, to UTM zone 32, datum ETRS89, one must, in the simplest case, go through 5 steps:

1. Back-project the UTM coordinates to geographic coordinates
2. Convert the geographic coordinates to 3D cartesian geocentric coordinates
3. Apply a Helmert transformation from ED50 to ETRS89
4. Convert back from cartesian to geographic coordinates
5. Finally project the geographic coordinates to UTM zone 32 planar coordinates.

5.3.1 Transformation pipelines

The homology between the above steps and a Unix shell style pipeline is evident. It is there the main architectural inspiration behind the transformation pipeline framework. The pipeline framework is realized by utilizing a special “projection”, that takes as its user supplied arguments, a series of elementary operations, which it strings together in order to implement the full transformation needed. Additionally, a number of elementary geodetic operations, including Helmert transformations, general high order polynomial shifts and the Molodensky transformation are available as part of the pipeline framework. In anticipation of upcoming support for full time-varying transformations, we also introduce a 4D spatiotemporal data type, and a programming interface (API) for handling this.

The Molodensky transformation converts directly from geodetic coordinates in one datum, to geodetic coordinates in another datum, while the (typically more accurate) Helmert transformation converts from 3D cartesian to 3D cartesian coordinates. So when using the Helmert transformation one typically needs to do an initial conversion from geodetic to cartesian coordinates, and a final conversion the other way round, to arrive at the desired result. Fortunately, this three-step compound transformation has the attractive characteristic that each step depends only on the output of the immediately preceding step. Hence, we can build a geodetic-to-geodetic Helmert transformation by tying together the outputs and inputs of 3 steps (geodetic-to-cartesian → Helmert → cartesian-to-geodetic), pipeline style. The pipeline driver, makes this kind of chained transformations possible. The implementation is compact, consisting of just one pseudo-projection, called pipeline, which takes as its arguments strings of elementary projections (note: “projection” is the, slightly misleading, PROJ term used for any kind of transformation). The pipeline pseudo projection is supplemented by a number of elementary transformations, all in all providing a framework for building high accuracy solutions for a wide spectrum of geodetic tasks.

As a first example, let us take a look at the iconic geodetic → Cartesian → Helmert → geodetic case (steps 2 to 4 in the example in the introduction). In PROJ it can be implemented as

```
proj=pipeline
step proj=cart ellps=intl
step proj=helmert convention=coordinate_frame
  x=-81.0703  y=-89.3603  z=-115.7526
  rx=-0.48488  ry=-0.02436  rz=-0.41321  s=-0.540645
step proj=cart inv ellps=GRS80
```

The pipeline can be expanded at both ends to accommodate whatever coordinate type is needed for input and output: In the example below, we transform from the deprecated Danish System 45, a 2D system with some tension in the original defining network, to UTM zone 33, ETRS89. The tension is reduced using a polynomial transformation (the init=./s45b... step, s45b.pol is a file containing the polynomial coefficients), taking the S45 coordinates to a technical coordinate system (TC32), defined to represent “UTM zone 32 coordinates, as they would look if the Helmert transformation between ED50 and ETRS89 was perfect”. The TC32 coordinates are then converted back to geodetic(ED50) coordinates, using an inverse UTM projection, further to cartesian(ED50), then to cartesian(ETRS89), using the relevant Helmert transformation, and back to geodetic(ETRS89), before finally being projected onto the UTM zone 33, ETRS89 system. All in all a 6 step pipeline, implementing a transformation with centimeter level accuracy from a deprecated system with decimeter level tensions.

```
proj=pipeline
step init=./s45b.pol:s45b_tc32
step proj=utm inv ellps=intl zone=32
step proj=cart ellps=intl
step proj=helmert convention=coordinate_frame
  x=81.0703  y=89.3603  z=-115.7526
  rx=-0.48488  ry=-0.02436  rz=-0.41321  s=-0.540645
step proj=cart inv ellps=GRS80
```

(continues on next page)
With the pipeline framework spatiotemporal transformation is possible. This is possible by leveraging the time dimension in PROJ that enables 4D coordinates (three spatial components and one temporal component) to be passed through a transformation pipeline. In the example below a transformation from ITRF93 to ITRF2000 is defined. The temporal component is given as GPS weeks in the input data, but the 14-parameter Helmert transform expects temporal units in decimal years. Hence the first step in the pipeline is the unitconvert pseudo-projection that makes sure the correct units are passed along to the Helmert transform. Most parameters of the Helmert transform are taken from [Altamimi2002], except the epoch which is the epoch of the transformation. The last step in the pipeline is converting the coordinate timestamps back to GPS weeks.

```
proj=pipeline
step proj=unitconvert t_in=gps_week t_out=decimalyear
step proj=helmert convention=coordinate_frame
  x=0.0127 y=0.0065 z=-0.0209 s=0.00195
  rx=0.00039 ry=-0.00080 rz=0.00114
  dx=-0.0029 dy=-0.0002 dz=-0.0006 ds=0.00001
  drx=0.00011 dry=0.00019 drz=-0.00007
  t_epoch=1988.0
step proj=unitconvert t_in=decimalyear t_out=gps_week
```

### 5.3.2 cs2cs paradigm

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>+datum</td>
<td>Datum name (see proj -ld)</td>
</tr>
<tr>
<td>+geoidgrids</td>
<td>Filename of GTX grid file to use for vertical datum transforms</td>
</tr>
<tr>
<td>+nadgrids</td>
<td>Filename of NTv2 grid file to use for datum transforms</td>
</tr>
<tr>
<td>+towgs84</td>
<td>3 or 7 term datum transform parameters</td>
</tr>
<tr>
<td>+to_meter</td>
<td>Multiplier to convert map units to 1.0m</td>
</tr>
<tr>
<td>+vto_meter</td>
<td>Vertical conversion to meters</td>
</tr>
</tbody>
</table>

The cs2cs framework delivers a subset of the geodetic transformations available with the pipeline framework. Coordinate transformations done in this framework are transformed in a two-step process with WGS84 as a pivot datum. That is, the input coordinates are transformed to WGS84 geodetic coordinates and then transformed from WGS84 coordinates to the specified output coordinate reference system, by utilizing either the Helmert transform, datum shift grids or a combination of both. Datum shifts can be described in a proj-string with the parameters +towgs84, +nadgrids and +geoidgrids. An inverse transform exists for all three and is applied if specified in the input proj-string. The most common is +towgs84, which is used to define a 3- or 7-parameter Helmert shift from the input reference frame to WGS84. Exactly which realization of WGS84 is not specified, hence a fair amount of uncertainty is introduced in this step of the transformation. With the +nadgrids parameter a non-linear planar correction derived from interpolation in a correction grid can be applied. Originally this was implemented as a means to transform coordinates between the North American datums NAD27 and NAD83, but corrections can be applied for any datum for which a correction grid exists. The inverse transform for the horizontal grid shift is “dumb”, in the sense that the correction grid is applied verbatim without taking into account that the inverse operation is non-linear. Similar to the horizontal grid correction, +geoidgrids can be used to perform grid corrections in the vertical component. Both grid correction methods allow inclusion of more than one grid in the same transformation.

In contrast to the transformation pipeline framework, transformations with the cs2cs framework are expressed as two separate proj-strings. One proj-string to WGS84 and one from WGS84. Together they form the mapping from the source coordinate reference system to the destination coordinate reference system. When used with the cs2cs the source and destination CRS’s are separated by the special +to parameter.
The following example demonstrates converting from the Greek GGRS87 datum to WGS84 with the \texttt{+towgs84} parameter.

\begin{verbatim}
+proj=latlong +ellps=GRS80 +towgs84=-199.87,74.79,246.62
to +proj=latlong +datum=WGS84
\end{verbatim}

20 35
20d0'5.467"E 35d0'9.575"N 0.000

The EPSG database provides this example for transforming from WGS72 to WGS84 using an approximated 7 parameter transformation.

\begin{verbatim}
+proj=latlong +ellps=WGS72 +towgs84=0,0,4.5,0,0,0.554,0.219
to +proj=latlong +datum=WGS84
\end{verbatim}

4 55
4d0'0.554"E 55d0'0.09"N 0.000

### 5.3.3 Grid Based Datum Adjustments

In many places (notably North America and Australia) national geodetic organizations provide grid shift files for converting between different datums, such as NAD27 to NAD83. These grid shift files include a shift to be applied at each grid location. Actually grid shifts are normally computed based on an interpolation between the containing four grid points.

PROJ supports use of grid files for shifting between various reference frames. The grid shift table formats are ctable, NTv1 (the old Canadian format), and NTv2 (.gsb - the new Canadian and Australian format).

The text in this section is based on the \texttt{cs2cs} framework. Gridshifting is off course also possible with the \textit{pipeline} framework. The major difference between the two is that the \texttt{cs2cs} framework is limited to grid mappings to WGS84, whereas with \textit{transformation pipelines} it is possible to perform grid shifts between any two reference frames, as long as a grid exists.

Use of grid shifts with \texttt{cs2cs} is specified using the \texttt{+nadgrids} keyword in a coordinate system definition. For example:

\begin{verbatim}
% cs2cs +proj=latlong +ellps=clrk66 +nadgrids=ntv1_can.dat 
   +to +proj=latlong +ellps=GRS80 +datum=NAD83 << EOF
-111 50
EOF
111d0'2.952"W 50d0'0.111"N 0.000
\end{verbatim}

In this case the \texttt{/usr/local/share/proj/ntv1_can.dat} grid shift file was loaded, and used to get a grid shift value for the selected point.

It is possible to list multiple grid shift files, in which case each will be tried in turn till one is found that contains the point being transformed.

\begin{verbatim}
% cs2cs +proj=latlong +ellps=clrk66 
   +nadgrids=conus,alaska,hawaii,stgeorge,stlrcn,stpaul 
   +to +proj=latlong +ellps=GRS80 +datum=NAD83 << EOF
-111 44
EOF
111d0'2.788"W 43d59'59.725"N 0.000
\end{verbatim}

### 5.3. Geodetic transformation
5.3.3.1 Skipping Missing Grids

The special prefix @ may be prefixed to a grid to make it optional. If it not found, the search will continue to the next grid. Normally any grid not found will cause an error. For instance, the following would use the ntv2_0.gsb file if available, otherwise it would fallback to using the ntv1_can.dat file.

```
cs2cs +proj=latlong +ellps=clrk66 +nadgrids=@ntv2_0.gsb,ntv1_can.dat
  +to +proj=latlong +ellps=GRS80 +datum=NAD83 << EOF
-111 50
EOF
111d0'3.006"W  50d0'0.103"N 0.000
```

5.3.3.2 The null Grid

A special null grid shift file is shift with releases after 4.4.6 (not inclusive). This file provides a zero shift for the whole world. It may be listed at the end of a nadgrids file list if you want a zero shift to be applied to points outside the valid region of all the other grids. Normally if no grid is found that contains the point to be transformed an error will occur.

```
cs2cs +proj=latlong +ellps=clrk66 +nadgrids=conus,null
  +to +proj=latlong +ellps=GRS80 +datum=NAD83 << EOF
-111 45
EOF
111d0'3.006"W  50d0'0.103"N 0.000

cs2cs +proj=latlong +ellps=clrk66 +nadgrids=conus,null
  +to +proj=latlong +ellps=GRS80 +datum=NAD83 << EOF
-111 44
-111 55
EOF
111d0'2.788"W  43d59'59.725"N 0.000
111dW   55dN 0.000
```

For more information see the chapter on Transformation grids.

5.3.3.3 Caveats

- Where grids overlap (such as conus and ntv1_can.dat for instance) the first found for a point will be used regardless of whether it is appropriate or not. So, for instance, +nadgrids=ntv1_can.dat,conus would result in the Canadian data being used for some areas in the northern United States even though the conus data is the approved data to use for the area. Careful selection of files and file order is necessary. In some cases border spanning datasets may need to be pre-segmented into Canadian and American points so they can be properly grid shifted.

- There are additional grids for shifting between NAD83 and various HPGN versions of the NAD83 datum. Use of these haven’t been tried recently so you may encounter problems. The FL.lla, WO.lla, MD.lla, TN.lla and WI.lla are examples of high precision grid shifts. Take care!

- Additional detail on the grid shift being applied can be found by setting the PROJ_DEBUG environment variable to a value. This will result in output to stderr on what grid is used to shift points, the bounds of the various grids loaded and so forth.

- The cs2cs framework always assumes that grids contain a shift to NAD83 (essentially WGS84). Other types of grids can be used with the pipeline framework.
5.4 Environment variables

PROJ can be controlled by setting environment variables. Most users will have a use for the PROJ_LIB.

On UNIX systems environment variables can be set for a shell-session with:

```bash
$ export VAR="some variable"
```

or it can be set for just one command line call:

```bash
$ VAR="some variable" ./cmd
```

Environment variables on UNIX are usually removed with the unset command:

```bash
$ unset VAR
```

On windows systems environment variables can be set in the command line with:

```bash
> set VAR="some variable"
```

`VAR` will be available for the entire session, unless it is unset. This is done by setting the variable with no content:

```bash
> set VAR=
```

**PROJ_LIB**

The location of PROJ resource files.

Starting with PROJ 6, multiple directories can be specified. On Unix, they should be separated by the colon (:) character. on Windows, by the semi-colon (;) character.

PROJ is hardcoded to look for resource files in other locations as well, amongst those are the users home directory, /usr/share/proj and the current folder.

You can also set the location of the resource files using proj_context_set_search_paths() in the proj.h API header.

Changed in version 6.1.0: Starting with PROJ version 6.1.0, the paths set by proj_context_set_search_paths() will have priority over the PROJ_LIB to allow for multiple versions of PROJ resource files on your system without conflicting.

**PROJ_DEBUG**

Set the debug level of PROJ. The default debug level is zero, which results in no debug output when using PROJ. A number from 1-3, with 3 being the most verbose setting.

5.5 Known differences between versions

Once in a while, a new version of PROJ causes changes in the existing behaviour. In this section we track deliberate changes to PROJ that break from previous behaviour. Most times that will be caused by a bug fix. Unfortunately, some bugs have existed for so long that their faulty behaviour is relied upon by software that uses PROJ.

Behavioural changes caused by new bugs are not tracked here, as they should be fixed in later versions of PROJ.
5.5.1 Version 4.6.0

The default datum application behavior changed with the 4.6.0 release. PROJ will now only apply a datum shift if both the source and destination coordinate system have valid datum shift information.

The PROJ 4.6.0 Release Notes states

MAJOR: Rework `pj_transform()` to avoid applying ellipsoid to ellipsoid transformations as a datum shift when no datum info is available.

5.5.2 Version 5.0.0

5.5.2.1 Longitude wrapping when using custom central meridian

By default PROJ wraps output longitudes in the range -180 to 180. Previous to PROJ 5, this was handled incorrectly when a custom central meridian was set with `+lon_0`. This caused a change in sign on the resulting easting as seen below:

```
$ proj +proj=merc +lon_0=110
-70 0
-20037508.34 0.00
290 0
20037508.34 0.00
```

From PROJ 5 on onwards, the same input now results in same coordinates, as seen from the example below where PROJ 5 is used:

```
$ proj +proj=merc +lon_0=110
-70 0
-20037508.34 0.00
290 0
-20037508.34 0.00
```

The change is made on the basis that $\lambda = 290^\circ$ is a full rotation of the circle larger than $\lambda = -70^\circ$ and hence should return the same output for both.

Adding the `+over` flag to the projection definition provides the old behaviour.

5.5.3 Version 6.0.0

5.5.3.1 Removal of proj_def.dat

Before PROJ 6, the `proj_def.dat` was used to provide general and per-projection parameters, when `+no_defs` was not specified. It has now been removed. In case, no ellipsoid or datum specification is provided in the PROJ string, the default ellipsoid is GRS80 (was WGS84 in previous PROJ versions).
5.5.3.2 Changes to deformation

Reversed order of operation

In the initial version of the deformation operation the time span between \( t_{obs} \) and \( t_{c} \) was determined by the expression

\[
dt = t_{c} - t_{obs}
\]

With version 6.0.0 this has been reversed in order to behave similarly to the Helmert operation, which determines time differences as

\[
dt = t_{obs} - t_{c}
\]

Effectively this means that the direction of the operation has been reversed, so that what in PROJ 5 was a forward operation is now an inverse operation and vice versa.

Pipelines written for PROJ 5 can be migrated to PROJ 6 by adding \texttt{+inv} to forward steps involving the deformation operation. Similarly \texttt{+inv} should be removed from inverse steps to be compatible with PROJ 6.

Removed \texttt{+t\_obs} parameter

The \texttt{+t\_obs} parameter was confusing for users since it effectively overwrote the observation time in input coordinates. To make it more clear what is the operation is doing, users are now required to directly specify the time span for which they wish to apply a given deformation. The parameter \texttt{+dt} has been added for that purpose. The new parameter is mutually exclusive with \texttt{+t\_epoch}. \texttt{+dt} is used when deformation for a set amount of time is needed and \texttt{+t\_epoch} is used (in conjunction with the observation time of the input coordinate) when deformation from a specific epoch to the observation time is needed.
Bundled with PROJ comes a set of small command line utilities. The `proj` program is limited to converting between geographic and projection coordinates within one datum. The `cs2cs` program operates similarly, but allows translation between any pair of definable coordinate systems, including support for datum transformation. The `geod` program provides the ability to do geodesic (great circle) computations. `gie` is the program used for regression tests in PROJ. `cct`, a 4D equivalent to the `proj` program, performs transformation coordinate systems on a set of input points. `projinfo` performs queries for geodetic objects and coordinate operations.

6.1 cct

6.1.1 Synopsis

```
cct [-cIostvz [args]] +opt[=arg] . . . file . . .
```

6.1.2 Description

cct a 4D equivalent to the `proj` projection program, performs transformation coordinate systems on a set of input points. The coordinate system transformation can include translation between projected and geographic coordinates as well as the application of datum shifts.

The following control parameters can appear in any order:

- `<c>` `<x,y,z,t>`
  Specify input columns for (up to) 4 input parameters. Defaults to 1,2,3,4.

- `<d>` `<n>`
  New in version 5.2.0: Specify the number of decimals in the output.

- `<I>`
  Do the inverse transformation.

- `<o>` `<output file name>, --output=<output file name>`
  Specify the name of the output file.

- `<t>` `<time>, --time=<time>`
  Specify a fixed observation `time` to be used for all input data.

- `<z>` `<height>, --height=<height>`
  Specify a fixed observation `height` to be used for all input data.

- `<s>` `<n>, --skip-lines=<n>`
  New in version 5.1.0.
Skip the first \( n \) lines of input. This applies to any kind of input, whether it comes from STDIN, a file or interactive user input.

- \( v \),\, \texttt{--verbose}  
  Write non-essential, but potentially useful, information to stderr. Repeat for additional information (\( -vv, -vvv \), etc.)

\texttt{--version}  
Print version number.

The \( +opt \) arguments are associated with coordinate operation parameters. Usage varies with operation.

\texttt{cct} is an acronym meaning \textit{Coordinate Conversion and Transformation}.

The acronym refers to definitions given in the OGC 08-015r2/ISO-19111 standard “Geographical Information – Spatial Referencing by Coordinates”, which defines two different classes of \textit{coordinate operations}:

\textit{Coordinate Conversions}, which are coordinate operations where input and output datum are identical (e.g. conversion from geographical to cartesian coordinates) and

\textit{Coordinate Transformations}, which are coordinate operations where input and output datums differ (e.g. change of reference frame).

### 6.1.3 Examples

1. The operator specs describe the action to be performed by \texttt{cct}. So the following script

   \begin{verbatim}
   echo 12 55 0 0 | cct +proj=utm +zone=32 +ellps=GRS80
   \end{verbatim}

   will transform the input geographic coordinates into UTM zone 32 coordinates. Hence, the command

   \begin{verbatim}
   echo 12 55 | cct -z0 -t0 +proj=utm +zone=32 +ellps=GRS80
   \end{verbatim}

   Should give results comparable to the classic \texttt{proj} command

   \begin{verbatim}
   echo 12 55 | proj +proj=utm +zone=32 +ellps=GRS80
   \end{verbatim}

2. Convert geographical input to UTM zone 32 on the GRS80 ellipsoid:

   \begin{verbatim}
   cct +proj=utm +ellps=GRS80 +zone=32
   \end{verbatim}

3. Roundtrip accuracy check for the case above:

   \begin{verbatim}
   cct +proj=pipeline +proj=utm +ellps=GRS80 +zone=32 +step +step +inv
   \end{verbatim}

4. As (2) but specify input columns for longitude, latitude, height and time:

   \begin{verbatim}
   cct -c 5,2,1,4 +proj=utm +ellps=GRS80 +zone=32
   \end{verbatim}

5. As (2) but specify fixed height and time, hence needing only 2 cols in input:

   \begin{verbatim}
   cct -t 0 -z 0 +proj=utm +ellps=GRS80 +zone=32
   \end{verbatim}

6. Auxiliary data following the coordinate input is forward to the output stream:

   \begin{verbatim}
   $ echo 12 56 100 2018.0 auxiliary data | cct +proj=merc
   1335833.8895  7522963.2411  100.0000  2018.0000 auxiliary data
   \end{verbatim}
6.1.4 Background

cct also refers to Carl Christian Tscherning (1942–2014), professor of Geodesy at the University of Copenhagen, mentor and advisor for a generation of Danish geodesists, colleague and collaborator for two generations of global geodesists, Secretary General for the International Association of Geodesy, IAG (1995–2007), fellow of the American Geophysical Union (1991), recipient of the IAG Levallois Medal (2007), the European Geosciences Union Vening Meinesz Medal (2008), and of numerous other honours.

cct, or Christian, as he was known to most of us, was recognized for his good mood, his sharp wit, his tireless work, and his great commitment to the development of geodesy – both through his scientific contributions, comprising more than 250 publications, and by his mentoring and teaching of the next generations of geodesists.

As Christian was an avid Fortran programmer, and a keen Unix connoisseur, he would have enjoyed to know that his initials would be used to name a modest Unix style transformation filter, hinting at the tireless aspect of his personality, which was certainly one of the reasons he accomplished so much, and meant so much to so many people.

Hence, in honour of cct (the geodesist) this is cct (the program).

6.2 cs2cs

6.2.1 Synopsis

```
cs2cs [-eEflrstvwW [args]] [+opt[=arg] ...] [+to opt[=arg] ...] file ...
```

or

```
cs2cs [-eEflrstvwW [args]] {source_crs} +to {target_crs} file ...
```

where {source_crs} or {target_crs} is a PROJ string, a WKT string or a AUTHORITY:CODE (where AUTHORITY is the name of a CRS authority and CODE the code of a CRS found in the proj.db database), expressing a coordinate reference system.

New in version 6.0.0.

or

```
cs2cs [-eEflrstvwW [args]] {source_crs} {target_crs}
```

New in version 6.0.0.

6.2.2 Description

cs2cs performs transformation between the source and destination cartographic coordinate reference system on a set of input points. The coordinate reference system transformation can include translation between projected and geographic coordinates as well as the application of datum shifts.

The following control parameters can appear in any order:

- **-I**
  Method to specify inverse translation, convert from +to coordinate system to the primary coordinate system defined.

- **-t<a>**
  Where a specifies a character employed as the first character to denote a control line to be passed through without processing. This option applicable to ASCII input only. (# is the default value).

- **-d <n>**
  New in version 5.2.0: Specify the number of decimals in the output.
PROJ coordinate transformation software library, Release 6.1.1

- e <string>
  Where string is an arbitrary string to be output if an error is detected during data transformations. The default value is a three character string: *\t*.

- E
  Causes the input coordinates to be copied to the output line prior to printing the converted values.

- l<[=id]>
  List projection identifiers that can be selected with +proj. cs2cs -l=id gives expanded description of projection id, e.g. cs2cs -l=merc.

- lp
  List of all projection id that can be used with the +proj parameter. Equivalent to cs2cs -l.

- lP
  Expanded description of all projections that can be used with the +proj parameter.

- le
  List of all ellipsoids that can be selected with the +ellps parameters.

- lu
  List of all distance units that can be selected with the +units parameter.

- ld
  List of datums that can be selected with the +datum parameter.

- r
  This options reverses the order of the expected input from longitude-latitude or x-y to latitude-longitude or y-x.

- s
  This options reverses the order of the output from x-y or longitude-latitude to y-x or latitude-longitude.

- f <format>
  Where format is a printf format string to control the form of the output values. For inverse projections, the output will be in degrees when this option is employed. If a format is specified for inverse projection the output data will be in decimal degrees. The default format is "%.2f" for forward projection and DMS for inverse.

- w<n>
  Where n is the number of significant fractional digits to employ for seconds output (when the option is not specified, -w3 is assumed).

- W<n>
  Where n is the number of significant fractional digits to employ for seconds output. When -W is employed the fields will be constant width with leading zeroes.

- v
  Causes a listing of cartographic control parameters tested for and used by the program to be printed prior to input data.

The cs2cs program requires two coordinate reference system (CRS) definitions. The first (or primary is defined based on all projection parameters not appearing after the +to argument. All projection parameters appearing after the +to argument are considered the definition of the second CRS. If there is no second CRS defined, a geographic CRS based on the datum and ellipsoid of the source CRS is assumed. Note that the source and destination CRS can both of same or different nature (geographic, projected, compound CRS), or one of each and may have the same or different datums.

When using a WKT definition or a AUTHORITY:CODE, the axis order of the CRS will be enforced. So for example if using EPSG:4326, the first value expected (or returned) will be a latitude.

Internally, cs2cs uses the proj_create_crs_to_crs() function to compute the appropriate coordinate operation, so implementation details of this function directly impact the results returned by the program.
The environment parameter `PROJ_LIB` establishes the directory for resource files (database, datum shift grids, etc.)

One or more files (processed in left to right order) specify the source of data to be transformed. A `-` will specify the location of processing standard input. If no files are specified, the input is assumed to be from stdin. For input data the two data values must be in the first two white space separated fields and when both input and output are ASCII all trailing portions of the input line are appended to the output line.

Input geographic data (longitude and latitude) must be in DMS or decimal degrees format and input cartesian data must be in units consistent with the ellipsoid major axis or sphere radius units. Output geographic coordinates will normally be in DMS format (use `-f %.12f` for decimal degrees with 12 decimal places), while projected (cartesian) coordinates will be in linear (meter, feet) units.

### 6.2.3 Examples

#### 6.2.3.1 Using PROJ strings

The following script

```
cs2cs +proj=latlong +datum=NAD83 +to +proj=utm +zone=10 +datum=NAD27 -r <<EOF
45d15'33.1" 111.5W
45d15.551666667N -111d30
+45.25919444444 111d30'000w
EOF
```

will transform the input NAD83 geographic coordinates into NAD27 coordinates in the UTM projection with zone 10 selected. The geographic values of this example are equivalent and meant as examples of various forms of DMS input. The x-y output data will appear as three lines of:

```
1402293.44 5076292.68 0.00
```

#### 6.2.3.2 Using EPSG codes

Transforming from WGS 84 latitude/longitude (in that order) to UTM Zone 31N/WGS 84

```
cs2cs EPSG:4326 EPSG:32631 <<EOF
45N 2E
EOF
```

outputs

```
421184.70 4983436.77 0.00
```

### 6.3 geod

#### 6.3.1 Synopsis

```
geod +ellps=<ellipse> [-affIlptwW [args]] [+optl=arg] ... file ... 
invgeod +ellps=<ellipse> [-affIlptwW [args]] [+optl=arg] ... file ... 
```

6.3. geod
6.3.2 Description

**geod** (direct) and **invgeod** (inverse) perform geodesic (Great Circle) computations for determining latitude, longitude and back azimuth of a terminus point given an initial point latitude, longitude, azimuth and distance (direct) or the forward and back azimuths and distance between an initial and terminus point latitudes and longitudes (inverse). The results are accurate to round off for $|f| < 1/50$, where $f$ is flattening.

**invgeod** may not be available on all platforms; in this case use **geod -I** instead.

The following command-line options can appear in any order:

- **-I**
  Specifies that the inverse geodesic computation is to be performed. May be used with execution of **geod** as an alternative to **invgeod** execution.

- **-a**
  Latitude and longitudes of the initial and terminal points, forward and back azimuths and distance are output.

- **-t<a>**
  Where $a$ specifies a character employed as the first character to denote a control line to be passed through without processing.

- **-le**
  Gives a listing of all the ellipsoids that may be selected with the **+ellps=** option.

- **-lu**
  Gives a listing of all the units that may be selected with the **+units=** option.

- **-f <format>**
  Where format is a printf format string to control the output form of the geographic coordinate values. The default mode is DMS for geographic coordinates and "%.3f" for distance.

- **-F <format>**
  Where format is a printf format string to control the output form of the distance value (−F). The default mode is DMS for geographic coordinates and "%.3f" for distance.

- **-w<n>**
  Where $n$ is the number of significant fractional digits to employ for seconds output (when the option is not specified, −w3 is assumed).

- **-W<n>**
  Where $n$ is the number of significant fractional digits to employ for seconds output. When −W is employed the fields will be constant width with leading zeroes.

- **-p**
  This option causes the azimuthal values to be output as unsigned DMS numbers between 0 and 360 degrees. Also note −f.

The **+opt** command-line options are associated with geodetic parameters for specifying the ellipsoidal or sphere to use. The options are processed in left to right order from the command line. Reentry of an option is ignored with the first occurrence assumed to be the desired value.

One or more files (processed in left to right order) specify the source of data to be transformed. A − will specify the location of processing standard input. If no files are specified, the input is assumed to be from stdin.

For direct determinations input data must be in latitude, longitude, azimuth and distance order and output will be latitude, longitude and back azimuth of the terminus point. Latitude, longitude of the initial and terminus point are input for the inverse mode and respective forward and back azimuth from the initial and terminus points are output along with the distance between the points.

Input geographic coordinates (latitude and longitude) and azimuthal data must be in decimal degrees or DMS format and input distance data must be in units consistent with the ellipsoid major axis or sphere radius units. The latitude
must lie in the range \([-90d,90d]\). Output geographic coordinates will be in DMS (if the \(-\ell\) switch is not employed) to 0.001" with trailing, zero-valued minute-second fields deleted. Output distance data will be in the same units as the ellipsoid or sphere radius.

The Earth’s ellipsoidal figure may be selected in the same manner as program \texttt{proj} by using \texttt{+ellps=}, \texttt{+a=}, \texttt{+es=} etc.

\texttt{geod} may also be used to determine intermediate points along either a geodesic line between two points or along an arc of specified distance from a geographic point. In both cases an initial point must be specified with \texttt{+lat_1=} \texttt{lat} and \texttt{+lon_1=} \texttt{lon} parameters and either a terminus point \texttt{+lat_2=} \texttt{lat} and \texttt{+lon_2=} \texttt{lon} or a distance and azimuth from the initial point with \texttt{+S=} \texttt{distance} and \texttt{+A=} \texttt{azimuth} must be specified.

If points along a geodesic are to be determined then either \texttt{+n_S=} \texttt{integer} specifying the number of intermediate points and/or \texttt{+del_S=} \texttt{distance} specifying the incremental distance between points must be specified.

To determine points along an arc equidistant from the initial point both \texttt{+del_A=} \texttt{angle} and \texttt{+n_A=} \texttt{integer} must be specified which determine the respective angular increments and number of points to be determined.

### 6.3.3 Examples

The following script determines the geodesic azimuths and distance in U.S. statute miles from Boston, MA, to Portland, OR:

```
geod +ellps=clrk66 <<EOF -I +units=us-mi
42d15'N 71d07'W 45d31'N 123d41'W
EOF
```

which gives the results:

```
-66d31'50.141" 75d39'13.083" 2587.504
```

where the first two values are the azimuth from Boston to Portland, the back azimuth from Portland to Boston followed by the distance.

An example of forward geodesic use is to use the Boston location and determine Portland’s location by azimuth and distance:

```
geod +ellps=clrk66 <<EOF +units=us-mi
42d15'N 71d07'W -66d31'50.141" 2587.504
EOF
```

which gives:

```
45d31'0.003"N 123d40'59.985"W 75d39'13.094"
```

**Note:** Lack of precision in the distance value compromises the precision of the Portland location.
6.3.4 Further reading

1. GeographicLib.
3. A geodesic bibliography.

6.4 gie

6.4.1 Synopsis

gie [ -hovql [ args ] ] file[s]

6.4.2 Description

gie, the Geospatial Integrity Investigation Environment, is a regression testing environment for the PROJ transformation library. Its primary design goal is to be able to perform regression testing of code that are a part of PROJ, while not requiring any other kind of tooling than the same C compiler already employed for compiling the library.

-h, --help
Print usage information

-o <file>, --output <file>
Specify output file name

-v, --verbose
Verbose: Provide non-essential informational output. Repeat -v for more verbosity (e.g. -vv)

-q, --quiet
Quiet: Opposite of verbose. In quiet mode not even errors are reported. Only interaction is through the return code (0 on success, non-zero indicates number of FAILED tests)

-l, --list
List the PROJ internal system error codes

--version
Print version number

Tests for gie are defined in simple text files. Usually having the extension .gie. Test for gie are written in the purpose-build command language for gie. The basic functionality of the gie command language is implemented through just 3 command verbs: operation, which defines the PROJ operation to test, accept, which defines the input coordinate to read, and expect, which defines the result to expect.

A sample test file for gie that uses the three above basic commands looks like:

```gie
--------------------------------------------
Test output of the UTM projection
--------------------------------------------
operation +proj=utm +zone=32 +ellps=GRS80
--------------------------------------------
accept 12 55
expect 691_875.632_14 6_098_907.825_05
</gie>
```
Parsing of a `gie` file starts at `<gie>` and ends when `</gie>` is reached. Anything before `<gie>` and after `</gie>` is not considered. Test cases are created by defining an `operation` which `accept` an input coordinate and `expect` an output coordinate.

Because `gie` tests are wrapped in the `<gie>` tags it is also possible to add test cases to custom made `init` files. The tests will be ignore by PROJ when reading the init file with `+init` and `gie` ignores anything not wrapped in `<gie>`.</`

`gie` tests are defined by a set of commands like `operation`, `accept` and `expect` in the example above. Together the commands make out the `gie` command language. Any line in a `gie` file that does not start with a command is ignored. In the example above it is seen how this can be used to add comments and styling to `gie` test files in order to make them more readable as well as documenting what the purpose of the various tests are.

Below the `gie command language` is explained in details.

### 6.4.3 Examples

1. Run all tests in a file with all debug information turned on

```bash
gie -vvvv corner-cases.gie
```

2. Run all tests in several files

```bash
gie foo bar
```

### 6.4.4 gie command language

**operation `<+args>`**

Define a PROJ operation to test. Example:

```bash
operation proj=utm zone=32 ellps=GRS80
# test 4D function
accept 12 55 0 0
expect 691875.63214 6098907.82501 0 0
# test 2D function
accept 12 56
expect 687071.4391 6210141.3267
```

**accept `<x y [z [t]]>`**

Define the input coordinate to read. Takes test coordinate. The coordinate can be defined by either 2, 3 or 4 values, where the first two values are the x- and y-components, the 3rd is the z-component and the 4th is the time component. The number of components in the coordinate determines which version of the operation is tested (2D, 3D or 4D). Many coordinates can be accepted for one `operation`. For each `accept` an accompanying `expect` is needed.

Note that `gie` accepts the underscore (\_) as a thousands separator. It is not required (in fact, it is entirely ignored by the input routine), but it significantly improves the readability of the very long strings of numbers typically required in projected coordinates.

See `operation` for an example.

**expect `<x y [z [t]]>` | `<error code>`**

Define the expected coordinate that will be returned from accepted coordinate passed though an operation. The expected coordinate can be defined by either 2, 3 or 4 components, similarly to `accept`. Many coordinates can be expected for one `operation`. For each `expect` an accompanying `accept` is needed.
See *operation* for an example.

In addition to expecting a coordinate it is also possible to expect a PROJ error code in case an operation can’t be created. This is useful when testing that errors are caught and handled correctly. Below is an example of that tests that the pipeline operator fails correctly when a non-invertible pipeline is constructed.

```
op  
operation proj=pipeline step
  proj=urm5 n=0.5 inv
expect failure pjd_err_malformed_pipeline
```

See *gie --list* for a list of error codes that can be expected.

**tolerance <tolerance>**

The *tolerance* command controls how much accepted coordinates can deviate from the expected coordinate. This is handy to test that an operation meets a certain numerical tolerance threshold. Some operations are expected to be accurate within millimeters where others might only be accurate within a few meters. *tolerance should*

```
op  
operation proj=merc
  # test coordinate as returned by ``echo 12 55 | proj +proj=merc``
tolerance 1 cm
accept 12 55
expect 1335833.89 7326837.72
  
  # test that the same coordinate with a 50 m false easting as determined
  # by ``echo 12 55 | proj +proj=merc +x_0=50`` is still within a 100 m
tolerance 100 m
accept 12 55
expect 1335883.89 7326837.72
```

The default tolerance is 0.5 mm. See *proj --lu* for a list of possible units.

**roundtrip <n> <tolerance>**

Do a roundtrip test of an operation. *roundtrip* needs a *operation* and a *accept* command to function. The accepted coordinate is passed to the operation first in it’s forward mode, then the output from the forward operation is passed back to the inverse operation. This procedure is done *n* times. If the resulting coordinate is within the set tolerance of the initial coordinate, the test is passed.

Example with the default 100 iterations and the default tolerance:

```
op  
operation proj=merc
accept 12 55
roundtrip
```

Example with count and default tolerance:

```
op  
operation proj=merc
accept 12 55
roundtrip 10000
```

Example with count and tolerance:

```
op  
operation proj=merc
accept 12 55
roundtrip 100000 5 mm
```

**direction <direction>**

The *direction* command specifies in which direction an operation is performed. This can either be forward
or inverse. An example of this is seen below where it is tested that a symmetrical transformation pipeline returns the same results in both directions.

```plaintext
operation proj=pipeline zone=32 step
    proj=utm ellps=GRS80 step
    proj=utm ellps=GRS80 inv
tolerance 0.1 mm
accept 12 55 0 0
expect 12 55 0 0

# Now the inverse direction (still same result: the pipeline is symmetrical)
direction inverse
expect 12 55 0 0
```

The default direction is “forward”.

**ignore** <error code>
This is especially useful in test cases that rely on a grid that is not guaranteed to be available. Below is an example of that situation.

```plaintext
operation proj=hgridshift +grids=nzgd2kgrid0005.gsb ellps=GRS80
tolerance 1 mm
ignore pjd_err_failed_to_load_grid
accept 172.999892181021551 -45.001620431954613
expect 173 -45
```

See **gie --list** for a list of error codes that can be ignored.

**require_grid** <grid_name>
Checks the availability of the grid <grid_name>. If it is not found, then all accept/expect pairs until the next operation will be skipped. require_grid can be repeated several times to specify several grids whose presence is required.

**echo** <text>
Add user defined text to the output stream. See the example below.

```plaintext
<gie>
echo ** Mercator projection tests **
operation +proj=merc
accept 0 0
expect 0 0
</gie>
```

which returns

```
Reading file 'test.gie'
** Mercator projection test **
-----------------------------------------------
total: 1 tests succeeded, 0 tests skipped, 0 tests failed.
-----------------------------------------------
```

**skip**
Skip any test after the first occurrence of **skip**. In the example below only the first test will be performed. The second test is skipped. This feature is mostly relevant for debugging when writing new test cases.
6.4.5 Background

More importantly than being an acronym for “Geospatial Integrity Investigation Environment”, gie were also the initials, user id, and USGS email address of Gerald Ian Evenden (1935–2016), the geospatial visionary, who, already in the 1980s, started what was to become the PROJ of today.

Gerald’s clear vision was that map projections are just special functions. Some of them rather complex, most of them of two variables, but all of them just special functions, and not particularly more special than the \( \sin() \), \( \cos() \), \( \tan() \), and \( \text{hypot}() \) already available in the C standard library.

And hence, according to Gerald, they should not be particularly much harder to use, for a programmer, than the \( \sin() \)’s, \( \tan() \)’s and \( \text{hypot}() \)’s so readily available.

Gerald’s ingenuity also showed in the implementation of the vision, where he devised a comprehensive, yet simple, system of key-value pairs for parameterising a map projection, and the highly flexible \( PJ \) struct, storing run-time compiled versions of those key-value pairs, hence making a map projection function call, \( \text{pj_fwd}(PJ, \text{point}) \), as easy as a traditional function call like \( \text{hypot}(x, y) \).

While today, we may have more formally well defined metadata systems (most prominent the OGC WKT2 representation), nothing comes close being as easily readable (“human compatible”) as Gerald’s key-value system. This system in particular, and the PROJ system in general, was Gerald’s great gift to anyone using and/or communicating about geodata.

It is only reasonable to name a program, keeping an eye on the integrity of the PROJ system, in honour of Gerald.

So in honour, and hopefully also in the spirit, of Gerald Ian Evenden (1935–2016), this is the Geospatial Integrity Investigation Environment.

6.5 proj

6.5.1 Synopsis

\[
\text{proj [-beEfIllmorsStTvVwW] [args]] [+opt[=arg] . . .] file . . .}
\]

\[
\text{invproj [-beEfIllmorsStTvVwW] [args]] [+opt[=arg] . . .] file . . .}
\]
6.5.2 Description

`proj` and `invproj` perform respective forward and inverse conversion of cartographic data to or from cartesian data with a wide range of selectable projection functions.

`invproj` may not be available on all platforms; in this case use `proj -I` instead.

The following control parameters can appear in any order:

- **-b**
  Special option for binary coordinate data input and output through standard input and standard output. Data is assumed to be in system type double floating point words. This option is to be used when `proj` is a child process and allows bypassing formatting operations.

- **-d <n>**
  New in version 5.2.0: Specify the number of decimals in the output.

- **-i**
  Selects binary input only (see `-b`).

- **-I**
  Alternate method to specify inverse projection. Redundant when used with `invproj`.

- **-o**
  Selects binary output only (see `-b`).

- **-t <a>**
  Where `a` specifies a character employed as the first character to denote a control line to be passed through without processing. This option applicable to ASCII input only. (# is the default value).

- **-e <string>**
  Where `string` is an arbitrary string to be output if an error is detected during data transformations. The default value is a three character string: *\t*. Note that if the `-b`, `-i` or `-o` options are employed, an error is returned as HUGE_VAL value for both return values.

- **-E**
  Causes the input coordinates to be copied to the output line prior to printing the converted values.

- **-l[=id]**
  List projection identifiers that can be selected with `+proj`. For example, `proj -l=merc` gives expanded description of projection `merc`.

- **-lp**
  List of all projection id that can be used with the `+proj` parameter. Equivalent to `proj -l`.

- **-lp**
  Expanded description of all projections that can be used with the `+proj` parameter.

- **-le**
  List of all ellipsoids that can be selected with the `+ellps` parameters.

- **-lu**
  List of all distance units that can be selected with the `+units` parameter.

- **-ld**
  List of datums that can be selected with the `+datum` parameter.

- **-r**
  This option reverses the order of the expected input from longitude-latitude or x-y to latitude-longitude or y-x.

- **-s**
  This option reverses the order of the output from x-y or longitude-latitude to y-x or latitude-longitude.
Causes estimation of meridional and parallel scale factors, area scale factor and angular distortion, and maximum and minimum scale factors to be listed between <> for each input point. For conformal projections meridional and parallel scales factors will be equal and angular distortion zero. Equal area projections will have an area factor of 1.

The cartesian data may be scaled by the mult parameter. When processing data in a forward projection mode the cartesian output values are multiplied by mult otherwise the input cartesian values are divided by mult before inverse projection. If the first two characters of mult are 1/ or 1: then the reciprocal value of mult is employed.

Where format is a printf format string to control the form of the output values. For inverse projections, the output will be in degrees when this option is employed. The default format is "%.2f" for forward projection and DMS for inverse.

Where n is the number of significant fractional digits to employ for seconds output (when the option is not specified, −w3 is assumed).

Where n is the number of significant fractional digits to employ for seconds output. When −w is employed the fields will be constant width with leading zeroes.

Causes a listing of cartographic control parameters tested for and used by the program to be printed prior to input data.

This option causes an expanded annotated listing of the characteristics of the projected point. −v is implied with this option.

The +opt run-line arguments are associated with cartographic parameters. Additional projection control parameters may be contained in two auxiliary control files: the first is optionally referenced with the +init=file:id and the second is always processed after the name of the projection has been established from either the run-line or the contents of +init file. The environment parameter PROJ_LIB establishes the default directory for a file reference without an absolute path. This is also used for supporting files like datum shift files.

One or more files (processed in left to right order) specify the source of data to be converted. A − will specify the location of processing standard input. If no files are specified, the input is assumed to be from stdin. For ASCII input data the two data values must be in the first two white space separated fields and when both input and output are ASCII all trailing portions of the input line are appended to the output line.

Input geographic data (longitude and latitude) must be in DMS format and input cartesian data must be in units consistent with the ellipsoid major axis or sphere radius units. Output geographic coordinates will be in DMS (if the −w switch is not employed) and precise to 0.001” with trailing, zero-valued minute-second fields deleted.

6.5.3 Example

The following script

```bash
proj +proj=utm +lon_0=112w +ellps=clrk66 -r <<EOF
45d15'33.1" 111.5W
45d15.551666667N -111d30
+45.2591944444 111d30'000w
EOF
```
will perform UTM forward projection with a standard UTM central meridian nearest longitude 112W. The geographic values of this example are equivalent and meant as examples of various forms of DMS input. The x-y output data will appear as three lines of:

| 460769.27 | 5011648.45 |

6.6 projinfo

6.6.1 Synopsis

projinfo

[-o formats] [-k crosoperationellipsoid] [--summary] [-q]
[[-area name_or_code] | [-bbox west_long,south_lat,east_long,north_lat]]
[--spatial-test contains|intersects]
[--crs-extent-use none|both|intersection|smallest]
[--grid-check nonel discard_missing|sort] [--show-superseded]
[--pivot-crs always|no_direct_transformation|never]{auth:code[,auth:code]*}
[--boundcrs-to-wgs84]
[--main-db-path path] [--aux-db-path path]*
[--identify]
[[-c-ify] [-single-line]

{object_definition} | {object_reference} | (-s {srs_def} -t {srs_def})

where {object_definition} or {srs_def} is

- a proj-string,
- a WKT string,
- a OGC URN combining references for compound coordinate reference systems (e.g. “urn:ogc:def:crs,crs:EPSG::2393,crs:EPSG::5717” or custom abbreviated syntax “EPSG:2393+5717”),
- a OGC URN combining references for concatenated operations (e.g. “urn:ogc:def:coordinateOperation,coordinateOperation:EPSG::3895,coordinateOperation:EPSG::1618”)

{object_reference} is a filename preceded with the ‘@’ character. The file referenced by the {object_reference} must contain a valid {object_definition}.

6.6.2 Description

projinfo is a program that can query information on a geodetic object, coordinate reference system (CRS) or coordinate operation, when the -s and -t options are specified, and display it under different formats (PROJ string, WKT string).

It can also be used to query coordinate operations available between two CRS.

The program is named with some reference to the GDAL gdalsrsinfo that offers partly similar services.

The following control parameters can appear in any order:

6.6. projinfo
-o formats
   formats is a comma separated combination of: all, default, PROJ, WKT_ALL, WKT2_2015, WKT2_2018, WKT1_GDAL, WKT1_ESRI.

   Except all and default, other formats can be preceded by - to disable them.

-k crs|operation|ellipsoid
   When used to query a single object with a AUTHORITY:CODE, determines the (k)ind of the object in case there are CRS, coordinate operations or ellipsoids with the same CODE. The default is crs.

--summary
   When listing coordinate operations available between 2 CRS, return the result in a summary format, mentioning only the name of the coordinate operation, its accuracy and its area of use.

   Note: only used for coordinate operation computation

-q
   Turn on quiet mode. Quiet mode is only available for queries on single objects, and only one output format is selected. In that mode, only the PROJ or WKT string is displayed, without other introduction output. The output is then potentially compatible of being piped in other utilities.

--area name_or_code
   Specify an area of interest to restrict the results when researching coordinate operations between 2 CRS. The area of interest can be specified either as a name (e.g “Denmark - onshore”) or a AUTHORITY:CODE (EPSG:3237)
   This option is exclusive of --bbox.

   Note: only used for coordinate operation computation

--bbox west_long, south_lat, east_long, north_lat
   Specify an area of interest to restrict the results when researching coordinate operations between 2 CRS. The area of interest is specified as a bounding box with geographic coordinates, expressed in degrees in a unspecified geographic CRS. west_long and east_long should be in the [-180,180] range, and south_lat and north_lat in the [-90,90]. west_long is generally lower than east_long, except in the case where the area of interest crosses the antimeridian.

   Note: only used for coordinate operation computation

--spatial-test contains|intersects
   Specify how the area of use of coordinate operations found in the database are compared to the area of use specified explicitly with --area or --bbox, or derived implicitly from the area of use of the source and target CRS. By default, projinfo will only keep coordinate operations whose are of use is strictly within the area of interest (contains strategy). If using the intersects strategy, the spatial test is relaxed, and any coordinate operation whose area of use at least partly intersects the area of interest is listed.

   Note: only used for coordinate operation computation

--crs-extent-use none|both|intersection|smallest
   Specify which area of interest to consider when no explicit one is specified with --area or --bbox options. By default (smallest strategy), the area of use of the source or target CRS will be looked, and the one that is the smallest one in terms of area will be used as the area of interest. If using none, no area of interest is used. If using both, only coordinate operations that relate (contain or intersect depending of the --spatial-test
strategy) to the area of use of both CRS are selected. If using intersection, the area of interest is the intersection of the bounding box of the area of use of the source and target CRS.

**Note:** only used for coordinate operation computation

```
--grid-check none|discard_missing|sort
```

Specify how the presence or absence of a horizontal or vertical shift grid required for a coordinate operation affects the results returned when researching coordinate operations between 2 CRS. The default strategy is sort: in that case, all candidate operations are returned, but the actual availability of the grids is used to determine the sorting order. That is, if a coordinate operation involves using a grid that is not available in the PROJ resource directories (determined by the `PROJ_LIB` environment variable, it will be listed in the bottom of the results. The none strategy completely disables the checks of presence of grids and this returns the results as if all the grids where available. The discard_missing strategy discards results that involve grids not present in the PROJ resource directories.

**Note:** only used for coordinate operation computation

```
--show-superseded
```

When enabled, coordinate operations that are superseded by others will be listed. Note that supersession is not equivalent to deprecation: superseded operations are still considered valid although they have a better equivalent, whereas deprecated operations have been determined to be erroneous and are not considered at all.

**Note:** only used for coordinate operation computation

```
--pivot-crs always|if_no_direct_transformation|never|{auth:code[,auth:code]*}
```

Determine if intermediate (pivot) CRS can be used when researching coordinate operation between 2 CRS. A typical example is the WGS84 pivot. By default, projinfo will consider any potential pivot if there is no direct transformation (if_no_direct_transformation). If using the never strategy, only direct transformations between the source and target CRS will be used. If using the always strategy, intermediate CRS will be considered even if there are direct transformations. It is also possible to restrict the pivot CRS to consider by specifying one or several CRS by their AUTHORITY:CODE.

**Note:** only used for coordinate operation computation

```
--boundcrs-to-wgs84
```

When specified, this option researches a coordinate operation from the base geographic CRS of the single CRS, source or target CRS to the WGS84 geographic CRS, and if found, wraps those CRS into a BoundCRS object. This is mostly to be used for early-binding approaches.

```
--main-db-path path
```

Specify the name and path of the database to be used by projinfo. The default is proj.db in the PROJ resource directories.

```
--aux-db-path path
```

Specify the name and path of auxiliary databases, that are to be combined with the main database. Those auxiliary databases must have a table structure that is identical to the main database, but can be partly filled and their entries can refer to entries of the main database. The option may be repeated to specify several auxiliary databases.

```
--identify
```

When used with an object definition, this queries the PROJ database to find known objects, typically CRS,
that are close or identical to the object. Each candidate object is associated with an approximate likelihood percentage. This is useful when used with a WKT string that lacks an EPSG identifier, such as ESRI WKT1. This might also be used with PROJ strings. For example, \texttt{+proj=utm +zone=31 +datum=WGS84 +type=crs} will be identified with a likelihood of 70\% to EPSG:32631

\texttt{--c-ify}  
For developers only. Modify the string output of the utility so that it is easy to put those strings in C/C++ code

\texttt{--single-line}  
Output WKT strings on a single line, instead of multiple intended lines by default.

### 6.6.3 Examples

1. Query the CRS object corresponding to EPSG:4326

   \begin{verbatim}
   projinfo EPSG:4326
   \end{verbatim}

   Output:

   \begin{verbatim}
   PROJ.4 string:
   +proj=longlat +datum=WGS84 +no_defs +type=crs
   WKT2_2018 string:
   GEOGCRS["WGS 84",
   DATUM["World Geodetic System 1984",
   ELLIPSOID["WGS 84",6378137,298.257223563,
   LENGTHUNIT["metre",1]],
   PRIMEM["Greenwich",0,
   ANGLEUNIT["degree",0.0174532925199433]],
   CS[ellipsoidal,2],
   AXIS["geodetic latitude (Lat)",north,
   ORDER[1],
   ANGLEUNIT["degree",0.0174532925199433]],
   AXIS["geodetic longitude (Lon)",east,
   ORDER[2],
   ANGLEUNIT["degree",0.0174532925199433]],
   USAGE[
   SCOPE["unknown"],
   AREA["World"],
   BBOX[-90,-180,90,180],
   ID["EPSG",4326]]
   \end{verbatim}

2. List the coordinate operations between NAD27 (designed with its CRS name) and NAD83 (designed with its EPSG code 4269) within an area of interest

   \begin{verbatim}
   projinfo -s NAD27 -t EPSG:4269 --area "USA - Missouri"
   \end{verbatim}

   Output:

   \begin{verbatim}
   DERIVED_FROM(EPSG):1241, NAD27 to NAD83 (1), 0.15 m, USA - CONUS including EEZ
   PROJ string:
   +proj=pipeline +step +proj=axisswap +order=2,1 +step +proj=unitconvert \ 
   +xy_in=deg +xy_out=rad +step +proj=hgridshift +grids=conus \ 
   +step +proj=unitconvert +xy_in=rad +xy_out=deg +step +proj=axisswap +order=2,1
   WKT2_2018 string:
   \end{verbatim}

   (continues on next page)
COORDINATEOPERATION["NAD27 to NAD83 (1)",
SOURCECRS[
    GEOGCRS["NAD27",
        DATUM["North American Datum 1927",
            ELLIPSOID["Clarke 1866",6378206.4,294.978698213898,
                LENGTHUNIT["metre",1]],
            PRIMEM["Greenwich",0,
                ANGLEUNIT["degree",0.0174532925199433]],
            CS[ellipsoidal,2],
                AXIS["geodetic latitude (Lat)",north,
                    ORDER[1],
                ANGLEUNIT["degree",0.0174532925199433]],
            AXIS["geodetic longitude (Lon)",east,
                    ORDER[2],
                ANGLEUNIT["degree",0.0174532925199433]]],
    PARAMETERFILE["Latitude and longitude difference file","conus"],
    OPERATIONACCURACY[0.15],
    USAGE[SCOPE["unknown"],
        AREA["USA - CONUS including EEZ"],
        BBOX[23.81,-129.17,49.38,-65.69],
        ID["DERIVED_FROM(EPSG)",1241]]
]
CHAPTER
SEVEN

COORDINATE OPERATIONS

Coordinate operations in PROJ are divided into three groups: Projections, conversions and transformations. Projections are purely cartographic mappings of the sphere onto the plane. Technically projections are conversions (according to ISO standards), though in PROJ projections are distinguished from conversions. Conversions are coordinate operations that do not exert a change in reference frame. Operations that do exert a change in reference frame are called transformations.

7.1 Projections

Projections are coordinate operations that are technically conversions but since projections are so fundamental to PROJ we differentiate them from conversions.

Projections map the spherical 3D space to a flat 2D space.

7.1.1 Albers Equal Area

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<thead>
<tr>
<th>Classification</th>
<th>Conic</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
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</tr>
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<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
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<td>aea</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

7.1.1.1 Options

Required

+lat_1=<value>
  First standard parallel.
  *Defaults to 0.0.*
+lat_2=<value>
  Second standard parallel.
  *Defaults to 0.0.*
Optional

```
+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.
+ellps=<value>
  See `proj -le` for a list of available ellipsoids.
  Defaults to “GRS80”.
+R=<value>
  Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.
+x_0=<value>
  False easting.
  Defaults to 0.0.
+y_0=<value>
  False northing.
  Defaults to 0.0.
```

Fig. 1: proj-string: `+proj=aea +lat_1=29.5 +lat_2=42.5`
7.1.2 Azimuthal Equidistant

<table>
<thead>
<tr>
<th>Classification</th>
<th>Azimuthal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical and elliptical projection</td>
</tr>
<tr>
<td>Alias</td>
<td>aeqd</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

Fig. 2: proj-string: `+proj=aeqd`
7.1.2.1 Options

Note: All options are optional for the Azimuthal Equidistant projection.

+guam
   Use Guam elliptical formulas. Only accurate near the Island of Guam ($\lambda \approx 144.5^\circ, \phi \approx 13.5^\circ$)

+k_0=<value>
   Scale factor. Determines scale factor used in the projection.
   Defaults to 1.0.

+lat_ts=<value>
   Latitude of true scale. Defines the latitude where scale is not distorted. Takes precedence over +k_0 if both
   options are used together.
   Defaults to 0.0.

+lat_0=<value>
   Latitude of projection center.
   Defaults to 0.0.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

7.1.3 Airy

The Airy projection is an azimuthal minimum error projection for the region within the small or great circle defined
by an angular distance, $\phi_b$, from the tangency point of the plane ($\lambda_0, \phi_0$).

<table>
<thead>
<tr>
<th>Classification</th>
<th>Azimuthal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
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<tr>
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<td>Global</td>
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<tr>
<td>Alias</td>
<td>airy</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>
Fig. 3: proj-string: +proj=airy
7.1.3.1 Options

+lat_b
   Angular distance from tangency point of the plane \((\lambda_0, \phi_0)\) where the error is kept at minimum.
   Defaults to 90° (suitable for hemispherical maps).

+no_cut
   Do not cut at hemisphere limit

+lat_0=<value>
   Latitude of projection center.
   Defaults to 0.0.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

7.1.4 Aitoff

<table>
<thead>
<tr>
<th>Classification</th>
<th>Miscellaneous</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
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</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>aitoff</td>
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<tr>
<td>Domain</td>
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</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

7.1.4.1 Parameters

Note: All parameters for the projection are optional.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
Fig. 4: proj-string: +proj=aitoff

+x_0=<value>
False easting.
Defaults to 0.0.
+y_0=<value>
False northing.
Defaults to 0.0.

7.1.5 Modified Stereographic of Alaska

<table>
<thead>
<tr>
<th>Classification</th>
<th>Modified azimuthal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical and elliptical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Alaska</td>
</tr>
<tr>
<td>Alsk</td>
<td>alsk</td>
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<td>Domain</td>
<td>2D</td>
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<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

7.1.5.1 Options

Note: All options are optional for the projection.

+x_0=<value>
False easting.
Defaults to 0.0.
+y_0=<value>
False northing.
Fig. 5: proj-string: +proj=alsk
Defaults to 0.0.

`+ellps=<value>`

See `proj -le` for a list of available ellipsoids.

Defaults to “GRS80”.

7.1.6 Apian Globular I

<table>
<thead>
<tr>
<th>Classification</th>
<th>Miscellaneous</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
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<td>Global</td>
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<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

Fig. 6: proj-string: `+proj=apian`

7.1.6.1 Options

Note: All options are optional for the Apian Globular projection.

`+lat_0=<value>`

Latitude of projection center.

Defaults to 0.0.

`+lon_0=<value>`

Longitude of projection center.

Defaults to 0.0.

`+R=<value>`

Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.
7.1.7 August Epicycloidal

**Note:** All options are optional for the August Epicycloidal projection.

+lon_0=<value>
   Longitude of projection center.
   *Defaults to 0.0.*

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   *Defaults to 0.0.*

+y_0=<value>
   False northing.
   *Defaults to 0.0.*
\[ +y_0 = \text{value} \]
False northing.
Defaults to 0.0.

### 7.1.8 Bacon Globular

![Diagram of Bacon Globular projection]

Fig. 8: proj-string: \texttt{+proj=bacon}

#### 7.1.8.1 Parameters

\textbf{Note:} All parameters are optional for the Bacon Globular projection.

\[ +\text{lon}_0 = \text{value} \]
Longitude of projection center.
Defaults to 0.0.

\[ +R = \text{value} \]
Radius of the sphere given in meters. If used in conjunction with \texttt{+ellps +R} takes precedence.

\[ +x_0 = \text{value} \]
False easting.
Defaults to 0.0.

\[ +y_0 = \text{value} \]
False northing.
Defaults to 0.0.
7.1.9 Bertin 1953

New in version 6.0.0.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Miscellaneous</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward, spherical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>bertin1953</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

The Bertin 1953 projection is intended for making world maps. Created by Jacques Bertin in 1953, this projection was the go-to choice of the French cartographic school when they wished to represent phenomena on a global scale. The projection was formulated in 2017 by Philippe Rivière for visionscarto.net.

![Fig. 9: proj-string: +proj=bertin1953](image)

The Bertin 1953 projection is intended for making world maps. Created by Jacques Bertin in 1953, this projection was the go-to choice of the French cartographic school when they wished to represent phenomena on a global scale. The projection was formulated in 2017 by Philippe Rivière for visionscarto.net.
7.1.9.1 Usage

The Bertin 1953 projection has no special options. Its rotation parameters are fixed. Here is an example of a forward projection with scale 1:

```
$ echo 122 47 | src/proj +proj=bertin1953 +R=1 0.72 0.73
```

7.1.9.2 Parameters

**Note:** All parameters for the projection are optional.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   *Defaults to 0.0.*

+y_0=<value>
   False northing.
   *Defaults to 0.0.*

7.1.9.3 Further reading


7.1.10 Bipolar conic of western hemisphere

7.1.10.1 Parameters

**Note:** All options are optional for the Bipolar Conic projection.

+ns
   Return non-skewed cartesian coordinates.

+lon_0=<value>
   Longitude of projection center.
   *Defaults to 0.0.*

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   *Defaults to 0.0.*

+y_0=<value>
   False northing.
   *Defaults to 0.0.*
Fig. 10: proj-string: +proj=bipc +ns
7.1.11 Boggs Eumorphic

Fig. 11: proj-string: +proj=boggs

7.1.11.1 Parameters

Note: All options are optional for the Boggs Eumorphic projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.
7.1.12 Bonne (Werner lat_1=90)

![Map of the world in the Bonne projection]

Fig. 12: proj-string: +proj=bonne +lat_1=10

7.1.12.1 Parameters

Required

+lat_1=<value>
  First standard parallel.
  Defaults to 0.0.

Optional

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.

+ellps=<value>
  See proj -le for a list of available ellipsoids.
  Defaults to “GRS80”.

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
  False easting.
  Defaults to 0.0.

+y_0=<value>
  False northing.
  Defaults to 0.0.
7.1.13 Cal Coop Ocean Fish Invest Lines/Stations

The CalCOFI pseudo-projection is the line and station coordinate system of the California Cooperative Oceanic Fisheries Investigations program, known as CalCOFI, for sampling offshore of the west coast of the U.S. and Mexico.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Conformal cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical and elliptical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Only valid for the west coast of USA and Mexico</td>
</tr>
<tr>
<td>Alias</td>
<td>calcofi</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

The coordinate system is based on the Mercator projection with units rotated -30 degrees from the meridian so that they are oriented with the coastline of the Southern California Bight and Baja California. Lines increase from Northwest to Southeast. A unit of line is 12 nautical miles. Stations increase from inshore to offshore. A unit of station is equal
to 4 nautical miles. The rotation point is located at line 80, station 60, or 34.15 degrees N, -121.15 degrees W, and is depicted by the red dot in the figure. By convention, the ellipsoid of Clarke 1866 is used to calculate CalCOFI coordinates.

The CalCOFI program is a joint research effort by the U.S. National Oceanic and Atmospheric Administration, University of California Scripps Oceanographic Institute, and California Department of Fish and Game. Surveys have been conducted for the CalCOFI program since 1951, creating one of the oldest and most scientifically valuable joint oceanographic and fisheries data sets in the world. The CalCOFI line and station coordinate system is now used by several other programs including the Investigaciones Mexicanas de la Corriente de California (IMECOCAL) program offshore of Baja California. The figure depicts some commonly sampled locations from line 40 to line 156.7 and offshore to station 120. Blue numbers indicate line (bottom) or station (left) numbers along the grid. Note that lines spaced at approximate 3-1/3 intervals are commonly sampled, e.g., lines 43.3 and 46.7.

### 7.1.13.1 Usage

A typical forward CalCOFI projection would be from lon/lat coordinates on the Clark 1866 ellipsoid. For example:

```
proj +proj=calcofi +ellps=clrk66 -E <<EOF
-121.15 34.15
EOF
```

Output of the above command:

```
-121.15 34.15 80.00 60.00
```

The reverse projection from line/station coordinates to lon/lat would be entered as:

```
proj +proj=calcofi +ellps=clrk66 -I -E -f "%.2f" <<EOF
80.0 60.0
EOF
```

Output of the above command:

```
80.0 60.0 -121.15 34.15
```

### 7.1.13.2 Options

**Note:** All options are optional for the CalCOFI projection.

- `+ellps=<value>`
  
  See `proj -le` for a list of available ellipsoids.

  *Defaults to “GRS80”.*

- `+R=<value>`
  
  Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.
7.1.13.3 Mathematical definition

The algorithm used to make conversions is described in [EberHewitt1979] with a few corrections reported in [Weber-Moore2013].

7.1.13.4 Further reading

1. General information about the CalCOFI program
2. The Investigaciones Mexicanas de la Corriente de California

7.1.14 Cassini (Cassini-Soldner)

Although the Cassini projection has been largely replaced by the Transverse Mercator, it is still in limited use outside the United States and was one of the major topographic mapping projections until the early 20th century.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Transverse and oblique cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, Spherical and Elliptical</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global, but best used near the central meridian with long, narrow areas</td>
</tr>
<tr>
<td>Alias</td>
<td>cass</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

7.1.14.1 Usage

There has been little usage of the spherical version of the Cassini, but the ellipsoidal Cassini-Soldner version was adopted by the Ordnance Survey for the official survey of Great Britain during the second half of the 19th century [Steers1970]. Many of these maps were prepared at a scale of 1:2,500. The Cassini-Soldner was also used for the detailed mapping of many German states during the same period.

Example using EPSG 30200 (Trinidad 1903, units in clarke’s links):

```
$ echo 0.17453293 -1.08210414 | proj +proj=cass +lat_0=10.44166666666667 +lon_0=-61.33333333333334 +x_0=86501.46392051999 +y_0=65379.0134283 +a=6378293.645208759 +b=6356617.987679838 +to_meter=0.201166195164 +no_defs
66644.94 82536.22
```

Example using EPSG 3068 (Soldner Berlin):

```
$ echo 13.5 52.4 | proj +proj=cass +lat_0=52.41864827777778 +lon_0=13.62720366666667 +x_0=40000 +y_0=10000 +ellps=bessel +datum=potsdam +units=m +no_defs
31343.05 7932.76
```
Fig. 13: proj-string: +proj=cass
7.1.14.2 Options

**Note:** All options are optional for the Cassini projection.

```
+lat_0=<value>
   Latitude of projection center.
   Defaults to 0.0.
+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.
+x_0=<value>
   False easting.
   Defaults to 0.0.
+y_0=<value>
   False northing.
   Defaults to 0.0.
+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.
+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
```

7.1.14.3 Mathematical definition

The formulas describing the Cassini projection are taken from [Snyder1987].

\( \phi_0 \) is the latitude of origin that match the center of the map (default to 0). It can be set with +lat_0.

**Spherical form**

**Forward projection**

\[
x = \arcsin(\cos(\phi) \sin(\lambda))
\]

\[
y = \arctan(2(\tan(\phi), \cos(\lambda)) - \phi_0)
\]
Inverse projection

\[ \phi = \arcsin(\sin(y + \phi_0) \cos(x)) \]
\[ \lambda = \arctan(2\tan(x), \cos(y + \phi_0)) \]

Elliptical form

Forward projection

\[ N = (1 - e^2 \sin^2(\phi))^{-1/2} \]
\[ T = \tan^2(\phi) \]
\[ A = \lambda \cos(\phi) \]
\[ C = \frac{e^2}{1 - e^2} \cos^2(\phi) \]
\[ x = N(A - T\frac{A^3}{6} - (8 - T + 8C)T\frac{A^5}{120}) \]
\[ y = M(\phi) - M(\phi_0) + N \tan(\phi)(\frac{A^2}{2} + (5 - T + 6C)\frac{A^4}{24}) \]
and \( M() \) is the meridional distance function.

Inverse projection

\[ \phi' = M^{-1}(M(\phi_0) + y) \]
if \( \phi' = \frac{\pi}{2} \) then \( \phi = \phi' \) and \( \lambda = 0 \)
otherwise evaluate \( T \) and \( N \) above using \( \phi' \) and
\[ R = (1 - e^2)(1 - e^2 \sin^2 \phi')^{-3/2} \]
\[ D = \frac{x}{N} \]
\[ \phi = \phi' - \tan \phi' \frac{N}{R}(\frac{D^2}{2} - (1 + 3T)\frac{D^4}{24}) \]
\[ \lambda = \frac{(D - T\frac{D^3}{3} + (1 + 3T)T\frac{D^5}{15})}{\cos \phi'} \]
7.1.14.4 Further reading

1. Wikipedia
2. EPSG, POSC literature pertaining to Coordinate Conversions and Transformations including Formulas

7.1.15 Central Cylindrical

Fig. 14: proj-string: +proj=cc
# 7.1.15.1 Parameters

**Note:** All parameters are optional for the Central Cylindricla projection.

- **+lon_0=<value>**  
  Longitude of projection center.  
  *Defaults to 0.0.*

- **+R=<value>**  
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

- **+x_0=<value>**  
  False easting.  
  *Defaults to 0.0.*

- **+y_0=<value>**  
  False northing.  
  *Defaults to 0.0.*

## 7.1.16 Central Conic

New in version 5.0.0.

This is central (centrographic) projection on cone tangent at :option:`lat_1` latitude, identical with conic() projection from mapproj R package.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Conic</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global, but best used near the standard parallel</td>
</tr>
<tr>
<td>Alias</td>
<td>ccon</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

### 7.1.16.1 Usage

This simple projection is rarely used, as it is not equidistant, equal-area, nor conformal.

An example of usage (and the main reason to implement this projection in proj4) is the ATPOL geobotanical grid of Poland, developed in Institute of Botany, Jagiellonian University, Krakow, Poland in 1970s [Zajac1978]. The grid was originally handwritten on paper maps and further copied by hand. The projection (together with strange Earth radius) was chosen by its creators as the compromise fit to existing maps during first software development in DOS era. Many years later it is still de facto standard grid in Polish geobotanical research.

The ATPOL coordinates can be achieved with with the following parameters:

```
+proj=ccon +lat_1=52 +lon_0=19 +axis=esu +a=6390000 +x_0=330000 +y_0=-350000
```

For more information see [Komsta2016] and [Verey2017].
Fig. 15: proj-string: +proj=ccon +lat_1=52 +lon_0=19

7.1.16.2 Parameters

Required

+lat_1=<value>
  Standard parallel of projection.

Optional

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
  False easting.
  Defaults to 0.0.

+y_0=<value>
  False northing.
  Defaults to 0.0.
7.1.16.3 Mathematical definition

Forward projection

\[ r = \cot \phi_0 - \tan(\phi - \phi_0) \]
\[ x = r \sin(\lambda \sin \phi_0) \]
\[ y = \cot \phi_0 - r \cos(\lambda \sin \phi_0) \]

Inverse projection

\[ y = \cot \phi_0 - y \]
\[ \phi = \phi_0 - \tan^{-1}\left( \sqrt{x^2 + y^2} - \cot \phi_0 \right) \]
\[ \lambda = \tan^{-1}\left( \frac{\sqrt{x^2 + y^2}}{\sin \phi_0} \right) \]

7.1.16.4 Reference values

For ATPOL to WGS84 test, run the following script:

```
#!/bin/bash
cat << EOF | src/cs2cs -v -f "%E" +proj=ccon +lat_1=52 +lat_0=52 +lon_0=19 +axis=esu +a=6390000 +x_0=330000 +y_0=-350000 +to +proj=longlat +datum=WGS84 +no_defs 0 0
0 700000
700000 0
700000 700000
330000 350000
EOF
```

It should result with

```
1.384023E+01 5.503040E+01 0.000000E+00
1.451445E+01 4.877385E+01 0.000000E+00
2.478271E+01 4.877385E+01 0.000000E+00
2.402761E+01 4.875048E+01 0.000000E+00
1.900000E+01 5.200000E+01 0.000000E+00
```

Analogous script can be run for reverse test:

```
cat << EOF | src/cs2cs -v -f "%E" +proj=longlat +datum=WGS84 +no_defs +to +proj=ccon +lat_1=52 +lat_0=52 +lon_0=19 +axis=esu +a=6390000 +x_0=330000 +y_0=-350000 24 55
15 49
24 49
19 52
EOF
```
and it should give the following results:

<table>
<thead>
<tr>
<th>Value 1</th>
<th>Value 2</th>
<th>Value 3</th>
<th>Value 4</th>
<th>Value 5</th>
<th>Value 6</th>
</tr>
</thead>
<tbody>
<tr>
<td>6.500315E+05</td>
<td>4.106162E+03</td>
<td>0.000000E+00</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3.707419E+04</td>
<td>6.768262E+05</td>
<td>0.000000E+00</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>6.960534E+05</td>
<td>6.722946E+05</td>
<td>0.000000E+00</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3.300000E+05</td>
<td>3.500000E+05</td>
<td>0.000000E+00</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

7.1.17 Equal Area Cylindrical

Fig. 16: proj-string: +proj=cea

7.1.17.1 Parameters

**Note:** All parameters are optional for the Equal Area Cylindrical projection.

+lat_ts=<value>
  Latitude of true scale. Defines the latitude where scale is not distorted. Takes precedence over +k_0 if both options are used together.
  *Defaults to 0.0.*

+lon_0=<value>
  Longitude of projection center.
  *Defaults to 0.0.*

+ellps=<value>
  See `proj -le` for a list of available ellipsoids.
  *Defaults to “GRS80”.*

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+k_0=<value>
  Scale factor. Determines scale factor used in the projection.
  *Defaults to 1.0.*

+x_0=<value>
  False easting.
  *Defaults to 0.0.*
\texttt{+y_0=<value>}

False northing.\newline

\textit{Defaults to 0.0.}

\subsection*{7.1.18 Chamberlin Trimetric}

\begin{figure}
\centering
\includegraphics[width=\textwidth]{chamberlin_trimetric}
\caption{proj-string: \texttt{+proj=chamb +lat_1=10 +lon_1=30 +lon_2=40}}
\end{figure}

\subsection*{7.1.18.1 Parameters}

\textbf{Required}

\texttt{+lat_1=<value>}

Latitude of the first control point.

\texttt{+lon_1=<value>}

Longitude of the first control point.
+lat\_2=<value>  
Latitude of the second control point.

+lon\_2=<value>  
Longitude of the second control point.

+lat\_3=<value>  
Latitude of the third control point.

+lon\_3=<value>  
Longitude of the third control point.

Optional

+lon\_0=<value>  
Longitude of projection center.  
_Defaults to 0.0._

+R=<value>  
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x\_0=<value>  
False easting.  
_Defaults to 0.0._

+y\_0=<value>  
False northing.  
_Defaults to 0.0._

7.1.19 Collignon

![Collignon projection](image)

Fig. 18: proj-string: +proj=collg
7.1.19.1 Parameters

Note: All parameters are optional for the Collignon projection.

+lon_0=<value>
Longitude of projection center.
 Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
False easting.
 Defaults to 0.0.

+y_0=<value>
False northing.
 Defaults to 0.0.

7.1.20 Compact Miller

The Compact Miller projection is a cylindrical map projection with a height-to-width ratio of 0.6:1.
See [Jenny2015]

<table>
<thead>
<tr>
<th>Classification</th>
<th>Cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>comill</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

7.1.20.1 Parameters

Note: All parameters are optional for projection.

+lon_0=<value>
Longitude of projection center.
 Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
False easting.
 Defaults to 0.0.
Fig. 19: proj-string: +proj=comill

\[ +y_0 = \text{value} \]
False northing.  
Defaults to 0.0.

### 7.1.21 Craster Parabolic (Putnins P4)

Fig. 20: proj-string: +proj=crast
7.1.21.1 Parameters

**Note:** All parameters are optional for the Craster Parabolic projection.

+lon_0=<value>
    Longitude of projection center.
    *Defaults to 0.0.*

+R=<value>
    Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
    False easting.
    *Defaults to 0.0.*

+y_0=<value>
    False northing.
    *Defaults to 0.0.*

7.1.22 Denoyer Semi-Elliptical

Fig. 21: proj-string: +proj=denoy
7.1.22.1 Parameters

Note: All parameters are optional for the Denoyer Semi-Elliptical projection.

+lon_0=<value>
    Longitude of projection center.
    Defaults to 0.0.
+R=<value>
    Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
    False easting.
    Defaults to 0.0.
+y_0=<value>
    False northing.
    Defaults to 0.0.

7.1.23 Eckert I

Fig. 22: proj-string: +proj=eck1

\begin{align*}
x &= 2\sqrt{\frac{2}{3}}\pi\lambda(1 - |\phi|/\pi) \\
y &= 2\sqrt{\frac{2}{3}}\pi\phi
\end{align*}
7.1.23.1 Parameters

**Note:** All parameters are optional for the Eckert I projection.

- `+lon_0=<value>`
  Longitude of projection center.
  *Defaults to 0.0.*

- `+R=<value>`
  Radius of the sphere given in meters. If used in conjunction with `+ellps R` takes precedence.

- `+x_0=<value>`
  False easting.
  *Defaults to 0.0.*

- `+y_0=<value>`
  False northing.
  *Defaults to 0.0.*

7.1.24 Eckert II

![Eckert II Projection](image)

Fig. 23: proj-string: `+proj=eck2`
7.1.24.1 Parameters

Note: All parameters are optional for the Eckert II projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.25 Eckert III

Fig. 24: proj-string: +proj=eck3
7.1.25.1 Parameters

Note: All parameters are optional for the Eckert III projection.

\[ +\text{lon}_0=<\text{value}> \]
Longitude of projection center.
 Defaults to 0.0.

\[ +R=<\text{value}> \]
Radius of the sphere given in meters. If used in conjunction with \( +\text{ellps} +R \) takes precedence.

\[ +x_0=<\text{value}> \]
False easting.
 Defaults to 0.0.

\[ +y_0=<\text{value}> \]
False northing.
 Defaults to 0.0.

7.1.26 Eckert IV

Fig. 25: proj-string: \[ +\text{proj}=\text{eck}4 \]

\[
x = \lambda (1 + \cos \phi) / \sqrt{2 + \pi} \\
y = 2\phi / \sqrt{2 + \pi}
\]
7.1.26.1 Parameters

**Note:** All parameters are optional for the Eckert IV projection.

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
  False easting.
  Defaults to 0.0.

+y_0=<value>
  False northing.
  Defaults to 0.0.

7.1.27 Eckert V

Fig. 26: proj-string: +proj=eck5
7.1.27.1 Parameters

Note: All parameters are optional for the Eckert V projection.

+lon_0=<value>
  Longitude of projection center.
  
  Defaults to 0.0.

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
  False easting.
  
  Defaults to 0.0.

+y_0=<value>
  False northing.
  
  Defaults to 0.0.

7.1.28 Eckert VI

Fig. 27: proj-string: +proj=eck6
7.1.28.1 Parameters

Note: All parameters are optional for the Eckert VI projection.

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
  False easting.
  Defaults to 0.0.

+y_0=<value>
  False northing.
  Defaults to 0.0.

7.1.29 Equidistant Cylindrical (Plate Carrée)

The simplest of all projections. Standard parallels (0° when omitted) may be specified that determine latitude of true scale (k=h=1).

<table>
<thead>
<tr>
<th>Classification</th>
<th>Conformal cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global, but best used near the equator</td>
</tr>
<tr>
<td>Alias</td>
<td>eqc</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

Fig. 28: proj-string: +proj=eqc
7.1.29.1 Usage

Because of the distortions introduced by this projection, it has little use in navigation or cadastral mapping and finds its main use in thematic mapping. In particular, the plate carrée has become a standard for global raster datasets, such as Celestia and NASA World Wind, because of the particularly simple relationship between the position of an image pixel on the map and its corresponding geographic location on Earth.

The following table gives special cases of the cylindrical equidistant projection.

<table>
<thead>
<tr>
<th>Projection Name</th>
<th>(lat ts=) $\phi_0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Plain/Plane Chart</td>
<td>0°</td>
</tr>
<tr>
<td>Simple Cylindrical</td>
<td>0°</td>
</tr>
<tr>
<td>Plate Carrée</td>
<td>0°</td>
</tr>
<tr>
<td>Ronald Miller—minimum overall scale distortion</td>
<td>37°30'</td>
</tr>
<tr>
<td>E.Grafarend and A.Niermann</td>
<td>42°</td>
</tr>
<tr>
<td>Ronald Miller—minimum continental scale distortion</td>
<td>43°30'</td>
</tr>
<tr>
<td>Gall Isographic</td>
<td>45°</td>
</tr>
<tr>
<td>Ronald Miller Equirectangular</td>
<td>50°30'</td>
</tr>
<tr>
<td>E.Grafarend and A.Niermann minimum linear distortion</td>
<td>61°7'</td>
</tr>
</tbody>
</table>

Example using EPSG 32662 (WGS84 Plate Carrée):

```bash
$ echo 2 47 | proj +proj=eqc +lat_ts=0 +lat_0=0 +lon_0=0 +x_0=0 +y_0=0 +ellps=WGS84 ...
˓→+datum=WGS84 +units=m +no_defs
222638.98 5232016.07
```

Example using Plate Carrée projection with true scale at latitude 30° and central meridian 90°W:

```bash
$ echo -88 30 | proj +proj=eqc +lat_ts=30 +lon_0=90w
192811.01 3339584.72
```

7.1.29.2 Parameters

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.

+lat_0=<value>
  Latitude of projection center.
  Defaults to 0.0.

+lat_ts=<value>
  Latitude of true scale. Defines the latitude where scale is not distorted. Takes precedence over +k_0 if both options are used together.
  Defaults to 0.0.

+x_0=<value>
  False easting.
  Defaults to 0.0.

+y_0=<value>
  False northing.
  Defaults to 0.0.
+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

7.1.29.3 Mathematical definition

The formulas describing the Equidistant Cylindrical projection are all taken from [Snyder1987].

$\phi_{ts}$ is the latitude of true scale, that mean the standard parallels where the scale of the projection is true. It can be set with +lat_ts.

$\phi_0$ is the latitude of origin that match the center of the map. It can be set with +lat_0.

**Forward projection**

$$
  x = \lambda \cos \phi_{ts} \\
  y = \phi - \phi_0
$$

**Inverse projection**

$$
  \lambda = x / \cos \phi_{ts} \\
  \phi = y + \phi_0
$$

7.1.29.4 Further reading

1. Wikipedia
2. Wolfram Mathworld

7.1.30 Equidistant Conic

7.1.30.1 Parameters

**Required**

+lat_1=<value>
   First standard parallel.
   Defaults to 0.0.

+lat_2=<value>
   Second standard parallel.
   Defaults to 0.0.
Fig. 29: proj-string: +proj=eqdc +lat_1=55 +lat_2=60
Optional

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.

+ellps=<value>
  See proj -le for a list of available ellipsoids.
  Defaults to “GRS80”.

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
  False easting.
  Defaults to 0.0.

+y_0=<value>
  False northing.
  Defaults to 0.0.

7.1.31 Equal Earth

New in version 5.2.0.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Pseudo cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical and ellipsoidal projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>eqearth</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

Fig. 30: proj-string: +proj=eqearth
The Equal Earth projection is intended for making world maps. Equal Earth is a projection inspired by the Robinson projection, but unlike the Robinson projection retains the relative size of areas. The projection was designed in 2018 by Bojan Savric, Tom Patterson and Bernhard Jenny [Savric2018].

### 7.1.31.1 Usage

The Equal Earth projection has no special options. Here is an example of an forward projection on a sphere with a radius of 1 m:

```bash
$ echo 122 47 | src/proj +proj=eqearth +R=1
1.55 0.89
```

### 7.1.31.2 Parameters

**Note:** All parameters for the projection are optional.

- **+lon_0=<value>**  
  Longitude of projection center.  
  *Defaults to 0.0.*

- **+ellps=<value>**  
  See `proj -le` for a list of available ellipsoids.  
  *Defaults to “GRS80”.*

- **+R=<value>**  
  Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.

- **+x_0=<value>**  
  False easting.  
  *Defaults to 0.0.*

- **+y_0=<value>**  
  False northing.  
  *Defaults to 0.0.*

### 7.1.31.3 Further reading

7.1.32 Euler

Fig. 31: proj-string: +proj=euler +lat_1=67 +lat_2=75

7.1.32.1 Parameters

Required

+lat_1=<value>
First standard parallel.
Defaults to 0.0.

+lat_2=<value>
Second standard parallel.
Defaults to 0.0.
Optional

+lon_0=<value>
Longitude of projection center.
Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
False easting.
Defaults to 0.0.

+y_0=<value>
False northing.
Defaults to 0.0.

7.1.33 Fahey

Fig. 32: proj-string: +proj=fahey
7.1.33.1 Parameters

Note: All parameters are optional for the Fahey projection.

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+X_0=<value>
  False easting.
  Defaults to 0.0.

+Y_0=<value>
  False northing.
  Defaults to 0.0.

7.1.34 Foucaut

Fig. 33: proj-string: +proj=fouc
7.1.34.1 Parameters

Note: All parameters are optional for the Foucaut projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.
+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
   False easting.
   Defaults to 0.0.
+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.35 Foucaut Sinusoidal

Fig. 34: proj-string: +proj=fouc_s

The $y$-axis is based upon a weighted mean of the cylindrical equal-area and the sinusoidal projections. Parameter $n = n$ is the weighting factor where $0 \leq n \leq 1$.

\[
\begin{align*}
x &= \lambda \cos \phi / (n + (1 - n) \cos \phi) \\
y &= n\phi + (1 - n) \sin \phi
\end{align*}
\]

For the inverse, the Newton-Raphson method can be used to determine $\phi$ from the equation for $y$ above. As $n \to 0$ and $\phi \to \pi/2$, convergence is slow but for $n = 0$, $\phi = \sin^{-1} y$.
7.1.35.1 Parameters

**Note:** All parameters are optional for the Foucaut Sinusoidal projection.

+n=<value>
Weighting factor. Value should be in the interval 0-1.

+lon_0=<value>
Longitude of projection center.

*Defaults to 0.0.*

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
False easting.

*Defaults to 0.0.*

+y_0=<value>
False northing.

*Defaults to 0.0.*

7.1.36 Gall (Gall Stereographic)

The Gall stereographic projection, presented by James Gall in 1855, is a cylindrical projection. It is neither equal-area nor conformal but instead tries to balance the distortion inherent in any projection.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Transverse and oblique cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, Spherical</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>gall</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

7.1.36.1 Usage

The need for a world map which avoids some of the scale exaggeration of the Mercator projection has led to some commonly used cylindrical modifications, as well as to other modifications which are not cylindrical. The earliest common cylindrical example was developed by James Gall of Edinburgh about 1855 (Gall, 1885, p. 119-123). His meridians are equally spaced, but the parallels are spaced at increasing intervals away from the Equator. The parallels of latitude are actually projected onto a cylinder wrapped about the sphere, but cutting it at lats. 45° N. and S., the point of perspective being a point on the Equator opposite the meridian being projected. It is used in several British atlases, but seldom in the United States. The Gall projection is neither conformal nor equal-area, but has a blend of various features. Unlike the Mercator, the Gall shows the poles as lines running across the top and bottom of the map.

Example using Gall Stereographical

```
$ echo 9 51 | proj +proj=gall +lon_0=0 +x_0=0 +y_0=0 +ellps=WGS84 +datum=WGS84
+units=m +no_defs
708432.90 5193386.36
```
Fig. 35: proj-string: +proj=gall

Example using Gall Stereographical (Central meridian 90°W)

```
$ echo 9 51 | proj +proj=gall +lon_0=90w +x_0=0 +y_0=0 +ellps=WGS84 +datum=WGS84
    +units=m +no_defs
7792761.91 5193386.36
```

### 7.1.36.2 Parameters

**Note:** All parameters for the projection are optional.

- **+lon_0=<value>**
  Longitude of projection center.
  *
  Defaults to 0.0.

- **+R=<value>**
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

- **+x_0=<value>**
  False easting.
  *
  Defaults to 0.0.

- **+y_0=<value>**
  False northing.
  *
  Defaults to 0.0.
7.1.36.3 Mathematical definition

The formulas describing the Gall Stereographical are all taken from [Snyder1993].

**Spherical form**

**Forward projection**

\[ x = \frac{\lambda}{\sqrt{2}} \]
\[ y = (1 + \frac{\sqrt{2}}{2}) \tan(\frac{\phi}{2}) \]

**Inverse projection**

\[ \phi = 2 \arctan\left(\frac{y}{1 + \frac{\sqrt{2}}{2}}\right) \]
\[ \lambda = \sqrt{2}x \]

7.1.36.4 Further reading

1. Wikipedia

7.1.37 Geostationary Satellite View

The geos projection pictures how a geostationary satellite scans the earth at regular scanning angle intervals.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Azimuthal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical and elliptical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>geos</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>
Fig. 36: proj-string: +proj=geos +h=35785831.0 +lon_0=-60 +sweep=y
7.1.37.1 Usage

In order to project using the geos projection you can do the following:

```
proj +proj=geos +h=35785831.0
```

The required argument \( h \) is the viewing point (satellite position) height above the earth.

The projection coordinate relate to the scanning angle by the following simple relation:

```
scanning_angle (radians) = projection_coordinate / h
```

**Note on sweep angle**

The viewing instrument on-board geostationary satellites described by this projection have a two-axis gimbal viewing geometry. This means that the different scanning positions are obtained by rotating the gimbal along a N/S axis (or \( y \)) and a E/W axis (or \( x \)).

In the image above, the outer-gimbal axis, or sweep-angle axis, is the N/S axis (\( y \)) while the inner-gimbal axis, or fixed-angle axis, is the E/W axis (\( x \)).

This example represents the scanning geometry of the Meteosat series satellite. However, the GOES satellite series
use the opposite scanning geometry, with the E/W axis (x) as the sweep-angle axis, and the N/S (y) as the fixed-angle axis.

The sweep argument is used to tell PROJ which on which axis the outer-gimbal is rotating. The possible values are x or y, y being the default. Thus, the scanning geometry of the Meteosat series satellite should take sweep as y, and GOES should take sweep as x.

7.1.37.2 Parameters

Required

+h=<value>
Height of the view point above the Earth and must be in the same units as the radius of the sphere or semimajor axis of the ellipsoid.

Optional

+sweep=<axis>
Sweep angle axis of the viewing instrument. Valid options are “x” and “y”.

Defaults to “y”.

+lon_0=<value>
Longitude of projection center.

Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+ellps=<value>
See proj -le for a list of available ellipsoids.

Defaults to “GRS80”.

+x_0=<value>
False easting.

Defaults to 0.0.

+y_0=<value>
False northing.

Defaults to 0.0.

7.1.38 Ginsburg VIII (TsNIIGAiK)

7.1.38.1 Parameters

Note: All parameters are optional for the Ginsburg VIII projection.

+lon_0=<value>
Longitude of projection center.

Defaults to 0.0.
Fig. 37: proj-string: \texttt{+proj=gins8}

\texttt{+R=<value>}
   Radius of the sphere given in meters. If used in conjunction with \texttt{+ellps +R} takes precedence.

\texttt{+x_0=<value>}
   False easting.
   \textit{Defaults to 0.0.}

\texttt{+y_0=<value>}
   False northing.
   \textit{Defaults to 0.0.}

\section*{7.1.39 General Sinusoidal Series}

\subsection*{7.1.39.1 Parameters}

\textbf{Note:} All parameters are optional for the General Sinusoidal Series projection.

\texttt{+lon_0=<value>}
   Longitude of projection center.
   \textit{Defaults to 0.0.}

\texttt{+R=<value>}
   Radius of the sphere given in meters. If used in conjunction with \texttt{+ellps +R} takes precedence.
7.1.40 Gnomonic

7.1.40.1 Parameters

Note: All parameters are optional for the Gnomonic projection.

+lon_0=<value>
  Longitude of projection center.
  *Defaults to 0.0.*

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with *ellps* +R takes precedence.

+x_0=<value>
  False easting.
  *Defaults to 0.0.*

+y_0=<value>
  False northing.
  *Defaults to 0.0.*
Fig. 39: proj-string: +proj=gnom +lat_0=90 +lon_0=-50
7.1.41 Goode Homolosine

Fig. 40: proj-string: +proj=goode

7.1.41.1 Parameters

Note: All parameters are optional for the Goode Homolosine projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.42 Mod. Stererographic of 48 U.S.

7.1.42.1 Parameters

Note: All parameters are optional for the projection.

+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.

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**Fig. 41: proj-string: +proj=gs48**

\[ +x_0=<\text{value}> \]
False easting.
*Defaults to 0.0.*

\[ +y_0=<\text{value}> \]
False northing.
*Defaults to 0.0.*

### 7.1.43 Mod. Stererographics of 50 U.S.

**Fig. 42: proj-string: +proj=gs50**
7.1.43.1 Parameters

**Note:** All parameters are optional for the projection.

```
+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.
+x_0=<value>
   False easting.
   Defaults to 0.0.
+y_0=<value>
   False northing.
   Defaults to 0.0.
```

7.1.44 Hammer & Eckert-Greifendorff

```
Fig. 43: proj-string: +proj=hammer
```

7.1.44.1 Parameters

**Note:** All parameters are optional for the projection.

```
+W=<value>
   Set to 0.5 for the Hammer projection and 0.25 for the Eckert-Greifendorff projection. +W has to be larger than zero.
   Defaults to 0.5.
```
\[ +M = \text{value} \]
\[ +M \text{ has to be larger than zero.} \]
\[ \text{Defaults to 1.0.} \]

\[ +\text{lon}_0 = \text{value} \]
\[ \text{Longitude of projection center.} \]
\[ \text{Defaults to 0.0.} \]

\[ +R = \text{value} \]
\[ \text{Radius of the sphere given in meters. If used in conjunction with } +\text{ellps} +R \text{ takes precedence.} \]

\[ +x_0 = \text{value} \]
\[ \text{False easting.} \]
\[ \text{Defaults to 0.0.} \]

\[ +y_0 = \text{value} \]
\[ \text{False northing.} \]
\[ \text{Defaults to 0.0.} \]

### 7.1.45 Hatano Asymmetrical Equal Area

<table>
<thead>
<tr>
<th>Classification</th>
<th>Pseudocylindrical Projection</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>hatano</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

Fig. 44: proj-string: +proj=hatano
7.1.45.1 Parameters

**Note:** All parameters for the projection are optional.

- **+lon_0=<value>**
  - Longitude of projection center.
  - Defaults to 0.0.

- **+R=<value>**
  - Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

- **+x_0=<value>**
  - False easting.
  - Defaults to 0.0.

- **+y_0=<value>**
  - False northing.
  - Defaults to 0.0.

**Mathematical Definition**

**Forward**

\[
\begin{align*}
  x &= 0.85\lambda \cos \theta \\
  y &= C_y \sin \theta \\
  P(\theta) &= 2\theta + \sin 2\theta - C_p \sin \phi \\
  P'(\theta) &= 2(1 + \cos 2\theta) \\
  \theta_0 &= 2\phi
\end{align*}
\]

<table>
<thead>
<tr>
<th>Condition</th>
<th>(C_y)</th>
<th>(C_p)</th>
</tr>
</thead>
<tbody>
<tr>
<td>For (\phi &gt; 0)</td>
<td>1.75859</td>
<td>2.67595</td>
</tr>
<tr>
<td>For (\phi &lt; 0)</td>
<td>1.93052</td>
<td>2.43763</td>
</tr>
</tbody>
</table>

For \(\phi = 0\), \(y \leftarrow 0\), and \(x \leftarrow 0.85\lambda\).

**Further reading**

1. Compare Map Projections
2. Mathworks
7.1.46 HEALPix

<table>
<thead>
<tr>
<th>Classification</th>
<th>Miscellaneous</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical and elliptical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>healpix</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

The HEALPix projection is area preserving and can be used with a spherical and ellipsoidal model. It was initially developed for mapping cosmic background microwave radiation. The image below is the graphical representation of the mapping and consists of eight isomorphic triangular interrupted map graticules. The north and south contain four in which straight meridians converge polewards to a point and unequally spaced horizontal parallels. HEALPix provides a mapping in which points of equal latitude and equally spaced longitude are mapped to points of equal latitude and equally spaced longitude with the module of the polar interruptions.

7.1.46.1 Usage

To run a forward HEALPix projection on a unit sphere model, use the following command:

```
proj +proj=healpix +lon_0=0 +a=1 -E <<EOF
0 0
EOF
```

# output
0 0 0.00 0.00
7.1.46.2 Parameters

**Note:** All parameters for the projection are optional.

\[+\text{lon}_0=\text{value}\]

Longitude of projection center.

*Defaults to 0.0.*

\[+\text{x}_0=\text{value}\]

False easting.

*Defaults to 0.0.*

\[+\text{y}_0=\text{value}\]

False northing.

*Defaults to 0.0.*

\[+\text{ellps}=\text{value}\]

See `proj -le` for a list of available ellipsoids.

*Defaults to “GRS80”.*

\[+\text{R}=\text{value}\]

Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.

7.1.46.3 Further reading

1. NASA
2. Wikipedia

### 7.1.47 rHEALPix

<table>
<thead>
<tr>
<th>Classification</th>
<th>Miscellaneous</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical and elliptical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>rhealpix</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>
rHEALPix is a projection based on the HEALPix projection. The implementation of rHEALPix uses the HEALPix projection. The rHEALPix combines the peaks of the HEALPix into a square. The square’s position can be translated and rotated across the x-axis which is a novel approach for the rHEALPix projection. The initial intention of using rHEALPix in the Spatial Computation Engine Science Collaboration Environment (SCENZGrid).

7.1.47.1 Usage

To run a rHEALPix projection on a WGS84 ellipsoidal model, use the following command:

```
proj +proj=rhealpix -f '%.2f' +ellps=WGS84 +south_square=0 +north_square=2 -E << EOF
> 55 12
> EOF
55 12 6115727.86 1553840.13
```
7.1.47.2 Parameters

Note: All parameters for the projection are optional.

+north_square
  Position of the north polar square. Valid inputs are 0–3.
  Defaults to 0.0.

+south_square
  Position of the south polar square. Valid inputs are 0–3.
  Defaults to 0.0.

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.

+ellps=<value>
  See proj -le for a list of available ellipsoids.
  Defaults to “GRS80”.

+x_0=<value>
  False easting.
  Defaults to 0.0.

+y_0=<value>
  False northing.
  Defaults to 0.0.

7.1.47.3 Further reading

1. NASA
2. Wikipedia

7.1.48 Interrupted Goode Homolosine

7.1.48.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
7.1.49 International Map of the World Polyconic

Fig. 46: proj-string: +proj=imw_p +lat_1=30 +lat_2=-40
7.1.49.1 Parameters

**Required**

+lat_1=<value>
   First standard parallel.
   *Defaults to 0.0.*

+lat_2=<value>
   Second standard parallel.
   *Defaults to 0.0.*

**Optional**

+lon_0=<value>
   Longitude of projection center.
   *Defaults to 0.0.*

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   *Defaults to 0.0.*

+y_0=<value>
   False northing.
   *Defaults to 0.0.*

7.1.50 Icosahedral Snyder Equal Area

Fig. 47: proj-string: +proj=isea
7.1.50.1 Parameters

**Note:** All parameters are optional for the projection.

+**orient**=<string>
  Can be set to either isea or pole.

+**azi**=<value>
  Azimuth.
  *Defaults to 0.0*

+**aperture**=<value>
  *Defaults to 3.0*

+**resolution**=<value>
  *Defaults to 4.0*

+**mode**=<string>
  Can be either plane, di, dd or hex.

+**lon_0**=<value>
  Longitude of projection center.
  *Defaults to 0.0.*

+**lat_0**=<value>
  Latitude of projection center.
  *Defaults to 0.0.*

+**R**=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+**x_0**=<value>
  False easting.
  *Defaults to 0.0.*

+**y_0**=<value>
  False northing.
  *Defaults to 0.0.*

7.1.51 Kavraisky V

7.1.51.1 Parameters

**Note:** All parameters are optional for the Kavraisky V projection.

+**lon_0**=<value>
  Longitude of projection center.
  *Defaults to 0.0.*

+**R**=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
Fig. 48: proj-string: +proj=kav5

+\texttt{x}_0=\texttt{<value>}
   False easting.
   \textit{Defaults to 0.0.}

+\texttt{y}_0=\texttt{<value>}
   False northing.
   \textit{Defaults to 0.0.}

7.1.52 Kavraisky VII

Fig. 49: proj-string: +proj=kav7
7.1.52.1 Parameters

Note: All parameters are optional for the Kavraisky VII projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.53 Krovak

7.1.53.1 Parameters

Note: All parameters are optional for the Krovak projection.

+czech
   Reverse the sign of the output coordinates, as is tradition in the Czech Republic.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+lat_0=<value>
   Latitude of projection center.
   Defaults to 0.0.

+k_0=<value>
   Scale factor. Determines scale factor used in the projection.
   Defaults to 0.9999.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.
Fig. 50: proj-string: +proj=krovak
7.1.54 Laborde

7.1.54.1 Parameters

Required

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.
+lat_0=<value>
   Latitude of projection center.
   Defaults to 0.0.

Optional

+azi=<value>
   Azimuth of the central line.
   Defaults to 0.0
+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
   False easting.
   Defaults to 0.0.
+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.55 Lambert Azimuthal Equal Area

7.1.55.1 Parameters

Note: All parameters are optional.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.
+lat_0=<value>
   Latitude of projection center.
   Defaults to 0.0.
+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.

7.1. Projections
Fig. 51: proj-string: +proj=labrd +lon_0=40 +lat_0=-10
Fig. 52: proj-string: +proj=laea
+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
False easting.
Defaults to 0.0.

+y_0=<value>
False northing.
Defaults to 0.0.

7.1.56 Lagrange

Fig. 53: proj-string: +proj=lagrng
### 7.1.56.1 Parameters

**Note:** All parameters are optional for the projection.

- **\(+W=\text{<value>}\)**
  - The factor \(+W\) is the ratio of the difference in longitude from the central meridian to the a circular meridian to 90. \(+W\) must be a positive value.
  - *Defaults to 2.0*

- **\(\text{+lon}_0=\text{<value>}\)**
  - Longitude of projection center.
  - *Defaults to 0.0.*

- **\(\text{+lat}_1=\text{<value>}\)**
  - First standard parallel.
  - *Defaults to 0.0.*

- **\(\text{+ellps}=\text{<value>}\)**
  - See `proj -le` for a list of available ellipsoids.
  - *Defaults to “GRS80”.*

- **\(\text{+R}=\text{<value>}\)**
  - Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.

- **\(\text{+x}_0=\text{<value>}\)**
  - False easting.
  - *Defaults to 0.0.*

- **\(\text{+y}_0=\text{<value>}\)**
  - False northing.
  - *Defaults to 0.0.*

### 7.1.57 Larrivee

#### 7.1.57.1 Parameters

**Note:** All parameters are optional for the Larrivee projection.

- **\(\text{+lon}_0=\text{<value>}\)**
  - Longitude of projection center.
  - *Defaults to 0.0.*

- **\(\text{+R}=\text{<value>}\)**
  - Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.

- **\(\text{+x}_0=\text{<value>}\)**
  - False easting.
  - *Defaults to 0.0.*
Fig. 54: proj-string: `+proj=larr`
\[ +y_0 = \text{<value>} \]
False northing.
Defaults to 0.0.

### 7.1.58 Laskowski

7.1.58.1 Parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Default</th>
</tr>
</thead>
<tbody>
<tr>
<td>(+lon_0=\text{&lt;value}&gt;)</td>
<td>Longitude of projection center.</td>
<td>Defaults to 0.0.</td>
</tr>
<tr>
<td>(+R=\text{&lt;value}&gt;)</td>
<td>Radius of the sphere given in meters. If used in conjunction with (+ellps+R), takes precedence.</td>
<td></td>
</tr>
<tr>
<td>(+x_0=\text{&lt;value}&gt;)</td>
<td>False easting.</td>
<td>Defaults to 0.0.</td>
</tr>
<tr>
<td>(+y_0=\text{&lt;value}&gt;)</td>
<td>False northing.</td>
<td>Defaults to 0.0.</td>
</tr>
</tbody>
</table>

Note: All parameters are optional for the projection.

Fig. 55: proj-string: \(+proj=lask\)
7.1.59 Lambert Conformal Conic

A Lambert Conformal Conic projection (LCC) is a conic map projection used for aeronautical charts, portions of the State Plane Coordinate System, and many national and regional mapping systems. It is one of seven projections introduced by Johann Heinrich Lambert in 1772.

It has several different forms: with one and two standard parallels (referred to as 1SP and 2SP in EPSG guidance notes). Additionally we provide “2SP Michigan” form which is very similar to normal 2SP, but with a scaling factor on the ellipsoid (given as \( k_0 \) parameter). It is implemented as per EPSG Guidance Note 7-2 (version 54, August 2018, page 25). It is used in a few systems in the EPSG database which justifies adding this otherwise non-standard projection.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Conformal conic</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical and elliptical projection. One or two standard parallels (1SP and 2SP). “LCC 2SP Michigan” form can be used by setting (+k_0) parameter to specify ellipsoid scale.</td>
</tr>
<tr>
<td>Defined area</td>
<td>Best for regions predominantly east–west in extent and located in the middle north or south latitudes.</td>
</tr>
<tr>
<td>Alias</td>
<td>lcc</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

Fig. 56: proj-string: \(+proj=lcc +lon_0=-90 +lat_1=33 +lat_2=45\)
7.1.59.1 Parameters

Required

+lat_1=<value>
First standard parallel.
Defaults to 0.0.

Optional

+lon_0=<value>
Longitude of projection center.
Defaults to 0.0.
+lat_0=<value>
Latitude of projection center.
Defaults to 0.0.
+lat_2=<value>
Second standard parallel.
Defaults to 0.0.
+ellps=<value>
See proj -le for a list of available ellipsoids.
Defaults to “GRS80”.
+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
False easting.
Defaults to 0.0.
+y_0=<value>
False northing.
Defaults to 0.0.
+k_0=<value>
This parameter can represent two different values depending on the form of the projection. In LCC 1SP it determines the scale factor at natural origin. In LCC 2SP Michigan it determines the ellipsoid scale factor.
Defaults to 1.0.
7.1.59.2 Further reading

1. Wikipedia
2. Wolfram Mathworld
3. John P. Snyder “Map projections: A working manual” (pp. 104-110)
4. ArcGIS documentation on “Lambert Conformal Conic”
5. EPSG Guidance Note 7-2 (version 54, August 2018, page 25)

7.1.60 Lambert Conformal Conic Alternative

![Diagram of world map with grid lines and text overlays indicating proj-string: +proj=lcca +lat_0=35]

7.1.60.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
   Longitude of projection center.
   
   Defaults to 0.0.

+lat_0=<value>
   Latitude of projection center.
   
   Defaults to 0.0.

+ellps=<value>
   See proj -le for a list of available ellipsoids.
   
   Defaults to “GRS80”.

+R=<value>
    Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
    False easting.  
    Defaults to 0.0.

+y_0=<value>
    False northing.  
    Defaults to 0.0.

7.1.61 Lambert Equal Area Conic

Fig. 58: proj-string: +proj=leac

7.1.61.1 Parameters

Note: All parameters are optional for the Lambert Equal Area Conic projection.

+lat_1=<value>
    First standard parallel.  
    Defaults to 0.0.

+south
    Sets the second standard parallel to 90°S. When the flag is off the second standard parallel is set to 90°N.

+lon_0=<value>
    Longitude of projection center.  
    Defaults to 0.0.

+ellps=<value>
    See proj -le for a list of available ellipsoids.  
    Defaults to “GRS80”.

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+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.62 Lee Oblated Stereographic

7.1.62.1 Parameters

Note: All parameters are optional for the projection.

+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.63 Loximuthal

7.1.63.1 Parameters

Note: All parameters are optional for the Loximuthal projection.

+lat_1=<value>
   First standard parallel.
   Defaults to 0.0.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
Fig. 59: proj-string: +proj=lee_os
PROJ coordinate transformation software library, Release 6.1.1

Fig. 60: proj-string: +proj=loxim

+x_0=<value>
   False easting.
   Defaults to 0.0.
+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.64 Space oblique for LANDSAT

7.1.64.1 Parameters

Required

+lsat=<value>
   Landsat satellite used for the projection. Value between 1 and 5.
+path=<value>
   Selected path of satellite. Value between 1 and 253 when +lsat is set to 1,2 or 3, otherwise valid input is between 1 and 233.

Optional

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.
+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.

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Fig. 61: proj-string: +proj=lsat +ellps=GRS80 +lat_1=-60 +lat_2=60 +lsat=2 +path=2

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
  False easting.
  \textit{Defaults to 0.0}.

+y_0=<value>
  False northing.
  \textit{Defaults to 0.0}.

\section*{7.1.65 McBryde-Thomas Flat-Polar Sine (No. 1)}

\subsection*{7.1.65.1 Parameters}

\textbf{Note:} All parameters are optional for the McBryde-Thomas Flat-Polar Sine projection.

+lon_0=<value>
  Longitude of projection center.
  \textit{Defaults to 0.0}.

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
  False easting.
**7.1.66 McBryde-Thomas Flat-Pole Sine (No. 2)**

- **Fig. 62**: proj-string: `+proj=mbt_s`
  
  Defaults to 0.0.

- **+y_0=<value>**
  False northing.

  Defaults to 0.0.

- **Fig. 63**: proj-string: `+proj=mbt_fps`
7.1.66.1 Parameters

Note: All parameters are optional.

+lon_0=<value>
    Longitude of projection center.
    Defaults to 0.0.
+R=<value>
    Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
    False easting.
    Defaults to 0.0.
+y_0=<value>
    False northing.
    Defaults to 0.0.

7.1.67 McBride-Thomas Flat-Polar Parabolic

Fig. 64: proj-string: +proj=mbtfpp

7.1.67.1 Parameters

Note: All parameters are optional.

+lon_0=<value>
    Longitude of projection center.
    Defaults to 0.0.
+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   \textit{Defaults to 0.0.}

+y_0=<value>
   False northing.
   \textit{Defaults to 0.0.}

\section*{7.1.68 McBryde-Thomas Flat-Polar Quartic}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig65}
\caption{proj-string: +proj=mbtfpq}
\end{figure}

\subsection*{7.1.68.1 Parameters}

\textbf{Note:} All parameters are optional.

+lon_0=<value>
   Longitude of projection center.
   \textit{Defaults to 0.0.}

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   \textit{Defaults to 0.0.}

+y_0=<value>
   False northing.
   \textit{Defaults to 0.0.}
7.1.69 McBryde-Thomas Flat-Polar Sinusoidal

Fig. 66: proj-string: +proj=mbtfps

7.1.69.1 Parameters

Note: All parameters are optional for the McBryde-Thomas Flat-Polar Sinusoidal projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.
7.1.70 Mercator

The Mercator projection is a cylindrical map projection that originates from the 15th century. It is widely recognized as the first regularly used map projection. The projection is conformal which makes it suitable for navigational purposes.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Conformal cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical and elliptical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global, but best used near the equator</td>
</tr>
<tr>
<td>Alias</td>
<td>merc</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

Fig. 67: proj-string: +proj=merc
7.1.70.1 Usage

Applications should be limited to equatorial regions, but is frequently used for navigational charts with latitude of true scale (+lat_ts) specified within or near chart’s boundaries. Often inappropriately used for world maps since the regions near the poles cannot be shown [Evenden1995].

Example using latitude of true scale:

```
$ echo 56.35 12.32 | proj +proj=merc +lat_ts=56.5
3470306.37   759599.90
```

Example using scaling factor:

```
echo 56.35 12.32 | proj +proj=merc +k_0=2
12545706.61   2746073.80
```

Note that +lat_ts and +k_0 are mutually exclusive. If used together, +lat_ts takes precedence over +k_0.

7.1.70.2 Parameters

Note: All parameters for the projection are optional.

+lat_ts=<value>
   Latitude of true scale. Defines the latitude where scale is not distorted. Takes precedence over +k_0 if both options are used together.
   Defaults to 0.0.

+k_0=<value>
   Scale factor. Determines scale factor used in the projection.
   Defaults to 1.0.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
7.1.70.3 Mathematical definition

The formulas describing the Mercator projection are all taken from G. Evenden’s libproj manuals [Evenden2005].

Spherical form

For the spherical form of the projection we introduce the scaling factor:

\[ k_0 = \cos \phi_{ts} \]

**Forward projection**

\[ x = k_0 \lambda \]
\[ y = k_0 \ln \left( \tan \left( \frac{\pi}{4} + \frac{\phi}{2} \right) \right) \]

**Inverse projection**

\[ \lambda = \frac{x}{k_0} \]
\[ \phi = \frac{\pi}{2} - 2 \arctan \left[ e^{-y/k_0} \right] \]

Elliptical form

For the elliptical form of the projection we introduce the scaling factor:

\[ k_0 = m(\phi_{ts}) \]

where \( m(\phi) \) is the parallel radius at latitude \( \phi \).

We also use the Isometric Latitude kernel function \( t() \).

**Note:** \( m() \) and \( t() \) should be described properly on a separate page about the theory of projections on the ellipsoid.

**Forward projection**

\[ x = k_0 \lambda \]
\[ y = k_0 \ln t(\phi) \]
Inverse projection

\[ \lambda = \frac{x}{k_0} \]

\[ \phi = t^{-1} \left[ e^{-y/k_0} \right] \]

7.1.70.4 Further reading

1. Wikipedia
2. Wolfram Mathworld

7.1.71 Miller Oblated Stereographic

Fig. 68: proj-string: +proj=mil_os
7.1.71.1 Parameters

Note: All parameters are optional for the projection.

+ellps=<value>
    See proj -le for a list of available ellipsoids.
    Defaults to “GRS80”.

+x_0=<value>
    False easting.
    Defaults to 0.0.

+y_0=<value>
    False northing.
    Defaults to 0.0.

7.1.72 Miller Cylindrical

The Miller cylindrical projection is a modified Mercator projection, proposed by Osborn Maitland Miller in 1942. The latitude is scaled by a factor of $\frac{4}{5}$, projected according to Mercator, and then the result is multiplied by $\frac{5}{4}$ to retain scale along the equator.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Neither conformal nor equal area cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse spherical</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global, but best used near the equator</td>
</tr>
<tr>
<td>Alias</td>
<td>mill</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

7.1.72.1 Usage

The Miller Cylindrical projection is used for world maps and in several atlases, including the National Atlas of the United States (USGS, 1970, p. 330-331) [Snyder1987].

Example using Central meridian 90°W:

$ echo -100 35 | proj +proj=mill +lon_0=90w
-1113194.91 4061217.24
7.1.72.2 Parameters

**Note:** All parameters for the projection are optional.

```
+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.
```
7.1.72.3 Mathematical definition

The formulas describing the Miller projection are all taken from [Snyder1987].

Forward projection

\[ x = \lambda \]
\[ y = 1.25 \times \ln \left( \tan \left( \frac{\pi}{4} + 0.4 \times \phi \right) \right) \]

Inverse projection

\[ \lambda = x \]
\[ \phi = 2.5 \times \arctan \left( e^{0.8 \times y} \right) - \frac{\pi}{4} \]

7.1.72.4 Further reading

1. Wikipedia

7.1.73 Space oblique for MISR

7.1.73.1 Parameters

Required

+path=<value>
Selected path of satellite. Value between 1 and 233.

Optional

+lon_0=<value>
Longitude of projection center.
Defaults to 0.0.
+ellps=<value>
See proj -le for a list of available ellipsoids.
Defaults to “GRS80”.
+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
False easting.
Defaults to 0.0.
Fig. 70: proj-string: +proj=misrsom +path=1
+y_0=<value>
False northing.

Defaults to 0.0.

7.1.74 Mollweide

Fig. 71: proj-string: +proj=moll

7.1.74.1 Parameters

Note: All parameters are optional.

+lon_0=<value>
Longitude of projection center.

Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
False easting.

Defaults to 0.0.

+y_0=<value>
False northing.

Defaults to 0.0.
7.1.75 Murdoch I

Fig. 72: proj-string: +proj=murdl +lat_1=30 +lat_2=50

7.1.75.1 Parameters

Required

+lat_1=<value>
  First standard parallel.
  Defaults to 0.0.
+lat_2=<value>
  Second standard parallel.
  Defaults to 0.0.

Optional

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.
+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
  False easting.
Defaults to 0.0.

+\text{y}_0 = <\text{value}>

False northing.

Defaults to 0.0.

7.1.76 Murdoch II

Fig. 73: proj-string: +proj=murd2 +lat_1=30 +lat_2=50

7.1.76.1 Parameters

Required

+\text{lat}_1 = <\text{value}>

First standard parallel.

Defaults to 0.0.

+\text{lat}_2 = <\text{value}>

Second standard parallel.

Defaults to 0.0.
Optional

+lon_0=<value>
    Longitude of projection center.
    Default to 0.0.

+R=<value>
    Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
    False easting.
    Default to 0.0.

+y_0=<value>
    False northing.
    Default to 0.0.

7.1.77 Murdoch III

Fig. 74: proj-string: +proj=murd3 +lat_1=30 +lat_2=50
7.1.77.1 Parameters

Required

\[ +\text{lat}_1=\text{value} \]
First standard parallel.
Defaults to 0.0.

\[ +\text{lat}_2=\text{value} \]
Second standard parallel.
Defaults to 0.0.

Optional

\[ +\text{lon}_0=\text{value} \]
Longitude of projection center.
Defaults to 0.0.

\[ +\text{R}=\text{value} \]
Radius of the sphere given in meters. If used in conjunction with \( +\text{ellps} +\text{R} \) takes precedence.

\[ +\text{x}_0=\text{value} \]
False easting.
Defaults to 0.0.

\[ +\text{y}_0=\text{value} \]
False northing.
Defaults to 0.0.

7.1.78 Natural Earth

<table>
<thead>
<tr>
<th>Classification</th>
<th>Pseudo cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>natearth</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

The Natural Earth projection is intended for making world maps. A distinguishing trait is its slightly rounded corners fashioned to emulate the spherical shape of Earth. The meridians (except for the central meridian) bend acutely inward as they approach the pole lines, giving the projection a hint of three-dimensionality. This bending also suggests that the meridians converge at the poles instead of truncating at the top and bottom edges. The distortion characteristics of the Natural Earth projection compare favorably to other world map projections.
7.1.78.1 Usage

The Natural Earth projection has no special options so usage is simple. Here is an example of an inverse projection on a sphere with a radius of 7500 m:

```bash
$ echo 3500 -8000 | proj -I +proj=natearth +a=7500
37d54'6.091"E 61d23'4.582"S
```

7.1.78.2 Parameters

**Note:** All parameters for the projection are optional.

```
+lon_0=<value>
Longitude of projection center.

  Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
False easting.

  Defaults to 0.0.

+y_0=<value>
False northing.

  Defaults to 0.0.
```
7.1.79 Natural Earth II

<table>
<thead>
<tr>
<th>Classification</th>
<th>Pseudo cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>natearth2</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

The Natural Earth II projection is intended for making world maps. At high latitudes, meridians bend steeply toward short pole lines resulting in a map with highly rounded corners that resembles an elongated globe.

See [Savric2015]

7.1.79.1 Parameters

**Note:** All parameters for the projection are optional.

`+lon_0=<value>`
- Longitude of projection center.
- Defaults to 0.0.

`+R=<value>`
- Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.
\[ +x_0 = \text{value} \]
False easting.
Defaults to 0.0.

\[ +y_0 = \text{value} \]
False northing.
Defaults to 0.0.

### 7.1.80 Nell

Fig. 77: proj-string: \(+\text{proj}=\text{nell}\)

#### 7.1.80.1 Parameters

**Note:** All parameters are optional.

\[ +\text{lon}_0 = \text{value} \]
Longitude of projection center.
Defaults to 0.0.

\[ +R = \text{value} \]
Radius of the sphere given in meters. If used in conjunction with \(+\text{ellps} +R\) takes precedence.

\[ +x_0 = \text{value} \]
False easting.
Defaults to 0.0.

\[ +y_0 = \text{value} \]
False northing.
Defaults to 0.0.
7.1.81 Nell-Hammer

Fig. 78: proj-string: +proj=nell_h

7.1.81.1 Parameters

Note: All parameters are optional.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.82 Nicolosi Globular

7.1.82.1 Parameters

Note: All parameters are optional.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
7.1.83 Near-sided perspective

The near-sided perspective projection simulates a view from a height \( h \) similar to how a satellite in orbit would see it.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Azimuthal. Neither conformal nor equal area.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse spherical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global, although for one hemisphere at a time.</td>
</tr>
<tr>
<td>Alias</td>
<td>nsper</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

7.1.83.1 Parameters

Required

\[ +h=<\text{value}> \]

Height of the view point above the Earth and must be in the same units as the radius of the sphere or semimajor axis of the ellipsoid.
Fig. 80: proj-string: +proj=nsper +h=3000000 +lat_0=-20 +lon_0=145
Optional

+lon_0=<value>
Longitude of projection center.
Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
False easting.
Defaults to 0.0.

+y_0=<value>
False northing.
Defaults to 0.0.

7.1.84 New Zealand Map Grid

7.1.84.1 Parameters

Note: All standard projection parameters are hard-coded for this projection

7.1.85 General Oblique Transformation

7.1.85.1 Usage

All of the projections of spherical library can be used as an oblique projection by means of the General Oblique Transformation. The user performs the oblique transformation by selecting the oblique projection +proj=ob_tran, specifying the translation factors, +o_lat_p and +o_lon_p, and the projection to be used, +o_proj. In the example of the Fairgrieve projection the latitude and longitude of the pole of the new coordinates, $\alpha$ and $\beta$ respectively, are to be placed at 45°N and 90°W and use the Mollweide projection. Because the central meridian of the translated coordinates will follow the $\beta$ meridian it is necessary to translate the translated system so that the Greenwich meridian will pass through the center of the projection by offsetting the central meridian.

The final control for this projection is:

+proj=ob_tran +o_proj=moll +o_lat_p=45 +o_lon_p=-90 +lon_0=-90

7.1.85.2 Parameters

Required

+o_proj=<projection>
Oblique projection.

In addition to specifying an oblique projection, how to rotate the projection should be specified. This is done in one of three ways: Define a new pole, rotate the projection about a given point or define a new “equator” spanned by two points on the sphere. See the details below.
Fig. 81: `proj-string: +proj=nzmg`
Fig. 82: proj-string: +proj=ob_tran +o_proj=mill +o_lon_p=40 +o_lat_p=50 +lon_0=60

New pole

+o_lat_p=<latitude>
Latitude of new pole for oblique projection.

+o_lon_p=<longitude>
Longitude of new pole for oblique projection.

Rotate about point

+o_alpha=<value>
Angle to rotate the projection with.

+o_lon_c=<value>
Longitude of the point the projection will be rotated about.

+o_lat_c=<value>
Latitude of the point the projection will be rotated about.
New “equator” points

+lon_1=<value>
   Longitude of first point.
+lat_1=<value>
   Latitude of first point.
+lon_2=<value>
   Longitude of second point.
+lat_2=<value>
   Latitude of second point.

Optional

+lon_0=<value>
   Longitude of projection center.
      Defaults to 0.0.
+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
   False easting.
      Defaults to 0.0.
+y_0=<value>
   False northing.
      Defaults to 0.0.

7.1.86 Oblique Cylindrical Equal Area

![Map of Oblique Cylindrical Equal Area](image)

Fig. 83: proj-string: +proj=oea
7.1.86.1 Parameters

**Required**

For the Oblique Cylindrical Equal Area projection a pole of rotation is needed. The pole can be defined in two ways:
By a point and azimuth or by providing to points that make up the pole.

**Point & azimuth**

+lonc=<value>
Longitude of rotational pole point.

+alpha=<value>
Angle of rotational pole.

**Two points**

+lon_1=<value>
Longitude of first point.

+lat_1=<value>
Latitude of first point.

+lon_2=<value>
Longitude of second point.

+lat_2=<value>
Latitude of second point.

**Optional**

+lon_0=<value>
Longitude of projection center.

 Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+k_0=<value>
Scale factor. Determines scale factor used in the projection.

 Defaults to 1.0.

+x_0=<value>
False easting.

 Defaults to 0.0.

+y_0=<value>
False northing.

 Defaults to 0.0.
7.1.87 Oblated Equal Area

Described in [Snyder1988].

7.1.87.1 Parameters

Required

+m=<value>
+n=<value>

Optional

+theta=<value>
+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.
+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
  False easting.
  Defaults to 0.0.
+y_0=<value>
  False northing.
  Defaults to 0.0.

7.1.88 Oblique Mercator

The Oblique Mercator projection is a cylindrical map projection that closes the gap between the Mercator and the Transverse Mercator projections.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Conformal cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical and elliptical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global, but reasonably accurate only within 15 degrees of the oblique central line</td>
</tr>
<tr>
<td>Alias</td>
<td>omerc</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

Figuratively, the cylinder used for developing the Mercator projection touches the planet along the Equator, while that of the Transverse Mercator touches the planet along a meridian, i.e. along a line perpendicular to the Equator.

The cylinder for the Oblique Mercator, however, touches the planet along a line at an arbitrary angle with the Equator. Hence, the Oblique Mercator projection is useful for mapping areas having their greatest extent along a direction that is neither north-south, nor east-west.
Fig. 84: proj-string: +proj=oea +m=1 +n=2
The Mercator and the Transverse Mercator projections are both limiting forms of the Oblique Mercator: The Mercator projection is equivalent to an Oblique Mercator with central line along the Equator, while the Transverse Mercator is equivalent to an Oblique Mercator with central line along a meridian.

For the sphere, the construction of the Oblique Mercator projection can be imagined as “tilting the cylinder of a plain Mercator projection”, so the cylinder, instead of touching the equator, touches an arbitrary great circle on the sphere. The great circle is defined by the tilt angle of the central line, hence putting land masses along that great circle near the centre of the map, where the Equator would go in the plain Mercator case.

The ellipsoidal case, developed by Hotine, and refined by Snyder [Snyder1987] is more complex, involving initial steps projecting from the ellipsoid to another curved surface, the “aposphere”, then projection from the aposphere to the skew uv-plane, before finally rectifying the skew uv-plane onto the map XY plane.

### 7.1.88.1 Usage

The tilt angle (azimuth) of the central line can be given in two different ways. In the first case, the azimuth is given directly, using the option \(+\alpha\alpha\) and defining the centre of projection using the options \(+\ellonc\) and \(+\ellat_0\). In the second case, the azimuth is given indirectly by specifying two points on the central line, using the options \(+\ellat_1, +\ellon_1, +\ellat_2, +\ellon_2\).

**Example: Verify that the Mercator projection is a limiting form of the Oblique Mercator**

```bash
$ echo 12 55 | proj +proj=merc +ellps=GRS80
1335833.89 7326837.71

$ echo 12 55 | proj +proj=omerc +lonc=0 +alpha=90 +ellps=GRS80
1335833.89 7326837.71
```

**Example: Second case - indirectly given azimuth**

```bash
$ echo 12 55 | proj +proj=omerc +lon_1=-1 +lat_1=1 +lon_2=0 +lat_2=0 +ellps=GRS80
349567.57 6839490.50
```

**Example: An approximation of the Danish “System 34” from [Rittri2012]**

```bash
$ echo 12 55 | proj +proj=omerc +lon_1=-1 +lat_1=1 +lon_2=0 +lat_2=0 +ellps=GRS80
349567.57 6839490.50
```
The input coordinate represents the System 34 datum point “Agri Bavnehøj”, with coordinates (200000, 200000) by definition. So at the datum point, the approximation is off by about 17 cm. This use case represents a datum shift from a cylinder projection on an old, slightly misaligned datum, to a similar projection on a modern datum.

7.1.88.2 Parameters

Central point and azimuth method

+alpha=<value>
Azimuth of centerline clockwise from north at the center point of the line. If +gamma is not given then +alpha determines the value of +gamma.

+gamma=<value>
Azimuth of centerline clockwise from north of the rectified bearing of centre line. If +alpha is not given, then +gamma is used to determine +alpha.

+lonc=<value>
Longitude of the central point.

+lat_0=<value>
Latitude of the central point.

Two point method

+lon_1=<value>
Longitude of first point.

+lat_1=<value>
Latitude of first point.

+lon_2=<value>
Longitude of second point.

+lat_2=<value>
Latitude of second point.

Optional

+no_rot
No rectification (not “no rotation” as one may well assume). Do not take the last step from the skew uv-plane to the map XY plane.

Note: This option is probably only marginally useful, but remains for (mostly) historical reasons.

+no_off
Do not offset origin to center of projection.
+k_0=<value>
Scale factor. Determines scale factor used in the projection.
Defaults to 1.0.

+lon_0=<value>
Longitude of projection center.
Defaults to 0.0.

+x_0=<value>
False easting.
Defaults to 0.0.

+y_0=<value>
False northing.
Defaults to 0.0.

7.1.89 Ortelius Oval

Fig. 86: proj-string: +proj=ortel

7.1.89.1 Parameters

Note: All parameters are optional.

+lon_0=<value>
Longitude of projection center.
Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
7.1.90 Orthographic

The orthographic projection is a perspective azimuthal projection centered around a given latitude and longitude.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Azimuthal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global, although only one hemisphere can be seen at a time</td>
</tr>
<tr>
<td>Alias</td>
<td>ortho</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

7.1.90.1 Parameters

**Note:** All parameters for the projection are optional.

+lon_0=<value>
   Longitude of projection center.
   *Defaults to 0.0.*

+lat_0=<value>
   Latitude of projection center.
   *Defaults to 0.0.*

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   *Defaults to 0.0.*

+y_0=<value>
   False northing.
   *Defaults to 0.0.*
Fig. 87: proj-string: +proj=ortho
7.1.91 Patterson

The Patterson projection is a cylindrical map projection designed for general-purpose mapmaking.
See [Patterson2014]

<table>
<thead>
<tr>
<th>Classification</th>
<th>Cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>patterson</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

Fig. 88: proj-string: +proj=patterson

7.1.91.1 Parameters

Note: All parameters are optional for projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.
\[ +y_0 = \text{<value>} \]

False northing.

Default to 0.0.

### 7.1.92 Perspective Conic

Fig. 89: proj-string: `+proj=pconic +lat_1=25 +lat_2=75`

#### 7.1.92.1 Parameters

**Required**

\[ +\text{lat}_1 = \text{<value>} \]

First standard parallel.

Default to 0.0.

\[ +\text{lat}_2 = \text{<value>} \]

Second standard parallel.

Default to 0.0.
Optional

\+lon_0=<value>
  Longitude of projection center.
  *Defaults to 0.0.*

\+R=<value>
  Radius of the sphere given in meters. If used in conjunction with \+ellps \+R takes precedence.

\+x_0=<value>
  False easting.
  *Defaults to 0.0.*

\+y_0=<value>
  False northing.
  *Defaults to 0.0.*

### 7.1.93 Polyconic (American)

![Fig. 90: proj-string: +proj=poly](image)

7.1. Projections
7.1.93.1 Parameters

Note: All parameters are optional for projection.

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.
+ellps=<value>
  See proj -le for a list of available ellipsoids.
  Defaults to “GRS80”.
+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
  False easting.
  Defaults to 0.0.
+y_0=<value>
  False northing.
  Defaults to 0.0.

7.1.94 Putnins P1

Fig. 91: proj-string: +proj=putp1
7.1.94.1 Parameters

**Note:** All parameters are optional for the Putnins P1 projection.

`+lon_0=<value>`

Longitude of projection center.

*Defaults to 0.0.*

`+R=<value>`

Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.

`+x_0=<value>`

False easting.

*Defaults to 0.0.*

`+y_0=<value>`

False northing.

*Defaults to 0.0.*

7.1.95 Putnins P2

Fig. 92: proj-string: `+proj=putp2`
7.1.95.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.96 Putnins P3

Fig. 93: proj-string: +proj=putp3
7.1.96.1 Parameters

Note: All parameters are optional for the projection.

\[ +\text{lon}_0=\text{value} \]
Longitude of projection center.

Defaults to 0.0.

\[ +\text{R}=\text{value} \]
Radius of the sphere given in meters. If used in conjunction with +ellps +\text{R} takes precedence.

\[ +\text{x}_0=\text{value} \]
False easting.

Defaults to 0.0.

\[ +\text{y}_0=\text{value} \]
False northing.

Defaults to 0.0.

7.1.97 Putnins P3’

Fig. 94: proj-string: +proj=putp3p
7.1.97.1 Parameters

Note: All parameters are optional for the projection.

\+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

\+R=<value>
   Radius of the sphere given in meters. If used in conjunction with \+ellps \+R takes precedence.

\+x_0=<value>
   False easting.
   Defaults to 0.0.

\+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.98 Putnins P4′

Fig. 95: proj-string: \+proj=putp4p
### 7.1.98.1 Parameters

**Note:** All parameters are optional for the projection.

+\texttt{lon}_0=<\texttt{value}>
- Longitude of projection center.
  
  *Defaults to 0.0.*

+\texttt{R}=<\texttt{value}>
- Radius of the sphere given in meters. If used in conjunction with +\texttt{ellps} +\texttt{R} takes precedence.

+\texttt{x}_0=<\texttt{value}>
- False easting.
  
  *Defaults to 0.0.*

+\texttt{y}_0=<\texttt{value}>
- False northing.
  
  *Defaults to 0.0.*

### 7.1.99 Putnins P5

![Putnins P5 projection](image-url)

Fig. 96: proj-string: +proj=putp5
7.1.99.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.100 Putnins P5'

Fig. 97: proj-string: +proj=putp5p
7.1.100.1 Parameters

**Note:** All parameters are optional for the projection.

`+lon_0=<value>`
Longitude of projection center.
*Defaults to 0.0.*

`+R=<value>`
Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.

`+x_0=<value>`
False easting.
*Defaults to 0.0.*

`+y_0=<value>`
False northing.
*Defaults to 0.0.*

7.1.101 Putnins P6

![Figure 98: proj-string: +proj=putp6](image)

Fig. 98: proj-string: `+proj=putp6`
7.1.101.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.102 Putnins P6’

![World map diagram](image)

Fig. 99: proj-string: +proj=putp6p
7.1.102.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.
+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
  False easting.
  Defaults to 0.0.
+y_0=<value>
  False northing.
  Defaults to 0.0.

7.1.103 Quartic Authalic

Fig. 100: proj-string: +proj=qua_aut

7.1.103.1 Parameters

Note: All parameters are optional for the Quartic Authalic projection.

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.
+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
  False easting.
  *Defaults to 0.0.*
+y_0=<value>
  False northing.
  *Defaults to 0.0.*

### 7.1.104 Quadrilateralized Spherical Cube

<table>
<thead>
<tr>
<th>Classification</th>
<th>Azimuthal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, elliptical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>qsc</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

The purpose of the Quadrilateralized Spherical Cube (QSC) projection is to project a sphere surface onto the six sides of a cube:
For this purpose, other alternatives can be used, notably *Gnomonic* or *HEALPix*. However, QSC projection has the following favorable properties:

It is an equal-area projection, and at the same time introduces only limited angular distortions. It treats all cube sides equally, i.e. it does not use different projections for polar areas and equatorial areas. These properties make QSC projection a good choice for planetary-scale terrain rendering. Map data can be organized in quadtree structures for each cube side. See [LambersKolb2012] for an example.

The QSC projection was introduced by [ONeilLaubscher1976], building on previous work by [ChanONeil1975]. For clarity: The earlier QSC variant described in [ChanONeil1975] became known as the COBE QSC since it was used by the NASA Cosmic Background Explorer (COBE) project; it is an approximately equal-area projection and is not the same as the QSC projection.

See also [CalabrettaGreisen2002] Sec. 5.6.2 and 5.6.3 for a description of both and some analysis.

In this implementation, the QSC projection projects onto one side of a circumscribed cube. The cube side is selected by choosing one of the following six projection centers:

| +lat_0=0 +lon_0=0 | front cube side |
| +lat_0=0 +lon_0=90 | right cube side |
| +lat_0=0 +lon_0=180 | back cube side |
| +lat_0=0 +lon_0=-90 | left cube side |
| +lat_0=90 | top cube side |
| +lat_0=-90 | bottom cube side |

Furthermore, this implementation allows the projection to be applied to ellipsoids. A preceding shift to a sphere is performed automatically; see [LambersKolb2012] for details.

### 7.1.104.1 Usage

The following example uses QSC projection via GDAL to create the six cube side maps from a world map for the WGS84 ellipsoid:

```
    gdalwarp -t_srs "+wktext +proj=qsc +units=m +ellps=WGS84 +lat_0=0 +lon_0=0"
             "-wo SOURCE_EXTRA=100 -wo SAMPLE_GRID=YES -te -6378137 -6378137 6378137 6378137"
             "worldmap.tif frontside.tif"

    gdalwarp -t_srs "+wktext +proj=qsc +units=m +ellps=WGS84 +lat_0=0 +lon_0=90"
             "-wo SOURCE_EXTRA=100 -wo SAMPLE_GRID=YES -te -6378137 -6378137 6378137 6378137"
             "worldmap.tif rightside.tif"

    gdalwarp -t_srs "+wktext +proj=qsc +units=m +ellps=WGS84 +lat_0=0 +lon_0=180"
             "-wo SOURCE_EXTRA=100 -wo SAMPLE_GRID=YES -te -6378137 -6378137 6378137 6378137"
             "worldmap.tif backside.tif"

    gdalwarp -t_srs "+wktext +proj=qsc +units=m +ellps=WGS84 +lat_0=0 +lon_0=-90"
             "-wo SOURCE_EXTRA=100 -wo SAMPLE_GRID=YES -te -6378137 -6378137 6378137 6378137"
             "worldmap.tif leftside.tif"

    gdalwarp -t_srs "+wktext +proj=qsc +units=m +ellps=WGS84 +lat_0=90 +lon_0=0"
             "-wo SOURCE_EXTRA=100 -wo SAMPLE_GRID=YES -te -6378137 -6378137 6378137 6378137"
             "worldmap.tif topside.tif"

    gdalwarp -t_srs "+wktext +proj=qsc +units=m +ellps=WGS84 +lat_0=-90 +lon_0=0"
             "-wo SOURCE_EXTRA=100 -wo SAMPLE_GRID=YES -te -6378137 -6378137 6378137 6378137"
             "worldmap.tif bottomside.tif"
```
**7.1.104.2 Parameters**

**Note:** All parameters for the projection are optional.

```
+lon_0=<value>
    Longitude of projection center.
    *Defaults to 0.0.*

+lat_0=<value>
    Latitude of projection center.
    *Defaults to 0.0.*
```
+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to "GRS80".

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.104.3 Further reading

1. Wikipedia
2. NASA

7.1.105 Robinson

![Robinson projection diagram]

Fig. 101: proj-string: +proj=robin

7.1.105.1 Parameters

**Note:** All parameters are optional for the projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
PROJ coordinate transformation software library, Release 6.1.1

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.106 Roussilhe Stereographic

7.1.106.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.
7.1.107 Rectangular Polyconic

Fig. 103: proj-string: +proj=rpoly

7.1.107.1 Parameters

Note: All parameters are optional for the projection.

+lat_ts=<value>
Latitude of true scale. Defines the latitude where scale is not distorted. Takes precedence over +k_0 if both options are used together.
Defaults to 0.0.

+lon_0=<value>
Longitude of projection center.
Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
False easting.
Defaults to 0.0.

+y_0=<value>
False northing.
Defaults to 0.0.
7.1.108 Spherical Cross-track Height

<table>
<thead>
<tr>
<th>Classification</th>
<th>Miscellaneous</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse.</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>sch</td>
</tr>
<tr>
<td>Domain</td>
<td>3D</td>
</tr>
<tr>
<td>Input type</td>
<td>3D coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

**proj-string:** `+proj=sch +plat_0=XX +plon_0=XX +phdg_0=XX`

The SCH coordinate system is a sensor aligned coordinate system developed at JPL (Jet Propulsion Laboratory) for radar mapping missions.

See [Hensley2002]

### 7.1.108.1 Parameters

**Required**

- `+plat_0=<value>`
  - Peg latitude (in degree)
- `+plon_0=<value>`
  - Peg longitude (in degree)
- `+phdg_0=<value>`
  - Peg heading (in degree)

**Optional**

- `+h_0=<value>`
  - Average height (in metre)
  - Defaults to 0.0.
- `+lon_0=<value>`
  - Longitude of projection center.
  - Defaults to 0.0.
- `+x_0=<value>`
  - False easting.
  - Defaults to 0.0.
- `+y_0=<value>`
  - False northing.
  - Defaults to 0.0.
- `+ellps=<value>`
  - See `proj -le` for a list of available ellipsoids.
  - Defaults to “GRS80”.

---

**Chapter 7. Coordinate operations**
7.1.109 Sinusoidal (Sanson-Flamsteed)

Fig. 104: proj-string: +proj=sinu

MacBryde and Thomas developed generalized formulas for several of the pseudocylindricals with sinusoidal meridians:

\[
\begin{align*}
x &= C\lambda(m + \cos\theta)/(m + 1) \\
y &= C\theta \\
C &= \sqrt{(m + 1)/n}
\end{align*}
\]

7.1.109.1 Parameters

**Note:** All parameters are optional for the Sinusoidal projection.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+lon_0=<value>
   Longitude of projection center.
   *Defaults to 0.0.*

+x_0=<value>
   False easting.
   *Defaults to 0.0.*

+y_0=<value>
   False northing.
   *Defaults to 0.0.*
7.1.110 Swiss Oblique Mercator

Fig. 105: proj-string: `+proj=somerc`

7.1.110.1 Parameters

Note: All parameters are optional for the projection.

`+lon_0=<value>`
Longitude of projection center.

`Defaults to 0.0.`

`+ellps=<value>`
See `proj -le` for a list of available ellipsoids.

`Defaults to “GRS80”.`

`+R=<value>`
Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.
+k_0=<value>
Scale factor. Determines scale factor used in the projection.
Defaults to 1.0.

+x_0=<value>
False easting.
Defaults to 0.0.

+y_0=<value>
False northing.
Defaults to 0.0.

7.1.111 Stereographic

Fig. 106: proj-string: +proj=stere +lat_0=90 +lat_ts=75
7.1.111.1 Parameters

Note: All parameters are optional for the projection.

+\texttt{lat\_ts}=<value>
Latitude of true scale. Defines the latitude where scale is not distorted. Takes precedence over +k_0 if both options are used together.
Default to 0.0.

+\texttt{lon\_0}=<value>
Longitude of projection center.
Default to 0.0.

+\texttt{ellps}=<value>
See \texttt{proj -le} for a list of available ellipsoids.
Default to “GRS80”.

+\texttt{R}=<value>
Radius of the sphere given in meters. If used in conjunction with +\texttt{ellps +R} takes precedence.

+\texttt{x\_0}=<value>
False easting.
Default to 0.0.

+\texttt{y\_0}=<value>
False northing.
Default to 0.0.

7.1.112 Oblique Stereographic Alternative

7.1.112.1 Parameters

Note: All parameters are optional for the projection.

+\texttt{lon\_0}=<value>
Longitude of projection center.
Default to 0.0.

+\texttt{lat\_0}=<value>
Latitude of projection center.
Default to 0.0.

+\texttt{ellps}=<value>
See \texttt{proj -le} for a list of available ellipsoids.
Default to “GRS80”.

+\texttt{R}=<value>
Radius of the sphere given in meters. If used in conjunction with +\texttt{ellps +R} takes precedence.
Fig. 107: proj-string: +proj=sterea +lat_0=90
7.1.113 Gauss-Schreiber Transverse Mercator (aka Gauss-Laborde Reunion)

Fig. 108: proj-string: +proj=gstmerc

7.1.113.1 Parameters

Note: All parameters are optional for the projection.

+k_0=<value>
   Scale factor. Determines scale factor used in the projection.
   Defaults to 1.0.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+lat_0=<value>
   Latitude of projection center.
   Defaults to 0.0.

+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.
+y_0=<value>
  False northing.
  *Defaults to 0.0.*

### 7.1.114 Transverse Central Cylindrical

![Proj-string: +proj=tcc](image)

**Fig. 109:** proj-string: `+proj=tcc`

#### 7.1.114.1 Parameters

**Note:** All parameters are optional for the projection.

- `+lon_0=<value>`
  Longitude of projection center.
  *Defaults to 0.0.*

- `+R=<value>`
  Radius of the sphere given in meters. If used in conjunction with `+ellps R` takes precedence.

- `+x_0=<value>`
  False easting.
  *Defaults to 0.0.*

- `+y_0=<value>`
  False northing.
  *Defaults to 0.0.*
7.1.115 Transverse Cylindrical Equal Area

7.1.115.1 Parameters

**Note:** All parameters are optional for the projection.

```
+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.
+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+k_0=<value>
   Scale factor. Determines scale factor used in the projection.
   Defaults to 1.0.
+x_0=<value>
   False easting.
   Defaults to 0.0.
+y_0=<value>
   False northing.
   Defaults to 0.0.
```

7.1.116 Times

See [Snyder1993], p.213-214.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Available forms</strong></td>
<td>Forward and inverse, spherical projection</td>
</tr>
<tr>
<td><strong>Defined area</strong></td>
<td>Global</td>
</tr>
<tr>
<td><strong>Alias</strong></td>
<td>times</td>
</tr>
<tr>
<td><strong>Domain</strong></td>
<td>2D</td>
</tr>
<tr>
<td><strong>Input type</strong></td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td><strong>Output type</strong></td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

7.1.116.1 Parameters

**Note:** All parameters are optional for projection.

```
+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.
+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
```
Fig. 110: proj-string: +proj=tcea
Fig. 111: proj-string: +proj=times

+\texttt{x}_0=<value>
False easting.
\emph{Defaults to 0.0.}

+\texttt{y}_0=<value>
False northing.
\emph{Defaults to 0.0.}

7.1.117 Tissot

7.1.117.1 Parameters

Required

+\texttt{lat}_1=<value>
First standard parallel.
\emph{Defaults to 0.0.}

+\texttt{lat}_2=<value>
Second standard parallel.
\emph{Defaults to 0.0.}
Fig. 112: proj-string: `+proj=tissot +lat_1=60 +lat_2=65`
Optional

+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
  False easting.
  Defaults to 0.0.

+y_0=<value>
  False northing.
  Defaults to 0.0.

7.1.118 Transverse Mercator

The transverse Mercator projection in its various forms is the most widely used projected coordinate system for world topographical and offshore mapping.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Transverse and oblique cylindrical</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, Spherical and Elliptical</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global, but reasonably accurate only within 15 degrees of the central meridian</td>
</tr>
<tr>
<td>Alias</td>
<td>tmerc</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

![Fig. 113: proj-string: +proj=tmerc](image)
7.1.118.1 Usage

Prior to the development of the Universal Transverse Mercator coordinate system, several European nations demonstrated the utility of grid-based conformal maps by mapping their territory during the interwar period. Calculating the distance between two points on these maps could be performed more easily in the field (using the Pythagorean theorem) than was possible using the trigonometric formulas required under the graticule-based system of latitude and longitude. In the post-war years, these concepts were extended into the Universal Transverse Mercator/Universal Polar Stereographic (UTM/UPS) coordinate system, which is a global (or universal) system of grid-based maps.

The following table gives special cases of the Transverse Mercator projection.

<table>
<thead>
<tr>
<th>Projection Name</th>
<th>Areas</th>
<th>Central meridian</th>
<th>Zone width</th>
<th>Scale Factor</th>
</tr>
</thead>
<tbody>
<tr>
<td>Transverse Mercator</td>
<td>World wide</td>
<td>Various</td>
<td>less than 6°</td>
<td>Various</td>
</tr>
<tr>
<td>Transverse Mercator</td>
<td>Southern Africa</td>
<td>2° intervals E of 11°E</td>
<td>2°</td>
<td>1.000</td>
</tr>
<tr>
<td>UTM North hemisphere</td>
<td>World wide equator to 84°N</td>
<td>6° intervals E &amp; W of 3° E &amp; W</td>
<td>Always 6°</td>
<td>0.9996</td>
</tr>
<tr>
<td>UTM South hemisphere</td>
<td>World wide north of 80°S to equator</td>
<td>6° intervals E &amp; W of 3° E &amp; W</td>
<td>Always 6°</td>
<td>0.9996</td>
</tr>
<tr>
<td>Gauss-Kruger</td>
<td>Former USSR, Yugoslavia, Germany, S. America, China</td>
<td>Various, according to area</td>
<td>Usually less than 6°, often less than 4°</td>
<td>1.0000</td>
</tr>
<tr>
<td>Gauss Boaga</td>
<td>Italy</td>
<td>Various, according to area</td>
<td>6°</td>
<td>0.9996</td>
</tr>
</tbody>
</table>

Example using Gauss-Kruger on Germany area (aka EPSG:31467)

```
$ echo 9 51 | proj +proj=tmerc +lat_0=0 +lon_0=9 +k_0=1 +x_0=3500000 +y_0=0 +ellps=bessel +datum=potsdam +units=m +no_defs
3500000.00 5651505.56
```

Example using Gauss Boaga on Italy area (EPSG:3004)

```
$ echo 15 42 | proj +proj=tmerc +lat_0=0 +lon_0=15 +k_0=0.9996 +x_0=2520000 +y_0=0 +ellps=intl +units=m +no_defs
2520000.00 4649858.60
```

7.1.118.2 Parameters

**Note:** All parameters for the projection are optional.

**+approx**

New in version 6.0.0.

Use the algorithm described in section “Elliptical Form” below. It is faster than the default algorithm, but also diverges faster as the distance from the central meridian increases.

**+lon_0=<value>**

Longitude of projection center.

*Defaults to 0.0.*
+lat_0=<value>
  Latitude of projection center.
  
  Defaults to 0.0.

+ellps=<value>
  See proj -le for a list of available ellipsoids.
  
  Defaults to “GRS80”.

+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+k_0=<value>
  Scale factor. Determines scale factor used in the projection.
  
  Defaults to 1.0.

+x_0=<value>
  False easting.
  
  Defaults to 0.0.

+y_0=<value>
  False northing.
  
  Defaults to 0.0.

### 7.1.118.3 Mathematical definition

The formulas describing the Transverse Mercator below are quoted from [Evenden2005].

$\phi_0$ is the latitude of origin that match the center of the map. It can be set with +lat_0.

$k_0$ is the scale factor at the natural origin (on the central meridian). It can be set with +k_0.

$M(\phi)$ is the meridional distance.

#### Spherical form

**Forward projection**

\[
B = \cos \phi \sin \lambda \\
\begin{align*}
x &= \frac{k_0}{2} \ln \left( \frac{1 + B}{1 - B} \right) \\
y &= k_0 \left( \arctan \left( \frac{\tan(\phi)}{\cos \lambda} \right) - \phi_0 \right)
\end{align*}
\]
Inverse projection

\[ D = \frac{y}{k_0} + \phi_0 \]
\[ x' = \frac{x}{k_0} \]
\[ \phi = \arcsin\left(\frac{\sin D}{\cosh x'}\right) \]
\[ \lambda = \arctan\left(\frac{\sinh x'}{\cos D}\right) \]

Elliptical form

The formulas below describe the algorithm used when giving the \texttt{+approx} option. They are originally from [Snyder1987], but here quoted from [Evenden1995]. The default algorithm is given by Poder and Engsager in [Poder1998]

Forward projection

\[ N = \frac{k_0}{(1 - e^2 \sin^2 \phi)^{1/2}} \]
\[ R = \frac{k_0(1 - e^2)}{(1 - e^2 \sin^2 \phi)^{3/2}} \]
\[ t = \tan(\phi) \]
\[ \eta = \frac{e^2}{1 - e^2 \cos^2 \phi} \]
\[ x = k_0 \lambda \cos \phi \]
\[ + \frac{k_0 \lambda^3 \cos^3 \phi}{3!} (1 - t^2 + \eta^2) \]
\[ + \frac{k_0 \lambda^5 \cos^5 \phi}{5!} (5 - 18t^2 + t^4 + 14\eta^2 - 58t^2\eta^2) \]
\[ + \frac{k_0 \lambda^7 \cos^7 \phi}{7!} (61 - 479t^2 + 179t^4 - t^6) \]
\[ y = M(\phi) \]
\[ + \frac{k_0 \lambda^2 \sin(\phi \cos \phi)}{2!} \]
\[ + \frac{k_0 \lambda^4 \sin(\phi \cos^3 \phi)}{4!} (5 - t^2 + 9\eta^2 + 4\eta^4) \]
\[ + \frac{k_0 \lambda^6 \sin(\phi \cos^5 \phi)}{6!} (61 - 58t^2 + t^4 + 270\eta^2 - 330t^2\eta^2) \]
\[ + \frac{k_0 \lambda^8 \sin(\phi \cos^7 \phi)}{8!} (1385 - 3111t^2 + 543t^4 - t^6) \]
Inverse projection

\[ \phi_1 = M^{-1}(y) \]
\[ N_1 = \frac{k_0}{1 - e^2 \sin^2 \phi_1}^{1/2} \]
\[ R_1 = \frac{k_0(1 - e^2)}{(1 - e^2 \sin^2 \phi_1)^{3/2}} \]
\[ t_1 = \tan(\phi_1) \]
\[ \eta_1 = \frac{e^2}{1 - e^2 \cos^2 \phi_1} \]
\[ \phi = \phi_1 - \frac{t_1 x^2}{2! R_1 N_1} + \frac{t_1 x^4}{4! R_1 N_1^3} (5 + 3t_1^2 + \eta_1^2 - 4t_1^2 \eta_1^2 - 9t_1^2 \eta_1^4) \]
\[ - \frac{t_1 x^6}{6! R_1 N_1^5} (61 + 90t_1^2 + 46\eta_1^2 + 45t_1^2 - 252t_1^2 \eta_1^2) \]
\[ + \frac{t_1 x^8}{8! R_1 N_1^7} (1385 + 3633t_1^2 + 4095t_1^4 + 1575t_1^6) \]
\[ \lambda = \frac{x}{\cos \phi N_1} - \frac{x^3}{3! \cos \phi N_1^3} (1 + 2t_1^2 + \eta_1^2) \]
\[ + \frac{x^5}{5! \cos \phi N_1^5} (5 + 6\eta_1^2 + 28t_1^2 - 3\eta_1^2 + 8t_1^2 \eta_1^4) \]
\[ - \frac{x^7}{7! \cos \phi N_1^7} (61 + 662t_1^2 + 1320t_1^4 + 720t_1^6) \]

7.1.118.4 Further reading

1. Wikipedia
2. EPSG, POSC literature pertaining to Coordinate Conversions and Transformations including Formulas

7.1.119 Tobler-Mercator

New in version 6.0.0.

Equal area cylindrical projection with the same latitudinal spacing as Mercator projection.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Cylindrical equal area</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical only</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global, conventionally truncated at about 80 degrees north and south</td>
</tr>
<tr>
<td>Alias</td>
<td>tobmerc</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>
7.1.119.1 Usage

The inappropriate use of the Mercator projection has declined but still occasionally occurs. One method of contrasting the Mercator projection is to present an alternative in the form of an equal area projection. The map projection derived here is thus not simply a pretty Christmas tree ornament: it is instead a complement to Mercator’s conformal navigation anamorphose and can be displayed as an alternative. The equations for the new map projection preserve the latitudinal stretching of the Mercator while adjusting the longitudinal spacing. This allows placement of the new map adjacent to that of Mercator. The surface area, while drastically warped, maintains the correct magnitude.

7.1.119.2 Parameters

Note: All parameters for the projection are optional.

+k_0=<value>
    Scale factor. Determines scale factor used in the projection.
    Defaults to 1.0.
+lon_0=<value>
    Longitude of projection center.
    Defaults to 0.0.
+x_0=<value>
    False easting.
Defaults to 0.0.
+\texttt{y}_0=<\texttt{value}>
False northing.
 Defaults to 0.0.
+\texttt{R}=<\texttt{value}>
Radius of the sphere given in meters. If used in conjunction with +\texttt{ellps} +\texttt{R} takes precedence.

7.1.119.3 Mathematical definition

The formulas describing the Tobler-Mercator are taken from Waldo Tobler’s article [Tobler2018]

**Spherical form**

For the spherical form of the projection we introduce the scaling factor:

\[ k_0 = \cos^2 \phi_{ts} \]

**Forward projection**

\[
x = k_0 \lambda
\]
\[
y = k_0 \ln \left[ \tan \left( \frac{\pi}{4} + \frac{\phi}{2} \right) \right]
\]

**Inverse projection**

\[
\lambda = \frac{x}{k_0}
\]
\[
\phi = \frac{\pi}{2} - 2 \arctan \left[ e^{-y/k_0} \right]
\]

7.1.120 Two Point Equidistant

7.1.120.1 Parameters

*Note:* All parameters are optional for the projection.

+\texttt{lon}_1=<\texttt{value}>
Longitude of first point.

+\texttt{lat}_1=<\texttt{value}>
Latitude of first point.
Fig. 115: proj-string: +proj=tpeqd +lat_1=60 +lat_2=65
+lon_2=<value>
Longitude of second point.

+lat_2=<value>
Latitude of second point.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
False easting.
Defaults to 0.0.

+y_0=<value>
False northing.
Defaults to 0.0.

7.1.121 Tilted perspective

<table>
<thead>
<tr>
<th>Classification</th>
<th>Azimuthal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, spherical projection</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>tper</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

Tilted Perspective is similar to Near-sided perspective (nsper) in that it simulates a perspective view from a height. Where nsper projects onto a plane tangent to the surface, Tilted Perspective orients the plane towards the direction of the view. Thus, extra parameters specifying azimuth and tilt are required beyond nsper’s h. As with nsper, lat_0 & lon_0 are also required for satellite position.

7.1.121.1 Parameters

Required

+h=<value>
Height of the view point above the Earth and must be in the same units as the radius of the sphere or semimajor axis of the ellipsoid.

Optional

+azi=<value>
Bearing in degrees away from north.
Defaults to 0.0.

+tilt=<value>
Angle in degrees away from nadir.
Defaults to 0.0.
Fig. 116: proj-string: +proj=tpers +h=5500000 +lat_0=40
**+lon_0=</value>**
Longitude of projection center.

*Defaults to 0.0.*

**+lat_0=</value>**
Latitude of projection center.

*Defaults to 0.0.*

**+R=</value>**
Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.

**+x_0=</value>**
False easting.

*Defaults to 0.0.*

**+y_0=</value>**
False northing.

*Defaults to 0.0.*

### 7.1.122 Universal Polar Stereographic

#### 7.1.122.1 Parameters

**Note:** All parameters are optional for the projection.

**+south**
South polar aspect.

**+lon_0=</value>**
Longitude of projection center.

*Defaults to 0.0.*

**+ellps=</value>**
See `proj -le` for a list of available ellipsoids.

*Defaults to “GRS80”.*

**+R=</value>**
Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.

**+x_0=</value>**
False easting.

*Defaults to 0.0.*

**+y_0=</value>**
False northing.

*Defaults to 0.0.*
Fig. 117: proj-string: \texttt{+proj=ups}
7.1.123 Urmaev V

Fig. 118: proj-string: `+proj=urm5 +n=0.9 +alpha=2 +q=4`

7.1.123.1 Parameters

Required parameters

`+n=<value>`

Set the \( n \) constant. Value between 0 and 1.
Optional parameters

+q=<value>
   Set the \( q \) constant.

+alpha=<value>
   Set the \( \alpha \) constant.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+ellps=<value>
   See \texttt{proj -le} for a list of available ellipsoids.
   Defaults to “GRS80”.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with \texttt{+ellps +R} takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.124 Urmaev Flat-Polar Sinusoidal

![Map of the world with the Urmaev Flat-Polar Sinusoidal projection]

Fig. 119: proj-string: \texttt{+proj=urmfps +n=0.5}
7.1.124.1 Parameters

Note: All parameters are optional for the projection.

+n=<value>
Set the \( n \) constant. Value between 0 and 1.

+lon_0=<value>
Longitude of projection center.

  Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with \+ellps\+R takes precedence.

+x_0=<value>
False easting.

  Defaults to 0.0.

+y_0=<value>
False northing.

  Defaults to 0.0.

7.1.125 Universal Transverse Mercator (UTM)

The Universal Transverse Mercator is a system of map projections divided into sixty zones across the globe, with each zone corresponding to 6 degrees of longitude.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Transverse cylindrical, conformal</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse, Spherical and Elliptical</td>
</tr>
<tr>
<td>Defined area</td>
<td>Within the used zone, but transformations of coordinates in adjacent zones can be expected to be accurate as well</td>
</tr>
<tr>
<td>Alias</td>
<td>utm</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

UTM projections are really the Transverse Mercator to which specific parameters, such as central meridians, have been applied. The Earth is divided into 60 zones each generally 6° wide in longitude. Bounding meridians are evenly divisible by 6°, and zones are numbered from 1 to 60 proceeding east from the 180th meridian from Greenwich with minor exceptions [Snyder1987].
PROJ coordinate transformation software library, Release 6.1.1

Fig. 120: UTM zones.

7.1.125.1 Usage

Convert geodetic coordinate to UTM Zone 32 on the northern hemisphere:

```
$ echo 12 56 | proj +proj=utm +zone=32
687071.44 6210141.33
```

Convert geodetic coordinate to UTM Zone 59 on the southern hemisphere:

```
$ echo 174 -44 | proj +proj=utm +zone=59 +south
740526.32 5123750.87
```

7.1.125.2 Parameters

Required

+zone=<value>

Select which UTM zone to use. Can be a value between 1-60.

Optional

+south

Add this flag when using the UTM on the southern hemisphere.

+approx

New in version 6.0.0.

Use faster, less accurate algorithm for the Transverse Mercator.
+ellps=<value>
   See `proj -le` for a list of available ellipsoids.
   
   Defaults to “GRS80”.

7.1.125.3 Further reading

1. Wikipedia

7.1.126 van der Grinten (I)

Fig. 121: proj-string: `+proj=vandj`
7.1.126.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.

7.1.127 van der Grinten II

7.1.127.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.
Fig. 122: proj-string: +proj=vandg2
7.1.128 van der Grinten III

Fig. 123: proj-string: +proj=vandg3

7.1.128.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
   Longitude of projection center.
   *Defaults to 0.0.*

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   *Defaults to 0.0.*
PROJ coordinate transformation software library, Release 6.1.1

+y_0=<value>
False northing.

Defaults to 0.0.

7.1.129 van der Grinten IV

Fig. 124: proj-string: +proj=vandg4

7.1.129.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
Longitude of projection center.

Defaults to 0.0.

+R=<value>
Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
False easting.

Defaults to 0.0.

+y_0=<value>
False northing.

Defaults to 0.0.
7.1.130 Vitkovsky I

Fig. 125: proj-string: +proj=vitk1 +lat_1=45 +lat_2=55

7.1.130.1 Parameters

Required

+lat_1=<value>
First standard parallel.
 Defaults to 0.0.
+lat_2=<value>
Second standard parallel.
 Defaults to 0.0.
Optional

\+lon\_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

\+R=<value>
   Radius of the sphere given in meters. If used in conjunction with \+ellps +R takes precedence.

\+x\_0=<value>
   False easting.
   Defaults to 0.0.

\+y\_0=<value>
   False northing.
   Defaults to 0.0.

7.1.131 Wagner I (Kavraisky VI)

Fig. 126: proj-string: +proj=wag1

7.1.131.1 Parameters

Note: All parameters are optional for the projection.

\+lon\_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

\+R=<value>
   Radius of the sphere given in meters. If used in conjunction with \+ellps +R takes precedence.
Fig. 127: proj-string: +proj=wag2

\[ \begin{align*}
  x &= 0.92483\lambda \cos \theta \\
  y &= 1.38725\theta \\
  \sin \theta &= 0.88022 \sin(0.8855\phi)
\end{align*} \]

### 7.1.132.1 Parameters

**Note:** All parameters are optional for the projection.

- \(+\text{lon}_0=<<\text{value}>\)
  Longitude of projection center.
  *Defaults to 0.0.*

- \(+\text{R}=<<\text{value}>\)
  Radius of the sphere given in meters. If used in conjunction with \(+\text{ellps} +R\) takes precedence.

- \(+x_0=<<\text{value}>\)
  False easting.
  *Defaults to 0.0.*
+y_0=<value>
    False northing.
    Defaults to 0.0.

7.1.133 Wagner III

Fig. 128: proj-string: +proj=wag3

\[
    x = \left[ \cos \phi_{ts} / \cos(2\phi_{ts}/3) \right] \lambda \cos(2\phi/3) \\
    y = \phi
\]

7.1.133.1 Parameters

Note: All parameters are optional for the projection.

+lat_ts=<value>
    Latitude of true scale. Defines the latitude where scale is not distorted. Takes precedence over +k_0 if both options are used together.
    Defaults to 0.0.

+lon_0=<value>
    Longitude of projection center.
    Defaults to 0.0.

+R=<value>
    Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
    False easting.
    Defaults to 0.0.
7.1.134 Wagner IV

Fig. 129: proj-string: +proj=wag4

7.1.134.1 Parameters

**Note:** All parameters are optional.

+lon_0=<value>
   Longitude of projection center.
   *Defaults to 0.0.*

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   *Defaults to 0.0.*

+y_0=<value>
   False northing.
   *Defaults to 0.0.*
7.1.135 Wagner V

![World map showing the Wagner V projection](image)

Fig. 130: proj-string: +proj=wag5

### 7.1.135.1 Parameters

**Note:** All parameters are optional.

- **+lon_0=<value>**
  - Longitude of projection center.
  - *Defaults to 0.0.*

- **+R=<value>**
  - Radius of the sphere given in meters. If used in conjunction with `+ellps +R` takes precedence.

- **+x_0=<value>**
  - False easting.
  - *Defaults to 0.0.*

- **+y_0=<value>**
  - False northing.
  - *Defaults to 0.0.*
7.1.136 Wagner VI

7.1.136.1 Parameters

Note: All parameters are optional for the Wagner VI projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.

+y_0=<value>
   False northing.
   Defaults to 0.0.
7.1.137 Wagner VII

Fig. 132: proj-string: +proj=wag7

7.1.138 Web Mercator / Pseudo Mercator

New in version 5.1.0.

The Web Mercator / Pseudo Mercator projection is a cylindrical map projection. This is a variant of the regular Mercator projection, except that the computation is done on a sphere, using the semi-major axis of the ellipsoid.

From Wikipedia:

This projection is widely used by the Web Mercator, Google Web Mercator, Spherical Mercator, WGS 84 Web Mercator[1] or WGS 84/Pseudo-Mercator is a variant of the Mercator projection and is the de facto standard for Web mapping applications. […] It is used by virtually all major online map providers […] Its official EPSG identifier is EPSG:3857, although others have been used historically.

<table>
<thead>
<tr>
<th>Classification</th>
<th>Cylindrical (non conformant if used with ellipsoid)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Available forms</td>
<td>Forward and inverse</td>
</tr>
<tr>
<td>Defined area</td>
<td>Global</td>
</tr>
<tr>
<td>Alias</td>
<td>webmerc</td>
</tr>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Projected coordinates</td>
</tr>
</tbody>
</table>

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7.1.138.1 Usage

Example:

```
$ echo 2 49 | proj +proj=webmerc +datum=WGS84
222638.98 6274861.39
```

7.1.138.2 Parameters

**Note:** All parameters for the projection are optional, except the ellipsoid definition, which is WGS84 for the typical use case of EPSG:3857. In which case, the other parameters are set to their default 0 value.

+\texttt{ellps=<value>}

See \texttt{proj --le} for a list of available ellipsoids.

*Defaults to “GRS80”.*

+\texttt{lon_0=<value>}

Longitude of projection center.

*Defaults to 0.0.*

+\texttt{x_0=<value>}

False easting.

*Defaults to 0.0.*

+\texttt{y_0=<value>}

False northing.

*Defaults to 0.0.*

7.1.138.3 Mathematical definition

The formulas describing the Mercator projection are all taken from G. Evenden’s libproj manuals [Evenden2005].

**Forward projection**

\[
x = \lambda
\]

\[
y = \ln \left[ \tan \left( \frac{\pi}{4} + \frac{\phi}{2} \right) \right]
\]
Inverse projection

\[\lambda = x\]
\[\phi = \frac{\pi}{2} - 2 \arctan \left( e^{-y} \right)\]

7.1.138.4 Further reading

1. Wikipedia

7.1.139 Werenskiold I

Fig. 133: proj-string: +proj=weren

7.1.139.1 Parameters

Note: All parameters are optional for the projection.

+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.

+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.

+x_0=<value>
   False easting.
   Defaults to 0.0.
\[ +y_0 = \text{value} \]
False northing.
\[ \text{Defaults to 0.0.} \]

### 7.1.140 Winkel I

Fig. 134: proj-string: +proj=wink1

#### 7.1.140.1 Parameters

**Note:** All parameters are optional for the projection.

\[ +\text{lat}_ts = \text{value} \]
Latitude of true scale. Defines the latitude where scale is not distorted. Takes precedence over \( +k_0 \) if both options are used together.
\[ \text{Defaults to 0.0.} \]

\[ +\text{lon}_0 = \text{value} \]
Longitude of projection center.
\[ \text{Defaults to 0.0.} \]

\[ +R = \text{value} \]
Radius of the sphere given in meters. If used in conjunction with \( +\text{ellps} +R \) takes precedence.

\[ +x_0 = \text{value} \]
False easting.
\[ \text{Defaults to 0.0.} \]

\[ +y_0 = \text{value} \]
False northing.
\[ \text{Defaults to 0.0.} \]
7.1.141 Winkel II

Fig. 135: proj-string: +proj=wink2

7.1.141.1 Parameters

Note: All parameters are optional for the projection.

+lat_ts=<value>
  Latitude of true scale. Defines the latitude where scale is not distorted. Takes precedence over +k_0 if both options are used together.
  Defaults to 0.0.
+lon_0=<value>
  Longitude of projection center.
  Defaults to 0.0.
+R=<value>
  Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
  False easting.
  Defaults to 0.0.
+y_0=<value>
  False northing.
  Defaults to 0.0.
7.1.142 Winkel Tripel

Fig. 136: proj-string: +proj=wintri

7.1.142.1 Parameters

Note: All parameters are optional for the projection.

+lat_1=<value>
   First standard parallel.
   Defaults to 0.0.
+lon_0=<value>
   Longitude of projection center.
   Defaults to 0.0.
+R=<value>
   Radius of the sphere given in meters. If used in conjunction with +ellps +R takes precedence.
+x_0=<value>
   False easting.
   Defaults to 0.0.
+y_0=<value>
   False northing.
   Defaults to 0.0.
7.2 Conversions

Conversions are coordinate operations in which both coordinate reference systems are based on the same datum. In PROJ projections are differentiated from conversions.

7.2.1 Axis swap

New in version 5.0.0.
Change the order and sign of 2, 3 or 4 axes.

Each of the possible four axes are numbered with 1–4, such that the first input axis is 1, the second is 2 and so on. The output ordering is controlled by a list of the input axes re-ordered to the new mapping.

7.2.1.1 Usage

Reversing the order of the axes:

```
+proj=axisswap +order=4,3,2,1
```

Swapping the first two axes (x and y):

```
+proj=axisswap +order=2,1,3,4
```

The direction, or sign, of an axis can be changed by adding a minus in front of the axis-number:

```
+proj=axisswap +order=1,-2,3,4
```

It is only necessary to specify the axes that are affected by the swap operation:

```
+proj=axisswap +order=2,1
```

7.2.1.2 Parameters

`+order=<list>`
Ordered comma-separated list of axis, e.g. `+order=2,1,3,4`. Adding a minus in front of an axis number results in a change of direction for that axis, e.g. southward instead of northward.

*Required.*
7.2.2 Geodetic to cartesian conversion

New in version 5.0.0.
Convert geodetic coordinates to cartesian coordinates (in the forward path).

<table>
<thead>
<tr>
<th>Alias</th>
<th>cart</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>3D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Geocentric cartesian coordinates</td>
</tr>
</tbody>
</table>

This conversion converts geodetic coordinate values (longitude, latitude, elevation above ellipsoid) to their geocentric (X, Y, Z) representation, where the first axis (X) points from the Earth centre to the point of longitude=0, latitude=0, the second axis (Y) points from the Earth centre to the point of longitude=90, latitude=0 and the third axis (Z) points to the North pole.

7.2.2.1 Usage

Convert geodetic coordinates to GRS80 cartesian coordinates:

```
echo 17.7562015132 45.3935192042 133.12 2017.8 | cct +proj=cart +ellps=GRS80
4272922.1553 1368283.0597 4518261.3501 2017.8000
```

7.2.2.2 Parameters

```
+ellps=<value>
```

See `proj -le` for a list of available ellipsoids.

Default to “GRS80”.

7.2.3 Geocentric Latitude

New in version 5.0.0.
Convert from Geodetic Latitude to Geocentric Latitude (in the forward path).

<table>
<thead>
<tr>
<th>Alias</th>
<th>geoc</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Geocentric angular coordinates</td>
</tr>
</tbody>
</table>

The geodetic (or geographic) latitude (also called planetographic latitude in the context of non-Earth bodies) is the angle between the equatorial plane and the normal (vertical) to the ellipsoid surface at the considered point. The geodetic latitude is what is normally used everywhere in PROJ when angular coordinates are expected or produced.

The geocentric latitude (also called planetocentric latitude in the context of non-Earth bodies) is the angle between the equatorial plane and a line joining the body centre to the considered point.
7.2.3.1 Mathematical definition

The formulas describing the conversion are taken from [Snyder1987] (equation 3-28)

Let $\phi'$ to be the geocentric latitude and $\phi$ the geodetic latitude, then

$$\phi' = \arctan \left( (1 - e^2) \tan(\phi) \right)$$

The geocentric latitude is consequently lesser (in absolute value) than the geodetic latitude, except at the equator and the poles where they are equal.

On a sphere, they are always equal.

7.2.3.2 Usage

Converting from geodetic latitude to geocentric latitude:

```
+proj=geoc +ellps=GRS80
```

Converting from geocentric latitude to geodetic latitude:

```
+proj=pipeline +step +proj=geoc +inv +ellps=GRS80
```
7.2.3.3 Parameters

+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.

7.2.4 Lat/long (Geodetic alias)

Passes geodetic coordinates through unchanged.

<table>
<thead>
<tr>
<th>Aliases</th>
<th>latlon, latlong, lonlat, longlat</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>2D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Geodetic coordinates</td>
</tr>
</tbody>
</table>

Note: Can not be used with the proj application.

7.2.4.1 Parameters

No parameters will affect the output of the operation if used on it’s own. However, the parameters below can be used in a declarative manner when used with cs2cs or in a transformation pipeline.

+ellps=<value>
   See proj -le for a list of available ellipsoids.
   Defaults to “GRS80”.
+datum=<value>
   Declare the datum used with the coordinates. See cs2cs -l for a list of available datums.
+towgs84=<list>
   A list of three or seven Helmert parameters that maps the input coordinates to the WGS84 datum.

7.2.5 No operation

New in version 6.1.0.

Pass a coordinate through unchanged.

<table>
<thead>
<tr>
<th>Alias</th>
<th>noop</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>4D</td>
</tr>
<tr>
<td>Input type</td>
<td>Any</td>
</tr>
<tr>
<td>Output type</td>
<td>Any</td>
</tr>
</tbody>
</table>

The no operation is a dummy operation that returns whatever is passed to it as seen in this example:

$ echo 12 34 56 78 | cct +proj=noop
12.0000 34.0000 56.0000 78.0000

The operation has no options and default options will not affect the output.
**7.2.6 Pop coordinate value to pipeline stack**

New in version 6.0.0.

Retrieve components of a coordinate that was saved in a previous pipeline step.

<table>
<thead>
<tr>
<th>Alias</th>
<th>pop</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>4D</td>
</tr>
<tr>
<td>Input type</td>
<td>Any</td>
</tr>
<tr>
<td>Output type</td>
<td>Any</td>
</tr>
</tbody>
</table>

This operation makes it possible to retrieve coordinate components that were saved in previous pipeline steps. A retrieved coordinate component is loaded, or popped, from a memory stack that is part of a **pipeline**. The pipeline coordinate stack is inspired by the stack data structure that is commonly used in computer science. There’s four stacks available: one for each coordinate dimension. The dimensions, or coordinate components, are numbered 1–4. It is only possible to move data to and from the stack within the same coordinate component number. Values can be saved to the stack by using the **push operation**.

If the pop operation is used by itself, e.g. not in a pipeline, it will function as a no-operation that passes the coordinate through unchanged. Similarly, if no coordinate component is available on the stack to be popped the operation does nothing.

**7.2.6.1 Examples**

A common use of the **push** and pop operations is in 3D **Helmert** transformations where only the horizontal components are needed. This is often the case when combining heights from a legacy vertical reference with a modern geocentric reference. Below is an example of such a transformation, where the horizontal part is transformed with a Helmert operation but the vertical part is kept exactly as the input was.

```
$ echo 12 56 12.3 2020 | cct +proj=pipeline \
+step +proj=push +v_3 \
+step +proj=cart +ellps=GRS80 \
+step +proj=helmert +x=3000 +y=1000 +z=2000 \
+step +proj=cart +ellps=GRS80 +inv \
+step +proj=pop +v_3 \
```

```
12.0056753463 55.9866540552 12.3000 2000.0000
```

Note that the third coordinate component in the output is the same as the input.

The same transformation without the push and pop operations would look like this:

```
$ echo 12 56 12.3 2020 | cct +proj=pipeline \
+step +proj=cart +ellps=GRS80 \
+step +proj=helmert +x=3000 +y=1000 +z=2000 \
+step +proj=cart +ellps=GRS80 +inv \
```

```
12.0057 55.9867 3427.7404 2000.0000
```

Here the vertical component is adjusted significantly.
7.2.6.2 Parameters

+v_1
Retrieves the first coordinate component from the pipeline stack

+v_2
Retrieves the second coordinate component from the pipeline stack

+v_3
Retrieves the third coordinate component from the pipeline stack

+v_4
Retrieves the fourth coordinate component from the pipeline stack

7.2.6.3 Further reading

1. Stack data structure on Wikipedia

7.2.7 Push coordinate value to pipeline stack

New in version 6.0.0.

Save components of a coordinate from one step of a pipeline and make it available for retrieving in another pipeline step.

<table>
<thead>
<tr>
<th>Alias</th>
<th>push</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>4D</td>
</tr>
<tr>
<td>Input type</td>
<td>Any</td>
</tr>
<tr>
<td>Output type</td>
<td>Any</td>
</tr>
</tbody>
</table>

This operation allows for components of coordinates to be saved for application in a later step. A saved coordinate component is moved, or *pushed*, to a memory stack that is part of a pipeline. The pipeline coordinate stack is inspired by the stack data structure that is commonly used in computer science. There’s four stacks available: One for each coordinate dimension. The dimensions, or coordinate components, are numbered 1–4. It is only possible to move data to and from the stack within the same coordinate component number. Values can be moved off the stack again by using the *pop operation*.

If the push operation is used by itself, e.g. not in a pipeline, it will function as a no-operation that passes the coordinate through unchanged.

7.2.7.1 Examples

A common use of the push and *pop* operations is in 3D *Helmert* transformations where only the horizontal components are needed. This is often the case when combining heights from a legacy vertical reference with a modern geocentric reference. Below is an example of such a transformation, where the horizontal part is transformed with a Helmert operation but the vertical part is kept exactly as the input was.

```bash
$ echo 12 56 12.3 2020 | cct +proj=pipeline \
+step +proj=push +v_3 \
+step +proj=cart +ellps=GRS80 \
+step +proj=helmert +x=3000 +y=1000 +z=2000 \
+step +proj=cart +ellps=GRS80 +inv \
+step +proj=pop +v_3
```

(continues on next page)
Note that the third coordinate component in the output is the same as the input.

The same transformation without the push and pop operations would look like this:

```
$ echo 12 56 12.3 2020 | cct +proj=pipeline \n+step +proj=cart +ellps=GRS80 \n+step +proj=helmert +x=3000 +y=1000 +z=2000 \n+step +proj=cart +ellps=GRS80 +inv \n 12.0057 55.9867 3427.7404 2000.0000
```

Here the vertical component is adjusted significantly.

### 7.2.7.2 Parameters

+\(v_1\)
  Stores the first coordinate component on the pipeline stack

+\(v_2\)
  Stores the second coordinate component on the pipeline stack

+\(v_3\)
  Stores the third coordinate component on the pipeline stack

+\(v_4\)
  Stores the fourth coordinate component on the pipeline stack

### 7.2.7.3 Further reading

1. Stack data structure on Wikipedia

### 7.2.8 Unit conversion

New in version 5.0.0.

Convert between various distance, angular and time units.

<table>
<thead>
<tr>
<th>Alias</th>
<th>unitconvert</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>2D, 3D or 4D</td>
</tr>
<tr>
<td>Input type</td>
<td>Any</td>
</tr>
<tr>
<td>Output type</td>
<td>Any</td>
</tr>
</tbody>
</table>

There are many examples of coordinate reference systems that are expressed in other units than the meter. There are also many cases where temporal data has to be translated to different units. The `unitconvert` operation takes care of that.

Many North American systems are defined with coordinates in feet. For example in Vermont:
Often when working with GNSS data the timestamps are presented in GPS-weeks, but when the data transformed with the helmert operation timestamps are expected to be in units of decimalyears. This can be fixed with unitconvert:

```
+proj=pipeline
+step +proj=unitconvert +xy_in=m +xy_out=us-ft
```

### 7.2.8.1 Parameters

- **+xy_in=<unit> or <conversion_factor>**
  
  Horizontal input units. See Distance units and Angular units for a list of available units. `<conversion_factor>` is the conversion factor from the input unit to metre for linear units, or to radian for angular units.

- **+xy_out=<unit> or <conversion_factor>**
  
  Horizontal output units. See Distance units and Angular units for a list of available units. `<conversion_factor>` is the conversion factor from the output unit to metre for linear units, or to radian for angular units.

- **+z_in=<unit> or <conversion_factor>**
  
  Vertical input units. See Distance units and Angular units for a list of available units. `<conversion_factor>` is the conversion factor from the input unit to metre for linear units, or to radian for angular units.

- **+z_out=<unit> or <conversion_factor>**
  
  Vertical output units. See Distance units and Angular units for a list of available units. `<conversion_factor>` is the conversion factor from the output unit to metre for linear units, or to radian for angular units.

- **+t_in=<unit>**
  
  Temporal input units. See Time units for a list of available units.

- **+t_out=<unit>**
  
  Temporal output units. See Time units for a list of available units.
7.2.8.2 Distance units

In the table below all distance units supported by PROJ are listed. The same list can also be produced on the command line with `proj` or `cs2cs`, by adding the `-lu` flag when calling the utility.

<table>
<thead>
<tr>
<th>Label</th>
<th>Name</th>
</tr>
</thead>
<tbody>
<tr>
<td>km</td>
<td>Kilometer</td>
</tr>
<tr>
<td>m</td>
<td>Meter</td>
</tr>
<tr>
<td>dm</td>
<td>Decimeter</td>
</tr>
<tr>
<td>cm</td>
<td>Centimeter</td>
</tr>
<tr>
<td>mm</td>
<td>Millimeter</td>
</tr>
<tr>
<td>kmi</td>
<td>International Nautical Mile</td>
</tr>
<tr>
<td>in</td>
<td>International Inch</td>
</tr>
<tr>
<td>ft</td>
<td>International Foot</td>
</tr>
<tr>
<td>yd</td>
<td>International Yard</td>
</tr>
<tr>
<td>mi</td>
<td>International Statute Mile</td>
</tr>
<tr>
<td>fath</td>
<td>International Fathom</td>
</tr>
<tr>
<td>ch</td>
<td>International Chain</td>
</tr>
<tr>
<td>link</td>
<td>International Link</td>
</tr>
<tr>
<td>us-in</td>
<td>U.S. Surveyor’s Inch</td>
</tr>
<tr>
<td>us-ft</td>
<td>U.S. Surveyor’s Foot</td>
</tr>
<tr>
<td>us-yd</td>
<td>U.S. Surveyor’s Yard</td>
</tr>
<tr>
<td>us-ch</td>
<td>U.S. Surveyor’s Chain</td>
</tr>
<tr>
<td>us-mi</td>
<td>U.S. Surveyor’s Statute Mile</td>
</tr>
<tr>
<td>ind-yd</td>
<td>Indian Yard</td>
</tr>
<tr>
<td>ind-ft</td>
<td>Indian Foot</td>
</tr>
<tr>
<td>ind-ch</td>
<td>Indian Chain</td>
</tr>
</tbody>
</table>

7.2.8.3 Angular units

New in version 5.2.0.

In the table below all angular units supported by PROJ `unitconvert` are listed.

<table>
<thead>
<tr>
<th>Label</th>
<th>Name</th>
</tr>
</thead>
<tbody>
<tr>
<td>deg</td>
<td>Degree</td>
</tr>
<tr>
<td>grad</td>
<td>Grad</td>
</tr>
<tr>
<td>rad</td>
<td>Radian</td>
</tr>
</tbody>
</table>

7.2.8.4 Time units

In the table below all time units supported by PROJ are listed.

<table>
<thead>
<tr>
<th>Label</th>
<th>Name</th>
</tr>
</thead>
<tbody>
<tr>
<td>mjd</td>
<td>Modified Julian date</td>
</tr>
<tr>
<td>decimalyear</td>
<td>Decimal year</td>
</tr>
<tr>
<td>gps_week</td>
<td>GPS Week</td>
</tr>
<tr>
<td>yyyyymmdd</td>
<td>Date in yyyyymmdd format</td>
</tr>
</tbody>
</table>
7.3 Transformations

Transformations coordinate operation in which the two coordinate reference systems are based on different datums.

7.3.1 Affine transformation

New in version 6.0.0.

The affine transformation applies translation and scaling/rotation terms on the x,y,z coordinates, and translation and scaling on the temporal coordinate.

<table>
<thead>
<tr>
<th>Alias</th>
<th>affine</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>4D</td>
</tr>
<tr>
<td>Input type</td>
<td>XYZT</td>
</tr>
<tr>
<td>output type</td>
<td>XYZT</td>
</tr>
</tbody>
</table>

By default, the parameters are set for an identity transforms. The transformation is reversible unless the determinant of the sj  matrix is 0, or tscale is 0.

7.3.1.1 Parameters

Optional

+\textit{xoff}=\textit{<value>}
  Offset in X. Default value: 0

+\textit{yoff}=\textit{<value>}
  Offset in Y. Default value: 0

+\textit{zoff}=\textit{<value>}
  Offset in Z. Default value: 0

+\textit{toff}=\textit{<value>}
  Offset in T. Default value: 0

+\textit{s11}=\textit{<value>}
  Rotation/scaling term. Default value: 1

+\textit{s12}=\textit{<value>}
  Rotation/scaling term. Default value: 0

+\textit{s13}=\textit{<value>}
  Rotation/scaling term. Default value: 0

+\textit{s21}=\textit{<value>}
  Rotation/scaling term. Default value: 0

+\textit{s22}=\textit{<value>}
  Rotation/scaling term. Default value: 1

+\textit{s23}=\textit{<value>}
  Rotation/scaling term. Default value: 0

+\textit{s31}=\textit{<value>}
  Rotation/scaling term. Default value: 0
+s32=<value>
Rotation/scaling term. Default value: 0

+s33=<value>
Rotation/scaling term. Default value: 1

+tscale=<value>
Time scaling term. Default value: 1

### Mathematical description

\[
\begin{bmatrix}
X \\
Y \\
Z \\
T \\
\end{bmatrix}_{\text{dest}} = \begin{bmatrix}
\text{xoff} \\
\text{yoff} \\
\text{zoff} \\
\text{toff} \\
\end{bmatrix} + \begin{bmatrix}
s11 & s12 & s13 & 0 \\
s21 & s22 & s23 & 0 \\
s31 & s32 & s33 & 0 \\
0 & 0 & 0 & \text{tscale} \\
\end{bmatrix} \begin{bmatrix}
X \\
Y \\
Z \\
T \\
\end{bmatrix}_{\text{source}} \tag{7.1}
\]

#### 7.3.2 Kinematic datum shifting utilizing a deformation model

New in version 5.0.0.

Perform datum shifts means of a deformation/velocity model.

<table>
<thead>
<tr>
<th>Input type</th>
<th>Cartesian coordinates (spatial), decimalyears (temporal).</th>
</tr>
</thead>
<tbody>
<tr>
<td>Output type</td>
<td>Cartesian coordinates (spatial), decimalyears (temporal).</td>
</tr>
<tr>
<td>Domain</td>
<td>4D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Geodetic coordinates</td>
</tr>
</tbody>
</table>

The deformation operation is used to adjust coordinates for intraplate deformations. Usually the transformation parameters for regional plate-fixed reference frames such as the ETRS89 does not take intraplate deformation into account. It is assumed that tectonic plate of the region is rigid. Often times this is true, but near the plate boundary and in areas with post-glacial uplift the assumption breaks. Intraplate deformations can be modelled and then applied to the coordinates so that they represent the physical world better. In PROJ this is done with the deformation operation.

The horizontal grid is stored in CTable2 format and the vertical grid is stored in the GTX format. Both grids are expected to contain grid-values in units of mm/year. GDAL both reads and writes both file formats. Using GDAL for construction of new grids is recommended.

#### 7.3.2.1 Example

In [Hakli2016] coordinate transformation including a deformation model is described. The paper describes how coordinates from the global ITRFxx frames are transformed to the local Nordic realisations of ETRS89. Scandinavia is an area with significant post-glacial rebound. The deformations from the post-glacial uplift is not accounted for in the official ETRS89 transformations so in order to get accurate transformations in the Nordic countries it is necessary to apply the deformation model. The transformation from ITRF2008 to the Danish realisation of ETRS89 is in PROJ described as:

```bash
proj = pipeline ellps = GRS80
    # ITRF2008@t_obs -> ITRF2000@t_obs
step  init = ITRF2008:ITRF2000
    # ITRF2000@t_obs -> ETRF2000@t_obs
```

(continues on next page)
From this we can see that the transformation from ITRF2008 to the Danish realisation of ETRS89 is a combination of Helmert transformations and adjustments with a deformation model. The first use of the deformation operation is:

```
proj = deformation t_epoch = 2000.0
xy_grids = ./nkgrf03vel_realigned_xy.ct2
z_grids = ./nkgrf03vel_realigned_z.gtx
```

Here we set the central epoch of the transformation, 2000.0. The observation epoch is expected as part of the input coordinate tuple. The deformation model is described by two grids, specified with `+xy_grids` and `+z_grids`. The first is the horizontal part of the model and the second is the vertical component.

### 7.3.2.2 Parameters

**+xy_grids=<list>**

Comma-separated list of grids to load. If a grid is prefixed by an @ the grid is considered optional and PROJ will the not complain if the grid is not available.

Grids for the horizontla component of a deformation model is expected to be in CTable2 format.

**+z_grids=<list>**

Comma-separated list of grids to load. If a grid is prefixed by an @ the grid is considered optional and PROJ will the not complain if the grid is not available.

Grids for the vertical component of a deformation model is expected to be in either GTX format.

**+t_epoch=<value>**

Central epoch of transformation given in decimalyears. Will be used in conjunction with the observation time from the input coordinate to determine $dt$ as used in eq. (7.1) below.

Note: $+t_epoch$ is mutually exclusive with $+dt$.

**+dt=<value>**

New in version 6.0.0.

$dt$ as used in eq. (7.1) below. Is useful when no observation time is available in the input coordinate or when a deformation for a specific timespan needs to be applied in a transformation. $dt$ is given in units of decimalyears.
Note: \( +dt \) is mutually exclusive with \( +t_{\text{epoch}} \)

### 7.3.2.3 Mathematical description

Mathematically speaking, application of a deformation model is simple. The deformation model is represented as a grid of velocities in three dimensions. Coordinate corrections are applied in cartesian space. For a given coordinate, \((X, Y, Z)\), velocities \((V_X, V_Y, V_Z)\) can be interpolated from the gridded model. The time span between \(t_{\text{obs}}\) and \(t_c\) determine the magnitude of the coordinate correction as seen in eq. (7.1) below.

\[
\begin{bmatrix}
X \\
Y \\
Z \\
\end{bmatrix}_B = \begin{bmatrix}
X \\
Y \\
Z \\
\end{bmatrix}_A + (t_{\text{obs}} - t_c) \begin{bmatrix}
V_X \\
V_Y \\
V_Z \\
\end{bmatrix} \\
\tag{7.1}
\]

Corrections are done in cartesian space.

Coordinates of the gridded model are in ENU (east, north, up) space because it would otherwise require an enormous 3 dimensional grid to handle the corrections in cartesian space. Keeping the correction in lat/long space reduces the complexity of the grid significantly. Consequently though, the input coordinates needs to be converted to lat/long space when searching for corrections in the grid. This is done with the \( \text{cart} \) operation. The converted grid corrections can then be applied to the input coordinates in cartesian space. The conversion from ENU space to cartesian space is done in the following way:

\[
\begin{bmatrix}
X \\
Y \\
Z \\
\end{bmatrix} = \begin{bmatrix}
-\sin \phi \cos \lambda N - \sin \lambda E + \cos \phi \cos \lambda U \\
-\sin \phi \sin \lambda N + \sin \lambda E + \cos \phi \sin \lambda U \\
\cos \phi N + \sin \phi U \\
\end{bmatrix} \\
\tag{7.1}
\]

where \( \phi \) and \( \lambda \) are the latitude and longitude of the coordinate that is searched for in the grid. \((E, N, U)\) are the grid values in ENU-space and \((X, Y, Z)\) are the corrections converted to cartesian space.

### 7.3.2.4 See also

1. *Behavioural changes from version 5 to 6*

### 7.3.3 Geographic offsets

New in version 6.0.0.

The Geographic offsets transformation adds an offset to the geographic longitude, latitude coordinates, and an offset to the ellipsoidal height.

<table>
<thead>
<tr>
<th>Alias</th>
<th>geogoffset</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>3D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates (horizontal), meters (vertical)</td>
</tr>
<tr>
<td>Output type</td>
<td>Geodetic coordinates (horizontal), meters (vertical)</td>
</tr>
</tbody>
</table>

This method is normally only used when low accuracy is tolerated. It is documented as coordinate operation method code 9619 (for geographic 2D) and 9660 (for geographic 3D) in the EPSG dataset ([IOGP2018])

It can also be used to implement the method Geographic2D with Height Offsets (code 9618) by noting that the input vertical component is a gravity-related height and the output vertical component is the ellipsoid height (dh being the geoid undulation).
It can also be used to implement the method Vertical offset (code 9616).
The reverse transformation simply consists in subtracting the offsets.
This method is a convenience wrapper for the more general Affine transformation.

### 7.3.3.1 Examples

Geographic offset from the old Greek geographic 2D CRS to the newer GGRS87 CRS:

```
proj=geogoffset dlon=0.28 dlat=-5.86
```

Conversion from Tokyo + JSLD69 height to WGS 84:

```
proj=geogoffset dlon=-13.97 dlat=7.94 dh=26.9
```

Conversion from Baltic 1977 height to Black Sea height:

```
proj=geogoffset dh=0.4
```

### 7.3.3.2 Parameters

Optional

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>+dlon=&lt;value&gt;</td>
<td>Offset in longitude, expressed in arc-second, to add.</td>
</tr>
<tr>
<td>+dlat=&lt;value&gt;</td>
<td>Offset in latitude, expressed in arc-second, to add.</td>
</tr>
<tr>
<td>+dh=&lt;value&gt;</td>
<td>Offset in height, expressed in meter, to add.</td>
</tr>
</tbody>
</table>

### 7.3.4 Helmert transform

New in version 5.0.0.

The Helmert transformation changes coordinates from one reference frame to another by means of 3-, 4- and 7-parameter shifts, or one of their 6-, 8- and 14-parameter kinematic counterparts.

<table>
<thead>
<tr>
<th>Alias</th>
<th>helmert</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>2D, 3D and 4D</td>
</tr>
<tr>
<td>Input type</td>
<td>Cartesian coordinates (spatial), decimalyears (temporal).</td>
</tr>
<tr>
<td>Output type</td>
<td>Cartesian coordinates (spatial), decimalyears (temporal).</td>
</tr>
<tr>
<td>Input type</td>
<td>Cartesian coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Cartesian coordinates</td>
</tr>
</tbody>
</table>

The Helmert transform, in all its various incarnations, is used to perform reference frame shifts. The transformation operates in cartesian space. It can be used to transform planar coordinates from one datum to another, transform 3D cartesian coordinates from one static reference frame to another or it can be used to do fully kinematic transformations from global reference frames to local static frames.

All of the parameters described in the table above are marked as optional. This is true as long as at least one parameter is defined in the setup of the transformation. The behaviour of the transformation depends on which parameters are
used in the setup. For instance, if a rate of change parameter is specified a kinematic version of the transformation is used.

The kinematic transformations require an observation time of the coordinate, as well as a central epoch for the transformation. The latter is usually documented alongside the rest of the transformation parameters for a given transformation. The central epoch is controlled with the parameter \( t_{epoch} \). The observation time is given as part of the coordinate when using PROJ’s 4D-functionality.

### 7.3.4.1 Examples

Transforming coordinates from NAD72 to NAD83 using the 4 parameter 2D Helmert:

```
proj=helmert
convention=coordinate_frame
x=-9597.3572
y=.6112
s=0.304794780637
theta=-1.244048
```

Simplified transformations from ITRF2008/IGS08 to ETRS89 using 7 parameters:

```
proj=helmert
convention=coordinate_frame
x=0.67678
y=0.65495
z=-0.52827
rx=-0.022742
ry=0.012667
rz=0.022704
s=-0.01070
```

Transformation from \( \text{ITRF2000} \) to \( \text{ITRF93} \) using 15 parameters:

```
proj=helmert
convention=position_vector
x=0.0127
y=0.0065
z=-0.0209
s=0.00195
dx=-0.0029
dy=-0.0002
dz=-0.0006
ds=0.00001
rx=-0.00039
ry=0.00080
rz=-0.00114
drx=-0.00011
dry=-0.00019
drz=0.00007
t_epoch=1988.0
```

### 7.3.4.2 Parameters

**Note:** All parameters are optional but at least one should be used, otherwise the operation will return the coordinates unchanged.

+\texttt{convention=coordinate_frame/position\_vector}

New in version 5.2.0.

Indicates the convention to express the rotational terms when a 3D-Helmert / 7-parameter more transform is involved. As soon as a rotational parameter is specified (one of \( \text{rx, ry, rz, drx, dry, drz} \)), \texttt{convention} is required.

The two conventions are equally popular and a frequent source of confusion. The coordinate frame convention is also described as an clockwise rotation of the coordinate frame. It corresponds to EPSG method code 1032 (in the geocentric domain) or 9607 (in the geographic domain) The position vector convention is also described as an anticlockwise (counter-clockwise) rotation of the coordinate frame. It corresponds to as EPSG method code 1033 (in the geocentric domain) or 9606 (in the geographic domain).

This parameter is ignored when only a 3-parameter (translation terms only: \( x, y, z \)), 4-parameter (3-parameter and \( \text{theta} \)) or 6-parameter (3-parameter and their derivative terms) is used.

The result obtained with parameters specified in a given convention can be obtained in the other convention by negating the rotational parameters (\( \text{rx, ry, rz, drx, dry, drz} \))
Note: This parameter obsoletes \texttt{transpose} which was present in PROJ 5.0 and 5.1, and is forbidden starting with PROJ 5.2

\[+x=<\text{value}>\]  
Translation of the x-axis given in meters.

\[+y=<\text{value}>\]  
Translation of the y-axis given in meters.

\[+z=<\text{value}>\]  
Translation of the z-axis given in meters.

\[+s=<\text{value}>\]  
Scale factor given in ppm.

\[+rx=<\text{value}>\]  
X-axis rotation in the 3D Helmert given arc seconds.

\[+ry=<\text{value}>\]  
Y-axis rotation in the 3D Helmert given arc seconds.

\[+rz=<\text{value}>\]  
Z-axis rotation in the 3D Helmert given arc seconds.

\[+\theta=<\text{value}>\]  
Rotation angle in the 2D Helmert given in arc seconds.

\[+dx=<\text{value}>\]  
Translation rate of the x-axis given in m/year.

\[+dy=<\text{value}>\]  
Translation rate of the y-axis given in m/year.

\[+dz=<\text{value}>\]  
Translation rate of the z-axis given in m/year.

\[+ds=<\text{value}>\]  
Scale rate factor given in ppm/year.

\[+drx=<\text{value}>\]  
Rotation rate of the x-axis given in arc seconds/year.

\[+dry=<\text{value}>\]  
Rotation rate of the y-axis given in arc seconds/year.

\[+drz=<\text{value}>\]  
Rotation rate of the y-axis given in arc seconds/year.

\[+t\_epoch=<\text{value}>\]  
Central epoch of transformation given in decimal year. Only used spatiotemporal transformations.

\[+\text{exact}\]  
Use exact transformation equations.

See (7.6)

\[+\text{transpose}\]  
Deprecated since version 5.2.0: (removed)

Transpose rotation matrix and follow the \texttt{Position Vector} rotation convention. If \texttt{transpose} is not added the \texttt{Coordinate Frame} rotation convention is used.
7.3.4.3 Mathematical description

In the notation used below, \( \dot{P} \) is the rate of change of a given transformation parameter \( P \). \( \dot{P} \) is the kinematically adjusted version of \( P \), described by

\[
\dot{P} = P + \dot{P} (t - t_{\text{central}})
\]

where \( t \) is the observation time of the coordinate and \( t_{\text{central}} \) is the central epoch of the transformation. Equation (7.1) can be used to propagate all transformation parameters in time.

Superscripts of vectors denote the reference frame the coordinates in the vector belong to.

2D Helmert

The simplest version of the Helmert transform is the 2D case. In the 2-dimensional case only the horizontal coordinates are changed. The coordinates can be translated, rotated and scaled. Translation is controlled with the \( x \) and \( y \) parameters.

The rotation is determined by \( \theta \) and the scale is controlled with the \( s \) parameters.

Note: The scaling parameter \( s \) is unitless for the 2D Helmert, as opposed to the 3D version where the scaling parameter is given in units of ppm.

Mathematically the 2D Helmert is described as:

\[
\begin{bmatrix}
X \\
Y 
\end{bmatrix}^B = \begin{bmatrix}
T_x \\
T_y 
\end{bmatrix} + s \begin{bmatrix}
\cos \theta & \sin \theta \\
-\sin \theta & \cos \theta 
\end{bmatrix} \begin{bmatrix}
X \\
Y 
\end{bmatrix}^A
\]

(7.2)

(7.2) can be extended to a time-varying kinematic version by adjusting the parameters with (7.1) to (7.2), which yields the kinematic 2D Helmert transform:

\[
\begin{bmatrix}
X \\
Y 
\end{bmatrix}^B = \begin{bmatrix}
\dot{T}_x \\
\dot{T}_y 
\end{bmatrix} + s(t) \begin{bmatrix}
\cos \dot{\theta} & \sin \dot{\theta} \\
-\sin \dot{\theta} & \cos \dot{\theta} 
\end{bmatrix} \begin{bmatrix}
X \\
Y 
\end{bmatrix}^A
\]

(7.2)

All parameters in (7.2) are determined by the use of (7.1), which applies the rate of change to each individual parameter for a given timespan between \( t \) and \( t_{\text{central}} \).

3D Helmert

The general form of the 3D Helmert is

\[
V^B = T + \left( 1 + s \times 10^{-6} \right) RV^A
\]

(7.2)

Where \( T \) is a vector consisting of the three translation parameters, \( s \) is the scaling factor and \( R \) is a rotation matrix. \( V^A \) and \( V^B \) are coordinate vectors, with \( V^A \) being the input coordinate and \( V^B \) is the output coordinate.

In the Position Vector convention, we define \( R_x = \text{radians} (rx) \), \( R_z = \text{radians} (ry) \) and \( R_z = \text{radians} (rz) \)

In the Coordinate Frame convention, \( R_x = -\text{radians} (rx) \), \( R_z = -\text{radians} (ry) \) and \( R_z = -\text{radians} (rz) \)

The rotation matrix is composed of three rotation matrices, one for each axis.

\[
R_X = \begin{bmatrix}
1 & 0 & 0 \\
0 & \cos R_x & -\sin R_x \\
0 & \sin R_x & \cos R_x
\end{bmatrix}
\]

(7.2)
The three rotation matrices can be combined in one:

\[ R = R_X R_Y R_Y \]  

(7.5)

For \( R \), this yields:

\[
\begin{bmatrix}
\cos R_y \cos R_z & -\cos R_x \sin R_z + \sin R_x \sin R_z \\
\sin R_x \sin R_y \cos R_z & \cos R_x \sin R_y \cos R_z \\
-\sin R_y & \cos R_y \cos R_z \\
\end{bmatrix}
\]

(7.6)

Using the small angle approximation the rotation matrix can be simplified to

\[
\begin{bmatrix}
1 & -R_z & R_y \\
R_z & 1 & -R_x \\
-R_y & R_x & 1 \\
\end{bmatrix}
\]

(7.7)

Which allow us to express the most common version of the Helmert transform, using the approximated rotation matrix:

\[
\begin{bmatrix}
X \\
Y \\
Z \\
\end{bmatrix}^B = \begin{bmatrix}
T_x \\
T_y \\
T_z \\
\end{bmatrix} + (1 + s \times 10^{-6}) \begin{bmatrix}
1 & -R_z & R_y \\
R_z & 1 & -R_x \\
-R_y & R_x & 1 \\
\end{bmatrix} \begin{bmatrix}
X \\
Y \\
Z \\
\end{bmatrix}^A
\]

(7.7)

If the rotation matrix is transposed, or the sign of the rotation terms negated, the rotational part of the transformation is effectively reversed. This is what happens when switching between the 2 conventions position_vector and coordinate_frame.

Applying (7.1) we get the kinematic version of the approximated 3D Helmert:

\[
\begin{bmatrix}
X \\
Y \\
Z \\
\end{bmatrix}^B = \begin{bmatrix}
T_x \\
T_y \\
T_z \\
\end{bmatrix} + (1 + \dot{s} \times 10^{-6}) \begin{bmatrix}
1 & -\dot{R}_z & \dot{R}_y \\
\dot{R}_z & 1 & -\dot{R}_x \\
-\dot{R}_y & \dot{R}_x & 1 \\
\end{bmatrix} \begin{bmatrix}
X \\
Y \\
Z \\
\end{bmatrix}^A
\]

(7.7)

The Helmert transformation can be applied without using the rotation parameters, in which case it becomes a simple translation of the origin of the coordinate system. When using the Helmert in this version equation (7.2) simplifies to:

\[
\begin{bmatrix}
X \\
Y \\
Z \\
\end{bmatrix}^B = \begin{bmatrix}
T_x \\
T_y \\
T_z \\
\end{bmatrix} + \begin{bmatrix}
X \\
Y \\
Z \\
\end{bmatrix}^A
\]

(7.7)

That after application of (7.1) has the following kinematic counterpart:

\[
\begin{bmatrix}
X \\
Y \\
Z \\
\end{bmatrix}^B = \begin{bmatrix}
T_x \\
T_y \\
T_z \\
\end{bmatrix} + \begin{bmatrix}
X \\
Y \\
Z \\
\end{bmatrix}^A
\]

(7.7)
7.3.5 Horner polynomial evaluation

New in version 5.0.0.

<table>
<thead>
<tr>
<th>Alias</th>
<th>horner</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>2D and 3D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic and projected coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Geodetic and projected coordinates</td>
</tr>
</tbody>
</table>

The Horner polynomial evaluation scheme is used for transformations between reference frames where one or both are inhomogenous or internally distorted. This will typically be reference frames created before the introduction of space geodetic techniques such as GPS.

Horner polynomials, or Multiple Regression Equations as they are also known as, have their strength in being able to create complicated mappings between coordinate reference frames while still being lightweight in both computational cost and disk space used.

PROJ implements two versions of the Horner evaluation scheme: Real and complex polynomial evaluation. Below both are briefly described. For more details consult [Ruffhead2016] and [IOGP2018].

The polynomial evaluation in real number space is defined by the following equations:

\[
\Delta X = \sum_{i,j} u_{i,j} U^i V^j \\
\Delta Y = \sum_{i,j} v_{i,j} U^i V^j
\]  

(7.7)

where

\[U = X_{in} - X_{origin}\]
\[V = Y_{in} - Y_{origin}\]  

(7.8)

and \(u_{i,j}\) and \(v_{i,j}\) are coefficients that make up the polynomial.

The final coordinates are determined as

\[X_{out} = X_{in} + \Delta X\]
\[Y_{out} = Y_{in} + \Delta Y\]  

(7.9)

The inverse transform is the same as the above but requires a different set of coefficients.

Evaluation of the complex polynomials are defined by the following equations:

\[\Delta X + i\Delta Y = \sum_{j=1}^n (c_{2j-1} + ic_{2j})(U + iV)^j\]  

(7.10)

Where \(n\) is the degree of the polynomial. \(U\) and \(V\) are defined as in (7.8) and the resulting coordinates are again determined by (7.9).

7.3.5.1 Examples

Mapping between Danish TC32 and ETRS89/UTM zone 32 using polynomials in real number space:
### Mapping between Danish System Storebælt and ETRS89/UTM zone 32 using complex polynomials:

```
+proj=horner
+ellps=intl
+range=500000
+fwd_origin=8.776057928e+05,9.9999752475e-01,-1.9107771273e-18
+inv_origin=6.1258103208e+06,1.0000002826e+00,-5.5627059451e-15,1
+deg=3
+fwd_c=6.19480258923588e+06,6.1258568148837e+06
+inv_c=4.94690026817276e+06,6.1334211383056e+06
```

### Parameters

Setting up Horner polynomials requires many coefficients being explicitly written, even for polynomials of low degree. For this reason it is recommended to store the polynomial definitions in an *init file* for easier writing and reuse.

#### Required

Below is a list of required parameters that can be set for the Horner polynomial transformation. As stated above, the transformation takes to forms, either using real or complex polynomials. These are divided into separate sections below. Parameters from the two sections are mutually exclusive, that is parameters describing real and complex polynomials can’t be mixed.

+ **ellps=**<em value>

See *proj -le* for a list of available ellipsoids.

*Defaults to “GRS80”.*
+deg=<value>
    Degree of polynomial
+fwd_origin=<northing,easting>
    Coordinate of origin for the forward mapping
+inv_origin=<northing,easting>
    Coordinate of origin for the inverse mapping

Real polynomials

The following parameters has to be set if the transformation consists of polynomials in real space. Each parameter takes a comma-separated list of coefficients. The number of coefficients is governed by the degree, $d$, of the polynomial:

$$N = \frac{(d+1)(d+2)}{2}$$

+fwd_u=<u_{11},u_{12},...,u_{ij},...,u_{mn}>
    Coefficients for the forward transformation i.e. latitude to northing as described in (7.7).
+fwd_v=<v_{11},v_{12},...,v_{ij},...,v_{mn}>
    Coefficients for the forward transformation i.e. longitude to easting as described in (7.7).
+inv_u=<u_{11},u_{12},...,u_{ij},...,u_{mn}>
    Coefficients for the inverse transformation i.e. latitude to northing as described in (7.7).
+inv_v=<v_{11},v_{12},...,v_{ij},...,v_{mn}>
    Coefficients for the inverse transformation i.e. longitude to easting as described in (7.7).

Complex polynomials

The following parameters has to be set if the transformation consists of polynomials in complex space. Each parameter takes a comma-separated list of coefficients. The number of coefficients is governed by the degree, $d$, of the polynomial:

$$N = 2d + 2$$

+fwd_c=<c_{1},c_{2},...,c_{N}>
    Coefficients for the complex forward transformation as described in (7.10).
+inv_c=<c_{1},c_{2},...,c_{N}>
    Coefficients for the complex inverse transformation as described in (7.10).

Optional

+range=<value>
    Radius of the region of validity.
+uneg
    Express latitude as southing. Only applies for complex polynomials.
+vneg
    Express longitude as westing. Only applies for complex polynomials.
7.3.6 Molodensky transform

New in version 5.0.0.

The Molodensky transformation resembles a Helmert transform with zero rotations and a scale of unity, but converts directly from geodetic coordinates to geodetic coordinates, without the intermediate shifts to and from cartesian geocentric coordinates, associated with the Helmert transformation. The Molodensky transformation is simple to implement and to parameterize, requiring only the 3 shifts between the input and output frame, and the corresponding differences between the semimajor axes and flattening parameters of the reference ellipsoids. Due to its algorithmic simplicity, it was popular prior to the ubiquity of digital computers. Today, it is mostly interesting for historical reasons, but nevertheless indispensable due to the large amount of data that has already been transformed that way [EversKnudsen2017].

<table>
<thead>
<tr>
<th>Alias</th>
<th>molodensky</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>3D</td>
</tr>
<tr>
<td>Input type</td>
<td>Geodetic coordinates (horizontal), meters (vertical)</td>
</tr>
<tr>
<td>output type</td>
<td>Geodetic coordinates (horizontal), meters (vertical)</td>
</tr>
</tbody>
</table>

The Molodensky transform can be used to perform a datum shift from coordinate \((\phi_1, \lambda_1, h_1)\) to \((\phi_2, \lambda_2, h_2)\) where the two coordinates are referenced to different ellipsoids. This is based on three assumptions:

1. The cartesian axes, \(X, Y, Z\), of the two ellipsoids are parallel.
2. The offset, \(\delta X, \delta Y, \delta Z\), between the two ellipsoid are known.
3. The characteristics of the two ellipsoids, expressed as the difference in semimajor axis \((\delta a)\) and flattening \((\delta f)\), are known.

The Molodensky transform is mostly used for transforming between old systems dating back to the time before computers. The advantage of the Molodensky transform is that it is fairly simple to compute by hand. The ease of computation come at the cost of limited accuracy.

A derivation of the mathematical formulas for the Molodensky transform can be found in [Deakin2004].

7.3.6.1 Examples

The abridged Molodensky:

```
proj=molodensky a=6378160 rf=298.25 da=-23 df=-8.120449e-8 dx=-134 dy=-48 dz=149
```

The same transformation using the standard Molodensky:

```
proj=molodensky a=6378160 rf=298.25 da=-23 df=-8.120449e-8 dx=-134 dy=-48 dz=149
```
7.3.6.2 Parameters

Required

```
+da=<value>
    Difference in semimajor axis of the defining ellipsoids.
+df=<value>
    Difference in flattening of the defining ellipsoids.
+dx=<value>
    Offset of the X-axes of the defining ellipsoids.
+dy=<value>
    Offset of the Y-axes of the defining ellipsoids.
+dz=<value>
    Offset of the Z-axes of the defining ellipsoids.
+ellps=<value>
    See `proj -le` for a list of available ellipsoids.
    Defaults to “GRS80”.
```

Optional

```
+abridged
    Use the abridged version of the Molodensky transform.
```

7.3.7 Molodensky-Badekas transform

New in version 6.0.0.

The Molodensky-Badekas transformation changes coordinates from one reference frame to another by means of a 10-parameter shift.

**Note:** It should not be confused with the Molodensky transform which operates directly in the geodetic coordinates. Molodensky-Badekas can rather be seen as a variation of Helmert transform.

<table>
<thead>
<tr>
<th>Alias</th>
<th>molobadekas</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>3D</td>
</tr>
<tr>
<td>Input type</td>
<td>Cartesian coordinates</td>
</tr>
<tr>
<td>Output type</td>
<td>Cartesian coordinates</td>
</tr>
</tbody>
</table>

The Molodensky-Badekas transformation is a variation of the Helmert transform where the rotational terms are not directly applied to the ECEF coordinates, but on cartesian coordinates relative to a reference point (usually close to Earth surface, and to the area of use of the transformation). When \( px = py = pz = 0 \), this is equivalent to a 7-parameter Helmert transformation.
7.3.7.1 Example

Transforming coordinates from La Canoa to REGVEN:

```
proj=molobadekas convention=coordinate_frame
    x=-270.933 y=115.599 z=-360.226 rx=-5.266 ry=-1.238 rz=2.381
    s=-5.109 px=2464351.59 py=-5783466.61 pz=974809.81
```

7.3.7.2 Parameters

**Note:** All parameters (except convention) are optional but at least one should be used, otherwise the operation will return the coordinates unchanged.

+**convention**=coordinate_frame/position_vector
  
  Indicates the convention to express the rotational terms when a 3D-Helmert / 7-parameter more transform is involved.

  The two conventions are equally popular and a frequent source of confusion. The coordinate frame convention is also described as an clockwise rotation of the coordinate frame. It corresponds to EPSG method code 1034 (in the geocentric domain) or 9636 (in the geographic domain) The position vector convention is also described as an anticlockwise (counter-clockwise) rotation of the coordinate frame. It corresponds to as EPSG method code 1061 (in the geocentric domain) or 1063 (in the geographic domain).

  The result obtained with parameters specified in a given convention can be obtained in the other convention by negating the rotational parameters \((rx, ry, rz)\)

+**x**=<value>
  
  Translation of the x-axis given in meters.

+**y**=<value>
  
  Translation of the y-axis given in meters.

+**z**=<value>
  
  Translation of the z-axis given in meters.

+**s**=<value>
  
  Scale factor given in ppm.

+**rx**=<value>
  
  X-axis rotation given arc seconds.

+**ry**=<value>
  
  Y-axis rotation given in arc seconds.

+**rz**=<value>
  
  Z-axis rotation given in arc seconds.

+**px**=<value>
  
  Coordinate along the x-axis of the reference point given in meters.

+**py**=<value>
  
  Coordinate along the y-axis of the reference point given in meters.

+**pz**=<value>
  
  Coordinate along the z-axis of the reference point given in meters.
7.3.7.3 Mathematical description

In the Position Vector convention, we define \( R_x = \text{radians}(rx) \), \( R_z = \text{radians}(ry) \) and \( R_z = \text{radians}(rz) \).

In the Coordinate Frame convention, \( R_x = -\text{radians}(rx) \), \( R_z = -\text{radians}(ry) \) and \( R_z = -\text{radians}(rz) \).

\[
\begin{bmatrix}
X^{\text{output}} \\
Y \\
Z
\end{bmatrix} = \begin{bmatrix}
T_x + P_x \\
T_y + P_y \\
T_z + P_z
\end{bmatrix} + (1 + s \times 10^{-6}) \begin{bmatrix}
1 & -R_z & R_y \\
R_z & 1 & -R_x \\
-R_y & R_x & 1
\end{bmatrix} \begin{bmatrix}
X^{\text{input}} - P_x \\
Y^{\text{input}} - P_y \\
Z^{\text{input}} - P_z
\end{bmatrix}
\] (7.11)

7.3.8 Horizontal grid shift

New in version 5.0.0.

Change of horizontal datum by grid shift.

<table>
<thead>
<tr>
<th>Domain</th>
<th>2D, 3D and 4D</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input type</td>
<td>Geodetic coordinates (horizontal), meters (vertical), decimalyear (temporal)</td>
</tr>
<tr>
<td>Output type</td>
<td>Geodetic coordinates (horizontal), meters (vertical), decimalyear (temporal)</td>
</tr>
</tbody>
</table>

The horizontal grid shift is done by offsetting the planar input coordinates by a specific amount determined by the loaded grids. The simplest use case of the horizontal grid shift is applying a single grid:

```bash
+proj=hgridshift +grids=nzgr2kgrid0005.gsb
```

More than one grid can be loaded at the same time, for instance in case the dataset needs to be transformed spans several countries. In this example grids of the continental US, Alaska and Canada is loaded at the same time:

```bash
+proj=hgridshift +grids=@conus,@alaska,@ntv2_0.gsb,@ntv_can.dat
```

The @ in the above example states that the grid is optional, in case the grid is not found in the PROJ search path. The list of grids is prioritized so that grids in the start of the list takes precedence over the grids in the back of the list.

PROJ supports CTable2, NTv1 and NTv2 files for horizontal grid corrections. Details about all three formats can be found in the GDAL documentation and/or driver source code. GDAL reads and writes all three formats. Using GDAL for construction of new grids is recommended.

7.3.8.1 Temporal gridshifting

New in version 5.1.0.

By initializing the horizontal gridshift operation with a central epoch, it can be used as a step function applying the grid offsets only if a coordinate is transformed from an epoch before grids central epoch to an epoch after. This is handy in transformations where it is necessary to handle deformations caused by seismic activity.

The central epoch of the grid is controlled with `+t_epoch` and the final epoch of the coordinate is set with `+t_final`. The observation epoch of the coordinate is part of the coordinate tuple.

Suppose we want to model the deformation of the 2008 earthquake in Iceland in a transformation of data from 2005 to 2009:

```bash
```
Note: The timestamp of the resulting coordinate is still 2005.0. The observation time is always kept unchanged as it would otherwise be impossible to do the inverse transformation.

Temporal gridshifting is especially powerful in transformation pipelines where several gridshifts can be chained together, effectively acting as a series of step functions that can be applied to a coordinate that is propagated through time. In the following example we establish a pipeline that allows transformation of coordinates from any given epoch up until the current date, applying only those gridshifts that have central epochs between the observation epoch and the final epoch:

```
+proj=pipeline +t_final=now
+step +proj=hgridshift +grids=earthquake_1.gsb +t_epoch=2010.421
+step +proj=hgridshift +grids=earthquake_2.gsb +t_epoch=2013.853
+step +proj=hgridshift +grids=earthquake_3.gsb +t_epoch=2017.713
```

Note: The special epoch now is used when specifying the final epoch with +t_final. This results in coordinates being transformed to the current date. Additionally, +t_final is used as a global pipeline parameter, which means that it is applied to all the steps in the pipeline.

In the above transformation, a coordinate with observation epoch 2009.32 would be subject to all three gridshift steps in the pipeline. A coordinate with observation epoch 2014.12 would only be offset by the last step in the pipeline.

### 7.3.8.2 Parameters

#### Required

+grids=<list>

Comma-separated list of grids to load. If a grid is prefixed by an @ the grid is considered optional and PROJ will the not complain if the grid is not available.

Grids are expected to be in CTable2, NTv1 or NTv2 format.

#### Optional

+t_epoch=<time>

Central epoch of the transformation.

New in version 5.1.0.

+t_final=<time>

Final epoch that the coordinate will be propagated to after transformation. The special epoch now can be used instead of writing a specific period in time. When now is used, it is replaced internally with the epoch of the transformation. This means that the resulting coordinate will be slightly different if carried out again at a later date.

New in version 5.1.0.
7.3.9 Vertical grid shift

New in version 5.0.0.

Change Vertical datum change by grid shift

<table>
<thead>
<tr>
<th>Domain</th>
<th>3D and 4D</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input type</td>
<td>Geodetic coordinates (horizontal), meters (vertical), decimalyear (temporal)</td>
</tr>
<tr>
<td>Output type</td>
<td>Geodetic coordinates (horizontal), meters (vertical), decimalyear (temporal)</td>
</tr>
</tbody>
</table>

The vertical grid shift is done by offsetting the vertical input coordinates by a specific amount determined by the loaded grids. The simplest use case of the horizontal grid shift is applying a single grid. Here we change the vertical reference from the ellipsoid to the global geoid model, EGM96:

```
+proj=vgridshift +grids=egm96_15.gtx
```

More than one grid can be loaded at the same time, for instance in the case where a better geoid model than the global is available for a certain area. Here the gridshift is set up so that the local DVR90 geoid model takes precedence over the global model:

```
+proj=vgridshift +grids=@dvr90.gtx,egm96_15.gtx
```

The `@` in the above example states that the grid is optional, in case the grid is not found in the PROJ search path. The list of grids is prioritized so that grids in the start of the list takes precedence over the grids in the back of the list.

PROJ supports the GTX file format for vertical grid corrections. Details about all the format can be found in the GDAL documentation. GDAL both reads and writes the format. Using GDAL for construction of new grids is recommended.

7.3.9.1 Temporal gridshifting

New in version 5.1.0.

By initializing the vertical gridshift operation with a central epoch, it can be used as a step function applying the grid offsets only if a coordinate is transformed from an epoch before grids central epoch to an epoch after. This is handy in transformations where it is necessary to handle deformations caused by seismic activity.

The central epoch of the grid is controlled with `+t_epoch` and the final epoch of the coordinate is set with `+t_final`. The observation epoch of the coordinate is part of the coordinate tuple.

Suppose we want to model the deformation of the 2008 earthquake in Iceland in a transformation of data from 2005 to 2009:

```
echo 63.992 -21.014 10.0 2005.0 | cct +proj=vgridshift +grids=iceland2008.gtx +t_epoch=2008.4071 +t_final=2009.0 63.992 -21.014 10.11 2005.0
```

Note: The timestamp of the resulting coordinate is still 2005.0. The observation time is always kept unchanged as it would otherwise be impossible to do the inverse transformation.

Temporal gridshifting is especially powerful in transformation pipelines where several gridshifts can be chained together, effectively acting as a series of step functions that can be applied to a coordinate that is propagated through time. In the following example we establish a pipeline that allows transformation of coordinates from any given epoch up until the current date, applying only those gridshifts that have central epochs between the observation epoch and the final epoch:
Note: The special epoch \texttt{now} is used when specifying the final epoch with \texttt{+t\_final}. This results in coordinates being transformed to the current date. Additionally, \texttt{+t\_final} is used as a \textit{global pipeline parameter}, which means that it is applied to all the steps in the pipeline.

In the above transformation, a coordinate with observation epoch 2009.32 would be subject to all three gridshift steps in the pipeline. A coordinate with observation epoch 2014.12 would only be offset by the last step in the pipeline.

### 7.3.9.2 Parameters

**Required**

\texttt{+grids=<list>}

Comma-separated list of grids to load. If a grid is prefixed by an \texttt{@} the grid is considered optional and PROJ will not complain if the grid is not available.

Grids are expected to be in GTX format.

**Optional**

\texttt{+t\_epoch=<time>}

Central epoch of the transformation.

New in version 5.1.0.

\texttt{+t\_final=<time>}

Final epoch that the coordinate will be propagated to after transformation. The special epoch \texttt{now} can be used instead of writing a specific period in time. When \texttt{now} is used, it is replaced internally with the epoch of the transformation. This means that the resulting coordinate will be slightly different if carried out again at a later date.

New in version 5.1.0.

\texttt{+multiplier=<value>}

Specify the multiplier to apply to the grid value in the forward transformation direction, such that:

\[
Z_{\text{target}} = Z_{\text{source}} + \text{multiplier} \times \text{gridvalue}
\]  

(7.11)

The multiplier can be used to control whether the gridvalue should be added or subtracted, and if unit conversion must be done (the multiplied gridvalue must be expressed in metre).

Note that the default is \texttt{-1.0} for historical reasons.

New in version 5.2.0.
7.4 The pipeline operator

New in version 5.0.0.

Construct complex operations by daisy-chaining operations in a sequential pipeline.

<table>
<thead>
<tr>
<th>Alias</th>
<th>pipeline</th>
</tr>
</thead>
<tbody>
<tr>
<td>Domain</td>
<td>2D, 3D and 4D</td>
</tr>
<tr>
<td>Input type</td>
<td>Any</td>
</tr>
<tr>
<td>Output type</td>
<td>Any</td>
</tr>
</tbody>
</table>

**Note:** See the section on *Geodetic transformation* for a more thorough introduction to the concept of transformation pipelines in PROJ.

With the pipeline operation it is possible to perform several operations after each other on the same input data. This feature makes it possible to create transformations that are made up of more than one operation, e.g. performing a datum shift and then applying a suitable map projection. Theoretically any transformation between two coordinate reference systems is possible to perform using the pipeline operation, provided that the necessary coordinate operations in each step is available in PROJ.

A pipeline is made up of a number of steps, with each step being a coordinate operation in itself. By connecting these individual steps sequentially we end up with a concatenated coordinate operation. An example of this is a transformation from geodetic coordinates on the GRS80 ellipsoid to a projected system where the east-west and north-east axes has been swapped:

```
+proj=pipeline +ellps=GRS80 +step +proj=merc +step +proj=axisswap +order=2,1
```

Here the first step is applying the *Mercator* projection and the second step is applying the *Axis swap* conversion. Note that the `+ellps=GRS80` is specified before the first occurrence of `+step`. This means that the GRS80 ellipsoid is used in both steps, since any parameter stated before the first occurrence of `+step` is treated as a global parameter and is transferred to each individual steps.

### 7.4.1 Rules for pipelines

1. **Pipelines must consist of at least one step.**
   
   ```
   +proj=pipeline
   ```
   
   Will result in an error.

2. **Pipelines can only be nested if the nested pipeline is defined in an init-file.**

   ```
   +proj=pipeline
   +step +proj=pipeline +step +proj=merc +step +proj=axisswap +order=2,1
   +step +proj=unitconvert +xy_in=m +xy_out=us-ft
   ```

   Results in an error, while

   ```
   +proj=pipeline
   +step +init=predefined_pipelines:projectandswap
   +step +proj=unitconvert +xy_in=m +xy_out=us-ft
   ```
3. Pipelines without a forward path can’t be constructed.

```
+proj=pipeline +step +inv +proj=urm5
```

Will result in an error since Urmaev V does not have an inverse operation defined.

4. Parameters added before the first `+step` are global and will be applied to all steps.

In the following the GRS80 ellipsoid will be applied to all steps.

```
+proj=pipeline +ellps=GRS80
+step +proj=cart
+step +proj=helmert +x=10 +y=3 +z=1
+step +proj=cart +inv
+step +proj=merc
```

5. Units of operations must match between steps.

New in version 5.1.0.

The output units of step $n$ must match the expected input unit of step $n+1$. E.g., you can’t pass an operation that outputs projected coordinates to an operation that expects angular units (degrees). An example of such a unit mismatch is displayed below.

```
+proj=pipeline
+step +proj=merc  # Mercator outputs projected coordinates
+step +proj=robin # The Robinson projection expects angular input
```

### 7.4.2 Parameters

#### 7.4.2.1 Required

`+step`

Separate each step in a pipeline.

#### 7.4.2.2 Optional

`+inv`

Invert a step in a pipeline.
A number of files containing preconfigured transformations and default parameters for certain projections are bundled with the PROJ distribution. Init files contain preconfigured proj-strings for various coordinate reference systems and the defaults file contains default values for parameters of select projections.

In addition to the bundled init-files the PROJ.4 project also distribute a number of packages containing transformation grids and additional init-files not included in the main PROJ package.

8.1 External resources

For a functioning PROJ installation of the proj-datumgrid is needed. If you have installed PROJ from a package system chances are that this will already be done for you. The proj-datumgrid package provides transformation grids that are essential for many of the predefined transformations in PROJ. Which grids are included in the package can be seen on the proj-datumgrid repository as well as descriptions of those grids.

In addition to the default proj-datumgrid package regional packages are also distributed. These include grids and init-files that are valid within the given region. The packages are divided into geographical regions in order to keep the needed disk space by PROJ at a minimum. Some users may have a use for resource files covering several regions in which case they can download more than one.

At the moment three regional resource file packages are distributed:

- Europe
- Oceania
- North America

Click the links to jump to the relevant README files for each package. Details on the content of the packages maintained there.

Links to the resource packages can be found in the download section.

8.2 Transformation grids

Grid files are important for shifting and transforming between datums.

PROJ supports CTable2, NTv1 and NTv2 files for horizontal grid corrections and the GTX file format for vertical corrections. Details about the formats can be found in the GDAL documentation. GDAL reads and writes all formats. Using GDAL for construction of new grids is recommended.

Below is a given a list of grid resources for various countries which are not included in the grid distributions mentioned above.
8.2.1 Free grids

Below is a list of grids distributed under a free and open license.

8.2.1.1 Switzerland

Background in ticket #145

We basically have two shift grids available. An official here:

Swiss CHENyx06 dataset in NTv2 format

And a derived in a temporary location which is probably going to disappear soon.

Main problem seems to be there’s no mention of distributivity of the grid from the official website. It just tells: “you can use freely”. The “contact” link is also broken, but maybe someone could make a phone call to ask for rephrasing that.

8.2.1.2 Hungary

Hungarian grid ETRS89 - HD72/EOV (epsg:23700), both horizontal and elevation grids

8.2.2 Non-Free Grids

Not all grid shift files have licensing that allows them to be freely distributed, but can be obtained by users through free and legal methods.

8.2.2.1 Austria

Austrian Grid for MGI

8.2.2.2 Brazil

Brazilian grids for datums Corrego Alegre 1961, Corrego Alegre 1970-72, SAD69 and SAD69(96)

8.2.2.3 Netherlands

Dutch grid (Registration required before download)

8.2.2.4 Portugal

Portuguese grids for ED50, Lisbon 1890, Lisbon 1937 and Datum 73
8.2.2.5 South Africa

South African grid (Cape to Hartebeesthoek94 or WGS84)

8.2.2.6 Spain

Spanish grids for ED50.

8.2.3 HARN

With the support of i-cubed, Frank Warmerdam has written tools to translate the HPGN grids from NOAA/NGS from .los/.las format into NTv2 format for convenient use with PROJ. This project included implementing a .los/.las reader for GDAL, and an NTv2 reader/writer. Also, a script to do the bulk translation was implemented in https://github.com/OSGeo/gdal/tree/trunk/gdal/swig/python/samples/loslas2ntv2.py. The command to do the translation was:

```
loslas2ntv2.py -auto *hpgn.los
```

As GDAL uses NAD83/WGS84 as a pivot datum, the sense of the HPGN datum shift offsets were negated to map from HPGN to NAD83 instead of the other way. The files can be used with PROJ like this:

```
cs2cs +proj=latlong +datum=NAD83
    +to +proj=latlong +nadgrids=./azhpgn.gsb +ellps=GRS80
```

# input:
-112 34

# output:
111d59'59.996"W 34d0'0.006"N 0.000

This was confirmed against the NGS HPGN calculator.

The grids are available at http://download.osgeo.org/proj/hpgn_ntv2.zip

8.2.4 HTDP

This page documents use of the crs2crs2grid.py script and the HTDP (Horizontal Time Dependent Positioning) grid shift modelling program from NGS/NOAA to produce PROJ compatible grid shift files for fine grade conversions between various NAD83 epochs and WGS84. Traditionally PROJ has treated NAD83 and WGS84 as equivalent and failed to distinguish between different epochs or realizations of those datums. At the scales of much mapping this is adequate but as interest grows in high resolution imagery and other high resolution mapping this is inadequate. Also, as the North American crust drifts over time the displacement between NAD83 and WGS84 grows (more than one foot over the last two decades).
### 8.2.4.1 Getting and building HTDP

The HTDP modelling program is in written FORTRAN. The source and documentation can be found on the HTDP page at [http://www.ngs.noaa.gov/TOOLS/Htdp/Htdp.shtml](http://www.ngs.noaa.gov/TOOLS/Htdp/Htdp.shtml)

On linux systems it will be necessary to install `gfortran` or some FORTRAN compiler. For ubuntu something like the following should work.

```shell
apt-get install gfortran
```

To compile the program do something like the following to produce the binary “htdp” from the source code.

```shell
gfortran htdp.for -o htdp
```

### 8.2.4.2 Getting crs2crs2grid.py

The `crs2crs2grid.py` script can be found at [https://github.com/OSGeo/gdal/tree/trunk/gdal/swig/python/samples/crs2crs2grid.py](https://github.com/OSGeo/gdal/tree/trunk/gdal/swig/python/samples/crs2crs2grid.py)

It depends on having the GDAL Python bindings operational. If they are not

```
Traceback (most recent call last):
  File "./crs2crs2grid.py", line 37, in <module>
    from osgeo import gdal, gdal_array, osr
ImportError: No module named osgeo
```

### 8.2.4.3 Usage

```
crs2crs2grid.py <src_crs_id> <src_crs_date> <dst_crs_id> <dst_crs_year> 
[-griddef <ul_lon> <ul_lat> <ll_lon> <ll_lat> <lon_count> <lat_count>] 
[-htdp <path_to_exe>] [-wkdir <dirpath>] [-kwf] 
-o <output_grid_name>
```

- `griddef`: by default the following values for roughly the continental USA
  at a six minute step size are used:
  -127 50 -66 25 251 611
- `kWF`: keep working files in the working directory for review.

```
```

The goal of `crs2crs2grid.py` is to produce a grid shift file for a designated region. The region is defined using the `-griddef` switch. When missing a continental US region is used. The script creates a set of sample points for the grid definition, runs the “htdp” program against it and then parses the resulting points and computes a point by point shift to encode into the final grid shift file. By default it is assumed the `htdp` program will be in the executable path. If not, please provide the path to the executable using the `-htdp` switch.

The `htdp` program supports transformations between many CRSes and for each (or most?) of them you need to provide a date at which the CRS is fixed. The full set of CRS Ids available in the HTDP program are:

```
1...NAD_83(2011) (North America tectonic plate fixed)
29...NAD_83(CORS96) (NAD_83(2011) will be used)
30...NAD_83(2007) (NAD_83(2011) will be used)
2...NAD_83(PA11) (Pacific tectonic plate fixed)
```
The typical use case is mapping from NAD83 on a particular date to WGS84 on some date. In this case the source CRS Id “29” (NAD_83(CORS96)) and the destination CRS Id is “8 (WGS_84(G1150)). It is also necessary to select the source and destination date (epoch). For example:

```
```

The output is a CTable2 format grid shift file suitable for use with PROJ (4.8.0 or newer). It might be utilized something like:

```
    cs2cs +proj=latlong +ellps=GRS80 +nadgrids=./nad83_2002.ct2 +to +proj=latlong +datum=WGS84
```

### 8.2.4.4 See Also


## 8.3 Init files

Init files are used for preconfiguring proj-strings for often used transformations, such as those found in the EPSG database. Most init files contain transformations from a given coordinate reference system to WGS84. This makes it easy to transformations between any two coordinate reference systems with cs2cs. Init files can however contain any proj-string and don’t necessarily have to follow the cs2cs paradigm where WGS84 is used as a pivot datum. The ITRF init file is a good example of that.

A number of init files come pre-bundled with PROJ but it is also possible to add your own custom init files. PROJ looks for the init files in the directory listed in the `PROJ_LIB` environment variable.

The format of init files made up of a identifier in angled brackets and a proj-string:

```
<3819> +proj=longlat +ellps=bessel +towgs84=595.48,121.69,515.35,4.115,-2.9383,0.853,-3.408 +no_defs <>
```

The above example is the first entry from the `epsg` init file. So, this is the coordinate reference system with ID 3819 in the EPSG database. Comments can be inserted by prefixing them with a “#”. With version 4.10.0 a new special
metadata entry is now accepted in init files. It can be parsed with a function from the public API. The metadata entry in the epsg init file looks like this at the time of writing:

```xml
<metadata> +version=9.0.0 +origin=EPSG +lastupdate=2017-01-10
```

Pre-configured proj-strings from init files are used in the following way:

```bash
$ cs2cs -v +proj=latlong +to +init=epsg:3819
# ---- From Coordinate System ----
# Lat/long (Geodetic alias)
# +proj=latlong +ellps=WGS84
# ---- To Coordinate System ----
# Lat/long (Geodetic alias)
# +init=epsg:3819 +proj=longlat +ellps=bessel
# +towgs84=595.48,121.69,515.35,4.115,-2.9383,0.853,-3.408 +no_defs
```

It is possible to override parameters when using `+init`. Just add the parameter to the proj-string alongside the `+init` parameter. For instance by overriding the ellipsoid as in the following example

```bash
+init=epsg:25832 +ellps=intl
```

where the Hayford ellipsoid is used instead of the predefined GRS80 ellipsoid. It is also possible to add additional parameters not specified in the init file, for instance by adding an observation epoch when transforming from ITRF2000 to ITRF2005:

```bash
+init=ITRF2000:ITRF2005 +t_obs=2010.5
```

which then expands to

```bash
+proj=helmert +x=-0.0001 +y=0.0008 +z=0.0058 +s=-0.0004
+dx=0.0002 +dy=-0.0001 +dz=0.0018 +ds=-0.000008
+t_epoch=2000.0 +convention=position_vector
+t_obs=2010.5
```

Below is a list of the init files that are packaged with PROJ.

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>esri</td>
<td>Auto-generated mapping from Esri projection index. Not maintained any more</td>
</tr>
<tr>
<td>epsg</td>
<td>EPSG database</td>
</tr>
<tr>
<td>GL27</td>
<td>Great Lakes Grids</td>
</tr>
<tr>
<td>IGNF</td>
<td>French coordinate systems supplied by the IGNF</td>
</tr>
<tr>
<td>ITRF2000</td>
<td>Full set of transformation parameters between ITRF2000 and other ITRF’s</td>
</tr>
<tr>
<td>ITRF2008</td>
<td>Full set of transformation parameters between ITRF2008 and other ITRF’s</td>
</tr>
<tr>
<td>ITRF2014</td>
<td>Full set of transformation parameters between ITRF2014 and other ITRF’s</td>
</tr>
<tr>
<td>nad27</td>
<td>State plane coordinate systems, North American Datum 1927</td>
</tr>
<tr>
<td>nad83</td>
<td>State plane coordinate systems, North American Datum 1983</td>
</tr>
</tbody>
</table>
8.4 The defaults file

Before PROJ 6.0, a proj_def.dat file could be used to supply default parameters to PROJ. It has been removed due to the confusion and errors it caused.
CHAPTER NINE

GEODESIC CALCULATIONS

9.1 Introduction

Consider an ellipsoid of revolution with equatorial radius \(a\), polar semi-axis \(b\), and flattening \(f = (a - b)/a\). Points on the surface of the ellipsoid are characterized by their latitude \(\phi\) and longitude \(\lambda\). (Note that latitude here means the geographical latitude, the angle between the normal to the ellipsoid and the equatorial plane).

The shortest path between two points on the ellipsoid at \((\phi_1, \lambda_1)\) and \((\phi_2, \lambda_2)\) is called the geodesic. Its length is \(s_{12}\) and the geodesic from point 1 to point 2 has forward azimuths \(\alpha_1\) and \(\alpha_2\) at the two end points. In this figure, we have \(\lambda_{12} = \lambda_2 - \lambda_1\).

A geodesic can be extended indefinitely by requiring that any sufficiently small segment is a shortest path; geodesics are also the straightest curves on the surface.

9.2 Solution of geodesic problems

Traditionally two geodesic problems are considered:

- the direct problem — given \(\phi_1, \lambda_1, \alpha_1, s_{12}\), determine \(\phi_2, \lambda_2, \alpha_2\).
- the inverse problem — given \(\phi_1, \lambda_1, \phi_2, \lambda_2\), determine \(s_{12}, \alpha_1, \alpha_2\).

PROJ incorporates C library for Geodesics from GeographicLib. This library provides routines to solve the direct and inverse geodesic problems. Full double precision accuracy is maintained provided that \(|f| < \frac{1}{50}\). Refer to the application programming interface for full documentation. A brief summary of the routines is given in geodesic(3).

The interface to the geodesic routines differ in two respects from the rest of PROJ:

- angles (latitudes, longitudes, and azimuths) are in degrees (instead of in radians);
- the shape of ellipsoid is specified by the flattening \(f\); this can be negative to denote a prolate ellipsoid; setting \(f = 0\) corresponds to a sphere, in which case the geodesic becomes a great circle.

PROJ also includes a command line tool, `geod(1)`, for performing simple geodesic calculations.
9.3 Additional properties

The routines also calculate several other quantities of interest

- \( S_{12} \) is the area between the geodesic from point 1 to point 2 and the equator; i.e., it is the area, measured counter-clockwise, of the quadrilateral with corners \((\phi_1, \lambda_1), (0, \lambda_1), (0, \lambda_2), \) and \((\phi_2, \lambda_2)\). It is given in meters\(^2\).

- \( m_{12} \), the reduced length of the geodesic is defined such that if the initial azimuth is perturbed by \( d\alpha_1 \) (radians) then the second point is displaced by \( m_{12} d\alpha_1 \) in the direction perpendicular to the geodesic. \( m_{12} \) is given in meters. On a curved surface the reduced length obeys a symmetry relation, \( m_{12} + m_{21} = 0 \). On a flat surface, we have \( m_{12} = s_{12} \).

- \( M_{12} \) and \( M_{21} \) are geodesic scales. If two geodesics are parallel at point 1 and separated by a small distance \( dt \), then they are separated by a distance \( M_{12} dt \) at point 2. \( M_{21} \) is defined similarly (with the geodesics being parallel to one another at point 2). \( M_{12} \) and \( M_{21} \) are dimensionless quantities. On a flat surface, we have \( M_{12} = M_{21} = 1 \).

- \( \sigma_{12} \) is the arc length on the auxiliary sphere. This is a construct for converting the problem to one in spherical trigonometry. The spherical arc length from one equator crossing to the next is always \( 180^\circ \).

If points 1, 2, and 3 lie on a single geodesic, then the following addition rules hold:

- \( s_{13} = s_{12} + s_{23} \),
- \( \sigma_{13} = \sigma_{12} + \sigma_{23} \),
- \( S_{13} = S_{12} + S_{23} \),
- \( m_{13} = m_{12} M_{23} + m_{23} M_{21} \),
- \( M_{13} = M_{12} M_{23} - (1 - M_{12} M_{21}) m_{23}/m_{12} \),
- \( M_{31} = M_{32} M_{21} - (1 - M_{23} M_{32}) m_{12}/m_{23} \).

9.4 Multiple shortest geodesics

The shortest distance found by solving the inverse problem is (obviously) uniquely defined. However, in a few special cases there are multiple azimuths which yield the same shortest distance. Here is a catalog of those cases:

- \( \phi_1 = -\phi_2 \) (with neither point at a pole). If \( \alpha_1 = \alpha_2 \), the geodesic is unique. Otherwise there are two geodesics and the second one is obtained by setting \([\alpha_1, \alpha_2] \leftarrow [\alpha_2, \alpha_1], [M_{12}, M_{21}] \leftarrow [M_{21}, M_{12}], S_{12} \leftarrow -S_{12} \). (This occurs when the longitude difference is near \( \pm 180^\circ \) for oblate ellipsoids.)

- \( \lambda_2 = \lambda_1 \pm 180^\circ \) (with neither point at a pole). If \( \alpha_1 = 0^\circ \) or \( \pm 180^\circ \), the geodesic is unique. Otherwise there are two geodesics and the second one is obtained by setting \([\alpha_1, \alpha_2] \leftarrow [-\alpha_1, -\alpha_2], S_{12} \leftarrow -S_{12} \). (This occurs when \( \phi_2 \) is near \( -\phi_1 \) for prolate ellipsoids.)

- Points 1 and 2 at opposite poles. There are infinitely many geodesics which can be generated by setting \([\alpha_1, \alpha_2] \leftarrow [\alpha_1, \alpha_2] + [\delta, -\delta], \) for arbitrary \( \delta \). (For spheres, this prescription applies when points 1 and 2 are antipodal.)

- \( s_{12} = 0 \) (coincident points). There are infinitely many geodesics which can be generated by setting \([\alpha_1, \alpha_2] \leftarrow [\alpha_1, \alpha_2] + [\delta, \delta], \) for arbitrary \( \delta \).
9.5 Background

The algorithms implemented by this package are given in [Karney2013] (addenda) and are based on [Besse1825] and [Helmert1880]; the algorithm for areas is based on [Danielsen1989]. These improve on the work of [Vincenty1975] in the following respects:

- The results are accurate to round-off for terrestrial ellipsoids (the error in the distance is less than 15 nanometers, compared to 0.1 mm for Vincenty).
- The solution of the inverse problem is always found. (Vincenty’s method fails to converge for nearly antipodal points.)
- The routines calculate differential and integral properties of a geodesic. This allows, for example, the area of a geodesic polygon to be computed.

Additional background material is provided in GeographicLib’s geodesic bibliography, Wikipedia’s article “Geodesics on an ellipsoid”, and [Karney2011] (errata).
These pages are primarily focused towards developers either contributing to the PROJ project or using the library in their own software.

## 10.1 Quick start

This is a short introduction to the PROJ API. In the following section we create a simple program that transforms a geodetic coordinate to UTM and back again. The program is explained a few lines at a time. The complete program can be seen at the end of the section.

See the following sections for more in-depth descriptions of different parts of the PROJ API or consult the API reference for specifics.

Before the PROJ API can be used it is necessary to include the `proj.h` header file. Here `stdio.h` is also included so we can print some text to the screen:

```c
#include <stdio.h>
#include <proj.h>
```

Let’s declare a few variables that’ll be used later in the program. Each variable will be discussed below. See the reference for more info on data types.

```c
PJ_CONTEXT *C;
PJ *P;
PJ* P_for_GIS;
PJ_COORD a, b;
```

For use in multi-threaded programs the `PJ_CONTEXT` threading-context is used. In this particular example it is not needed, but for the sake of completeness it created here. The section on threads discusses this in detail.

```c
C = proj_context_create();
```

Next we create the `PJ` transformation object `P` with the function `proj_create_crs_to_crs()`. `proj_create_crs_to_crs()` takes the threading context `C` created above, a string that describes the source coordinate reference system (CRS), a string that describes the target CRS and an optional description of the area of use. The strings for the source or target CRS may be PROJ strings (`+proj=longlat +datum=WGS84`), CRS identified by their code (EPSG:4326 or urn:ogc:def:crs:EPSG::4326) or by a well-known text (WKT) string (`GEOGCRS|"WGS 84", DATUM("World Geodetic System 1984", ELLIPSOID("WGS 84",6378137,298.257223563,` (continues on next page)
LENGTHUNIT["metre",1]],
PRIMEM["Greenwich",0,
ANGLEUNIT["degree",0.0174532925199433]],
CS[ellipsoidal,2],
AXIS["geodetic latitude (Lat)",north,
ORDER[1],
ANGLEUNIT["degree",0.0174532925199433]],
AXIS["geodetic longitude (Lon)",east,
ORDER[2],
ANGLEUNIT["degree",0.0174532925199433]],
USAGE[
  SCOPE["unknown"],
  AREA["World"],
  BBOX[-90,-180,90,180],
  ID["EPSG",4326]]

The use of PROJ strings to describe a CRS is considered as legacy (one of the main weakness of PROJ strings is their inability to describe a geodetic datum, other than the few ones hardcoded in the +datum parameter). Here we transform from geographic coordinates to UTM zone 32N. It is recommended to create one threading-context per thread used by the program. This ensures that all PJ objects created in the same context will be sharing resources such as error-numbers and loaded grids. In case the creation of the PJ object fails an error message is displayed and the program returns. See Error handling for further details.

```
P = proj_create_crs_to_crs (C,
    "EPSG:4326",
    "+proj=utm +zone=32 +datum=WGS84", /* or EPSG:32632 */
    NULL);
if (0==P) {
    fprintf(stderr, "Oops\n");
    return 1;
}
```

`proj_create_crs_to_crs()` creates a transformation object, which accepts coordinates expressed in the units and axis order of the definition of the source CRS, and return transformed coordinates in the units and axis order of the definition of the target CRS. For almost most geographic CRS, the units will be in most cases degrees (in rare cases, such as EPSG:4807 / NTF (Paris), this can be grads). For geographic CRS defined by the EPSG authority, the order of coordinates is latitude first, longitude second. When using a PROJ string, on contrary the order will be longitude first, latitude second. For projected CRS, the units may vary (metre, us-foot, etc..). For projected CRS defined by the EPSG authority, and with EAST / NORTH directions, the order might be easting first, northing second, or the reverse. When using a PROJ string, the order will be easting first, northing second, except if the +axis parameter modifies it.

If for the needs of your software, you want a uniform axis order (and thus do not care about axis order mandated by the authority defining the CRS), the `proj_normalize_for_visualization()` function can be used to modify the PJ* object returned by `proj_create_crs_to_crs()` so that it accepts as input and returns as output coordinates using the traditional GIS order, that is longitude, latitude (followed by elevation, time) for geographic CRS and easting, northing for most projected CRS.

```
P_for_GIS = proj_normalize_for_visualization(C, P);
if ( 0 == P_for_GIS ) {
    fprintf(stderr, "Oops\n");
    return 1;
}
proj_destroy(P);
P = P_for_GIS;
```
PROJ uses its own data structures for handling coordinates. Here we use a `PJ_COORD` which is easily assigned with the function `proj_coord()`. When using `+proj=longlat`, the order of coordinates is longitude, latitude, and values are expressed in degrees. If you used instead a EPSG geographic CRS, like EPSG:4326 (WGS84), it would be latitude, longitude.

```c
a = proj_coord(12, 55, 0, 0);
```

The coordinate defined above is transformed with `proj_trans()`. For this a `PJ` object, a transformation direction (either forward or inverse) and the coordinate is needed. The transformed coordinate is returned in `b`. Here the forward (`PJ_FWD`) transformation from geographic to UTM is made.

```c
b = proj_trans(P, PJ_FWD, a);
printf("easting: %.3f, northing: %.3f\n", b.enu.e, b.enu.n);
```

The inverse transformation (UTM to geographic) is done similar to above, this time using `PJ_INV` as the direction.

```c
b = proj_trans(P, PJ_INV, b);
printf("longitude: %g, latitude: %g\n", b.lp.lam, b.lp.phi);
```

Before ending the program the allocated memory needs to be released again:

```c
proj_destroy(P);
proj_context_destroy(C); /* may be omitted in the single threaded case */
```

A complete compilable version of the above can be seen here:

```c
#include <stdio.h>
#include <proj.h>

int main(void) {
  PJ_CONTEXT *C;
  PJ *P;
  PJ* P_for_GIS;
  PJ_COORD a, b;

  /* or you may set C=PJ_DEFAULT_CTX if you are sure you will */
  /* use PJ objects from only one thread */
  C = proj_context_create();

  P = proj_create_crs_to_crs(C, 
    "EPSG:4326",
    "+proj=utm +zone=32 +datum=WGS84", /* or EPSG:32632 */
    NULL);

  if (0==P) {
    fprintf(stderr, "Oops\n");
    return 1;
  }

  /* This will ensure that the order of coordinates for the input CRS */
  /* will be longitude, latitude, whereas EPSG:4326 mandates latitude, */
  /* longitude */
  P_for_GIS = proj_normalize_for_visualization(C, P);
  if( 0 == P_for_GIS ) {
    fprintf(stderr, "Oops\n");
    return 1;
  }
}
```

(continues on next page)
10.2 Transformations

10.3 Error handling

10.4 Threads

This page is about efforts to make PROJ thread safe.

10.4.1 Key Thread Safety Issues

- the global pj_errno variable is shared between threads and makes it essentially impossible to handle errors safely. Being addressed with the introduction of the projCtx execution context.

- the datum shift using grid files uses globally shared lists of loaded grid information. Access to this has been made safe in 4.7.0 with the introduction of a PROJ mutex used to protect access to these memory structures (see pj_mutex.c).

10.4.2 projCtx

Primarily in order to avoid having pj_errno as a global variable, a “thread context” structure has been introduced into a variation of the PROJ API for the 4.8.0 release. The pj_init() and pj_init_plus() functions now have context variations called pj_init_ctx() and pj_init_plus_ctx() which take a projections context.

The projections context can be created with pj_ctx_alloc(), and there is a global default context used when one is not provided by the application. There is a pj_ctx_set of functions to create, manipulate, query, and destroy contexts. The contexts are also used now to handle setting debugging mode, and to hold an error reporting function for textual error and debug messages. The API looks like:
Multithreaded applications are now expected to create a projCtx per thread using pj_ctx_alloc(). The context’s error handlers, and app data may be modified if desired, but at the very least each context has an internal error value accessed with pj_ctx_get_errno() as opposed to looking at pj_errno.

Note that pj_errno continues to exist, and it is set by pj_ctx_set_errno() (as well as setting the context specific error number), but pj_errno still suffers from the global shared problem between threads and should not be used by multithreaded applications.

Note that pj_init_ctx(), and pj_init_plus_ctx() will assign the projCtx to the created projPJ object. Functions like pj_transform(), pj_fwd() and pj_inv() will use the context of the projPJ for error reporting.

10.4.3 src/multistresstest.c

A small multi-threaded test program has been written (src/multistresstest.c) for testing multithreaded use of PROJ. It performs a series of reprojections to setup a table expected results, and then it does them many times in several threads to confirm that the results are consistent. At this time this program is not part of the builds but it can be built on linux like:

```bash
gcc -g multistresstest.c .libs/libproj.so -lpthread -o multistresstest ./multistresstest
```

10.5 Reference

10.5.1 Data types

This section describes the numerous data types in use in PROJ.4. As a rule of thumb PROJ.4 data types are prefixed with PJ_ or in one particular case, is simply called PJ. A few notable exceptions can be traced back to the very early days of PROJ.4 when the PJ_ prefix was not consistently used.
10.5.1.1 Transformation objects

PJ
Object containing everything related to a given projection or transformation. As a user of the PROJ.4 library you are only exposed to pointers to this object and the contents is hidden behind the public API. PJ objects are created with `proj_create()` and destroyed with `proj_destroy()`.

PJ_DIRECTION
Enumeration that is used to convey in which direction a given transformation should be performed. Used in transformation function call as described in the section on transformation functions.
Forward transformations are defined with the `typedef enum
```c
typedef enum proj_direction {
    PJ_FWD = 1,  /* Forward */
    PJ_IDENT = 0, /* Do nothing */
    PJ_INV = -1   /* Inverse */
} PJ_DIRECTION;
```

PJ_FWD
Perform transformation in the forward direction.

PJ_IDENT
Identity. Do nothing.

PJ_INV
Perform transformation in the inverse direction.

PJ_CONTEXT
Context objects enable safe multi-threaded usage of PROJ.4. Each PJ object is connected to a context (if not specified, the default context is used). All operations within a context should be performed in the same thread. PJ_CONTEXT objects are created with `proj_context_create()` and destroyed with `proj_context_destroy()`.

PJ_AREA
New in version 6.0.0.
Opaque object describing an area in which a transformation is performed.
It is used with `proj_create_crs_to_crs()` to select the best transformation between the two input coordinate reference systems.

10.5.1.2 2 dimensional coordinates

Various 2-dimensional coordinate data types.

PJ_LP
Geodetic coordinate, latitude and longitude. Usually in radians.
```c
typedef struct { double lam, phi; } PJ_LP;
```

double PJ_LP.lam
Longitude. Lambda.

double PJ_LP.phi
Latitude. Phi.

PJ_XY
2-dimensional cartesian coordinate.
typedef struct { double x, y; } PJ_XY;

double PJ_XY.x
Easting.

double PJ_XY.y
Northing.

PJ_UV
2-dimensional generic coordinate. Usually used when contents can be either a PJ_XY or PJ_LP.

typedef struct {double u, v; } PJ_UV;

double PJ_UV.u
Longitude or easting, depending on use.

double PJ_UV.v
Latitude or northing, depending on use.

10.5.1.3 3 dimensional coordinates

The following data types are the 3-dimensional equivalents to the data types above.

PJ_LPZ
3-dimensional version of PJ_LP. Holds longitude, latitude and a vertical component.

typedef struct { double lam, phi, z; } PJ_LPZ;

double PJ_LPZ.lam
Longitude. Lambda.

double PJ_LPZ.phi
Latitude. Phi.

double PJ_LPZ.z
Vertical component.

PJ_XYZ
Cartesian coordinate in 3 dimensions. Extension of PJ_XY.

typedef struct { double x, y, z; } PJ_XYZ;

double PJ_XYZ.x
Easting or the X component of a 3D cartesian system.

double PJ_XYZ.y
Northing or the Y component of a 3D cartesian system.

double PJ_XYZ.z
Vertical component or the Z component of a 3D cartesian system.

PJ_UVW
3-dimensional extension of PJ_UV.

typedef struct {double u, v, w; } PJ_UVW;

double PJ_UVW.u
Longitude or easting, depending on use.
10.5.1.4 Spatiotemporal coordinate types

The following data types are extensions of the triplets above into the time domain.

**PJ_LPZT**
Spatiotemporal version of `PJ_LPZ`.

```c
typedef struct {
    double lam;
    double phi;
    double z;
    double t;
} PJ_LPZT;
```

double `PJ_LPZT.lam`
Longitude.

double `PJ_LPZT.phi`
Latitude

double `PJ_LPZT.z`
Vertical component.

double `PJ_LPZT.t`
Time component.

**PJ_XYZT**
Generic spatiotemporal coordinate. Useful for e.g. cartesian coordinates with an attached time-stamp.

```c
typedef struct {
    double x;
    double y;
    double z;
    double t;
} PJ_XYZT;
```

double `PJ_XYZT.x`
Easting or the X component of a 3D cartesian system.

double `PJ_XYZT.y`
Northing or the Y component of a 3D cartesian system.

double `PJ_XYZT.z`
Vertical or the Z component of a 3D cartesian system.

double `PJ_XYZT.t`
Time component.

**PJ_UVWT**
Spatiotemporal version of `PJ_UVW`.

```c
typedef struct { double u, v, w, t; } PJ_UVWT;
```
double PJ_UVWT.e
   First horizontal component.

double PJ_UVWT.n
   Second horizontal component.

double PJ_UVWT.w
   Vertical component.

double PJ_UVWT.t
   Temporal component.

10.5.1.5 Ancillary types for geodetic computations

PJ_OPK
   Rotations, for instance three euler angles.

   \[
   \text{typedef struct} \left\{ \begin{array}{c}
   \text{double} \ o, \ p, \ k; \\
   \end{array} \right\} \text{PJ_OPK};
   \]

   double PJ_OPK.o
   First rotation angle, omega.

   double PJ_OPK.p
   Second rotation angle, phi.

   double PJ_OPK.k
   Third rotation angle, kappa.

10.5.1.6 Complex coordinate types

PJCOORD
   General purpose coordinate union type, applicable in two, three and four dimensions. This is the default coordinate datatype used in PROJ.

   \[
   \text{typedef union} \left\{ \begin{array}{c}
   \text{double} \ v[4]; \\
   \text{PJ}_X \text{YZT} \ \text{xyzt}; \\
   \text{PJ}_U \text{VWT} \ \text{uvw}; \\
   \text{PJ}_L \text{PZT} \ \text{lpzt}; \\
   \text{PJ}_X \text{YZ} \ \text{xyz}; \\
   \text{PJ}_U \text{VW} \ \text{uvw}; \\
   \text{PJ}_L \text{PZ} \ \text{lpz}; \\
   \text{PJ}_X \text{Y} \ \text{xy}; \\
   \text{PJ}_U \text{V} \ \text{uv}; \\
   \text{PJ}_L \text{P} \ \text{lp}; \\
   \end{array} \right\} \text{PJCOORD};
   \]

   double v[4]
   Generic four-dimensional vector.

   PJ_XYZT PJ_COORD.xyzt
   Spatiotemporal cartesian coordinate.

   PJ_UVWT PJ_COORD.uvwt
   Spatiotemporal generic coordinate.

   PJ_LPZT PJ_COORD.lpz
   Longitude, latitude, vertical and time components.
PJ_XYZ PJ_COORD.xyz
3-dimensional cartesian coordinate.

PJ_UVW PJ_COORD.uvw
3-dimensional generic coordinate.

PJ_LPZ PJ_COORD.lpz
Longitude, latitude and vertical component.

PJ_XY PJ_COORD.xy
2-dimensional cartesian coordinate.

PJ_UV PJ_COORD.uv
2-dimensional generic coordinate.

PJ_LP PJ_COORD.lp
Longitude and latitude.

10.5.1.7 Projection derivatives

PJ_FACTORS
Various cartographic properties, such as scale factors, angular distortion and meridian convergence. Calculated with proj_factors().

typedef struct {
    double meridional_scale;
    double parallel_scale;
    double areal_scale;
    double angular_distortion;
    double meridian_parallel_angle;
    double meridian_convergence;
    double tissot_semimajor;
    double tissot_semiminor;
    double dx_dlam;
    double dx_dphi;
    double dy_dlam;
    double dy_dphi;
} PJ_FACTORS;

double PJ_FACTORS.meridional_scale
Meridional scale at coordinate (\(\lambda, \phi\)).

double PJ_FACTORS.parallel_scale
Parallel scale at coordinate (\(\lambda, \phi\)).

double PJ_FACTORS.areal_scale
Areal scale factor at coordinate (\(\lambda, \phi\)).

double PJ_FACTORS.angular_distortion
Angular distortion at coordinate (\(\lambda, \phi\)).

double PJ_FACTORS.meridian_parallel_angle
Meridian/parallel angle, \(\theta'\), at coordinate (\(\lambda, \phi\)).

double PJ_FACTORS.meridian_convergence
Meridian convergence at coordinate (\(\lambda, \phi\)). Sometimes also described as grid declination.
double PJ_FACTORS.tissot_semimajor
   Maximum scale factor.

double PJ_FACTORS.tissot_semiminor
   Minimum scale factor.

double PJ_FACTORS.dx_dlam
   Partial derivative $\frac{\partial x}{\partial \lambda}$ of coordinate $(\lambda, \phi)$.

double PJ_FACTORS.dy_dlam
   Partial derivative $\frac{\partial y}{\partial \lambda}$ of coordinate $(\lambda, \phi)$.

double PJ_FACTORS.dx_dphi
   Partial derivative $\frac{\partial x}{\partial \phi}$ of coordinate $(\lambda, \phi)$.

double PJ_FACTORS.dy_dphi
   Partial derivative $\frac{\partial y}{\partial \phi}$ of coordinate $(\lambda, \phi)$.

10.5.1.8 List structures

**PJ_OPERATIONS**
Description a PROJ.4 operation

```c
struct PJ_OPERATIONS {
    const char *id; /* operation keyword */
    PJ *(*proj)(PJ *); /* operation entry point */
    char * const *descr; /* description text */
};
```

- **const char *id**
  Operation keyword.

- **PJ *(*op)(PJ *)**
  Operation entry point.

- **char * const *descr**
  Description of operation.

**PJ_ELLPS**
Description of ellipsoids defined in PROJ.4

```c
struct PJ_ELLPS {
    const char *id;
    const char *major;
    const char *ell;
    const char *name;
};
```

- **const char *id**
  Keyword name of the ellipsoid.

- **const char *major**
  Semi-major axis of the ellipsoid, or radius in case of a sphere.

- **const char *ell**
  Elliptical parameter, e.g. rf=298.257 or b=6356772.2.

- **const char *name**
  Name of the ellipsoid.
 PJ_UNITS
Distance units defined in PROJ.

```c
struct PJ_UNITS {
    const char *id; /* units keyword */
    const char *to_meter; /* multiply by value to get meters */
    const char *name; /* comments */
    double factor; /* to_meter factor in actual numbers */
};
```

- **id**
  Keyword for the unit.

- **to_meter**
  Text representation of the factor that converts a given unit to meters.

- **name**
  Name of the unit.

- **factor**
  Conversion factor that converts the unit to meters.

 PJ_PRIME_MERIDIANS
Prime meridians defined in PROJ.

```c
struct PJ_PRIME_MERIDIANS {
    const char *id;
    const char *defn;
};
```

- **id**
  Keyword for the prime meridian.

- **defn**
  Offset from Greenwich in DMS format.

10.5.1.9 Info structures

 PJ_INFO
Struct holding information about the current instance of PROJ. Struct is populated by `proj_info()`.

```c
typedef struct {
    int major;
    int minor;
    int patch;
    const char *release;
    const char *version;
    const char *searchpath;
} PJ_INFO;
```

- **PJ_INFO.release**
  Release info. Version number and release date, e.g. “Rel. 4.9.3, 15 August 2016”.

- **PJ_INFO.version**
  Text representation of the full version number, e.g. “4.9.3”.

- **PJ_INFO.major**
  Major version number.
int PJ_INFO.minor
Minor version number.

int PJ_INFO.patch
Patch level of release.

const char PJ_INFO.searchpath
Search path for PROJ. List of directories separated by semicolons (Windows) or colons (non-Windows), e.g. “C:\Users\doctorwho;C:\OSGeo4W64\share\proj”. Grids and init files are looked for in directories in the search path.

PJ_PROJ_INFO
Struct holding information about a PJ object. Populated by proj_pj_info(). The PJ_PROJ_INFO object provides a view into the internals of a PJ, so once the PJ is destroyed or otherwise becomes invalid, so does the PJ_PROJ_INFO

typedef struct {
    const char *id;
    const char *description;
    const char *definition;
    int has_inverse;
    double accuracy;
} PJ_PROJ_INFO;

const char *PJ_PROJ_INFO.id
Short ID of the operation the PJ object is based on, that is, what comes after the +proj= in a proj-string, e.g. “merc”.

const char *PJ_PROJ_INFO.description
Long describes of the operation the PJ object is based on, e.g. “Mercator Cyl, Sph&Ell lat_ts=”.

const char *PJ_PROJ_INFO.definition
The proj-string that was used to create the PJ object with, e.g. “+proj=merc +lat_0=24 +lon_0=53 +ellps=WGS84”.

int PJ_PROJ_INFO.has_inverse
1 if an inverse mapping of the defined operation exists, otherwise 0.

double PJ_PROJ_INFO.accuracy
Expected accuracy of the transformation. -1 if unknown.

PJ_GRID_INFO
Struct holding information about a specific grid in the search path of PROJ. Populated with the function proj_grid_info().

typedef struct {
    char gridname[32];
    char filename[260];
    char format[8];
    LP lowerleft;
    LP upperright;
    int n_lon, n_lat;
    double cs_lon, cs_lat;
} PJ_GRID_INFO;

char PJ_GRID_INFO.gridname[32]
Name of grid, e.g. “BETA2007.gsb”.

char PJ_GRID_INFO.filename[260]
Full path of grid file, e.g. “C:\OSGeo4W64\share\proj\BETA2007.gsb”
char PJ_GRID_INFO.format[8]
   File format of grid file, e.g. “ntv2”

LP PJ_GRID_INFO.lowerleft
   Geodetic coordinate of lower left corner of grid.

LP PJ_GRID_INFO.upperright
   Geodetic coordinate of upper right corner of grid.

int PJ_GRID_INFO.n_lon
   Number of grid cells in the longitudinal direction.

int PJ_GRID_INFO.n_lat
   Number of grid cells in the latitudinal direction.

double PJ_GRID_INFO.cs_lon
   Cell size in the longitudinal direction. In radians.

double PJ_GRID_INFO.cs_lat
   Cell size in the latitudinal direction. In radians.

PJ_INIT_INFO
   Struct holding information about a specific init file in the search path of PROJ. Populated with the function proj_init_info().

typedef struct {
   char name[32];
   char filename[260];
   char version[32];
   char origin[32];
   char lastupdate[16];
} PJ_INIT_INFO;

c char PJ_INIT_INFO.name[32]
   Name of init file, e.g. “epsg”.

c char PJ_INIT_INFO.filename[260]
   Full path of init file, e.g. “C:\OSGeo4W64\share\proj\epsg”

c char PJ_INIT_INFO.version[32]
   Version number of init-file, e.g. “9.0.0”

c char PJ_INIT_INFO.origin[32]
   Originating entity of the init file, e.g. “EPSG”

c char PJ_INIT_INFO.lastupdate
   Date of last update of the init-file.

10.5.1.10 Logging

PJ_LOG_LEVEL
   Enum of logging levels in PROJ. Used to set the logging level in PROJ. Usually using proj_log_level().

PJ_LOG_NONE
   Don’t log anything.

PJ_LOG_ERROR
   Log only errors.

PJ_LOG_DEBUG
   Log errors and additional debug information.
PJ_LOG_TRACE
Highest logging level. Log everything including very detailed debug information.

PJ_LOG_TELL
Special logging level that when used in proj_log_level() will return the current logging level set in PROJ.

New in version 5.1.0.

PJ_LOG_FUNC
Function prototype for the logging function used by PROJ. Defined as

define void (*PJ_LOG_FUNCTION)(void *, int, const char *);

where the void pointer references a data structure used by the calling application, the int is used to set the logging level and the const char pointer is the string that will be logged by the function.

New in version 5.1.0.

10.5.1.11 C API for ISO-19111 functionality

enum iso19111_types::PJ_GUESSED_WKT_DIALECT
Guessed WKT “dialect”.

Values:

PJ_GUESSED_WKT2_2018
WKT2_2018

PJ_GUESSED_WKT2_2015
WKT2_2015

PJ_GUESSED_WKT1_GDAL
WKT1

PJ_GUESSED_WKT1_ESRI
ESRI variant of WKT1

PJ_GUESSED_NOT_WKT
Not WKT / unrecognized

enum iso19111_types::PJ_CATEGORY
Object category.

Values:

PJ_CATEGORY_ELLIPSOID
PJ_CATEGORY_PRIME_MERIDIAN
PJ_CATEGORY_DATUM
PJ_CATEGORY_CRS
PJ_CATEGORY_COORDINATE_OPERATION

enum iso19111_types::PJ_TYPE
Object type.

Values:

PJ_TYPE_UNKNOWN
PJ_TYPE_ELLIPSOID


PJ_TYPE_PRIME_MERIDIAN
PJ_TYPE_GEODE蒂CREFERENCE_FRAME
PJ_TYPE_DYNAMIC_GEODEティCREFERENCE_FRAME
PJ_TYPE_VERTICALREFERENCE_FRAME
PJ_TYPE_DYNAMIC_VERTICALREFERENCE_FRAME
PJ_TYPE_DATUM_ENSEMBLE
PJ_TYPE_CRS
   Abstract type, not returned by proj_get_type()
PJ_TYPE_GEODEティC_CRS
PJ_TYPE_GEOCENTRIC_CRS
PJ_TYPE_GEOGRAPHIC_CRS
   proj_get_type() will never return that type, but PJ_TYPE_GEOGRAPHIC_2D_CRS or
   PJ_TYPE_GEOGRAPHIC_3D_CRS.
PJ_TYPE_GEOGRAPHIC_2D_CRS
PJ_TYPE_GEOGRAPHIC_3D_CRS
PJ_TYPE_VERTICAL_CRS
PJ_TYPE_PROJECTED_CRS
PJ_TYPE_COMPOUND_CRS
PJ_TYPE_TEMPORAL_CRS
PJ_TYPE_ENGINEERING_CRS
PJ_TYPE_BOUND_CRS
PJ_TYPE_OTHER_CRS
PJ_TYPE_CONVERSION
PJ_TYPE_TRANSFORMATION
PJ_TYPE_CONCATENATED_OPERATION
PJ_TYPE_OTHER_COORDINATE_OPERATION

enum iso19111_types::PJ_COMPARISON_CRITERION
   Comparison criterion.
   Values:
   PJ_COMP_STRICT
   All properties are identical.
   PJ_COMP_EQUIVALENT
   The objects are equivalent for the purpose of coordinate operations. They can differ by the name of their
   objects, identifiers, other metadata. Parameters may be expressed in different units, provided that the value
   is (with some tolerance) the same once expressed in a common unit.
   PJ_COMP_EQUIVALENT_EXCEPT_AXIS_ORDER_GEOGRCS
   Same as EQUIVALENT, relaxed with an exception that the axis order of the base CRS of a Derived-
   CRS/ProjectedCRS or the axis order of a GeographicCRS is ignored. Only to be used with Derived-
   CRS/ProjectedCRS/GeographicCRS
enum iso19111_types::PJ_WKT_TYPE

   WKT version.
   Values:

   PJ_WKT2_2015
      cf osgeo::proj::io::WKTFormatter::Convention::WKT2

   PJ_WKT2_2015_SIMPLIFIED
      cf osgeo::proj::io::WKTFormatter::Convention::WKT2_SIMPLIFIED

   PJ_WKT2_2018
      cf osgeo::proj::io::WKTFormatter::Convention::WKT2_2018

   PJ_WKT2_2018_SIMPLIFIED
      cf osgeo::proj::io::WKTFormatter::Convention::WKT2_2018_SIMPLIFIED

   PJ_WKT1_GDAL
      cf osgeo::proj::io::WKTFormatter::Convention::WKT1_GDAL

   PJ_WKT1_ESRI
      cf osgeo::proj::io::WKTFormatter::Convention::WKT1_ESRI

enum iso19111_types::PROJ_CRS_EXTENT_USE

   Specify how source and target CRS extent should be used to restrict candidate operations (only taken into account if no explicit area of interest is specified.
   Values:

   PJ_CRS_EXTENT_NONE
      Ignore CRS extent

   PJ_CRS_EXTENT_BOTH
      Test coordinate operation extent against both CRS extent.

   PJ_CRS_EXTENT_INTERSECTION
      Test coordinate operation extent against the intersection of both CRS extent.

   PJ_CRS_EXTENT_SMALLEST
      Test coordinate operation against the smallest of both CRS extent.

enum iso19111_types::PROJ_GRID_AVAILABILITY_USE

   Describe how grid availability is used.
   Values:

   PROJ_GRID_AVAILABILITY_USED_FOR_SORTING
      Grid availability is only used for sorting results. Operations where some grids are missing will be sorted last.

   PROJ_GRID_AVAILABILITY_DISCARD_OPERATION_IF_MISSING_GRID
      Completely discard an operation if a required grid is missing.

   PROJ_GRID_AVAILABILITY_IGNORED
      Ignore grid availability at all. Results will be presented as if all grids were available.

enum iso19111_types::PJ_PROJ_STRING_TYPE

   PROJ string version.
   Values:

   PJ_PROJ_5
      cf osgeo::proj::io::PROJStringFormatter::Convention::PROJ_5
PROJ coordinate transformation software library, Release 6.1.1

```c
PJ_PROJ_4
cf osgeo::proj::io::PROJStringFormatter::Convention::PJ_PROJ_4
```

```c
enum iso19111_types::PROJ_SPATIAL_CRITERION
Spatial criterion to restrict candidate operations.
Values:
```
PROJ_SPATIAL_CRITERION_STRICT_CONTAINMENT
The area of validity of transforms should strictly contain the area of interest.
```
```
PROJ_SPATIAL_CRITERION_PARTIAL_INTERSECTION
The area of validity of transforms should at least intersect the area of interest.
```

```c
enum iso19111_types::PROJ_INTERMEDIATE_CRS_USE
Describe if and how intermediate CRS should be used
Values:
```
PROJ_INTERMEDIATE_CRS_USE_ALWAYS
Always search for intermediate CRS.
```
```
PROJ_INTERMEDIATE_CRS_USE_IF_NO_DIRECT_TRANSFORMATION
Only attempt looking for intermediate CRS if there is no direct transformation available.
```
```
PROJ_INTERMEDIATE_CRS_USE_NEVER
```

```c
enum iso19111_types::PJ_COORDINATE_SYSTEM_TYPE
Type of coordinate system.
Values:
```
PJ_CS_TYPE_UNKNOWN
PJ_CS_TYPE_CARTESIAN
PJ_CS_TYPE_ELLIPSOIDAL
PJ_CS_TYPE_VERTICAL
PJ_CS_TYPE_SPHERICAL
PJ_CS_TYPE_ORDINAL
PJ_CS_TYPE_PARAMETRIC
PJ_CS_TYPE_DATETIMETEMPORAL
PJ_CS_TYPE_TEMPORALCOUNT
PJ_CS_TYPE_TEMPORALMEASURE
```

```c
typedef char **PROJ_STRING_LIST
Type representing a NULL terminated list of NULL-terminate strings.
```

```c
struct PROJ_CRS_INFO
#include <proj.h> Structure given overall description of a CRS.
This structure may grow over time, and should not be directly allocated by client code.
```

```c
struct PROJ_CRS_LIST_PARAMETERS
#include <proj.h> Structure describing optional parameters for proj_get_crs_list();.
This structure may grow over time, and should not be directly allocated by client code.
```
10.5.2 Functions

10.5.2.1 Threading contexts

PROJ coordinate transformation software library, Release 6.1.1

PJ_CONTEXT* proj_context_create (void)
Create a new threading-context.

Returns PJ_CONTEXT*

void proj_context_destroy (PJ_CONTEXT *ctx)
Deallocation a threading-context.

Parameters

• ctx (PJ_CONTEXT*) – Threading context.

10.5.2.2 Transformation setup

The objects returned by the functions defined in this section have minimal interaction with the the functions of the C API for ISO-19111 functionality, and vice versa. See its introduction paragraph for more details.

PJ* proj_create (PJ_CONTEXT *ctx, const char *definition)
Create a transformation object, or a CRS object, from:

• a proj-string,
• a WKT string,
• an object code (like “EPSG:4326”, “urn:ogc:def:crs:EPSG::4326”, “urn:ogc:def:coordinateOperation:EPSG::1671”),
• a OGC URN combining references for compound coordinate reference systems (e.g “urn:ogc:def:crs,crs:EPSG::2393,crs:EPSG::5717” or custom abbreviated syntax “EPSG:2393+5717”),
• a OGC URN combining references for concatenated operations (e.g. “urn:ogc:def:coordinateOperation, coordinateOperation:EPSG::3895,coordinateOperation:EPSG::1618”)

Example call:

PJ *P = proj_create(0, "+proj=etmerc +lat_0=38 +lon_0=125 +ellps=bessel");

If a proj-string contains a +type=crs option, then it is interpreted as a CRS definition. In particular geographic CRS are assumed to have axis in the longitude, latitude order and with degree angular unit. The use of proj-string to describe a CRS is discouraged. It is a legacy means of conveying CRS descriptions: use of object codes (EPSG:XXXX typically) or WKT description is recommended for better expressivity.

If a proj-string does not contain +type=crs, then it is interpreted as a coordination operation / transformation.

If creation of the transformation object fails, the function returns 0 and the PROJ error number is updated. The error number can be read with proj_errno() or proj_context_errno().

The returned PJ-pointer should be deallocated with proj_destroy().

Parameters

• ctx (PJ_CONTEXT*) – Threading context.
• definition (const char*) – Proj-string of the desired transformation.

PJ* proj_create_argv (PJ_CONTEXT *ctx, int argc, char **argv)
Create a transformation object, or a CRS object, with argc/argv-style initialization. For this application each parameter in the defining proj-string is an entry in argv.

10.5. Reference
Example call:

```c
char *args[3] = {"proj=utm", "zone=32", "ellps=GRS80"};
PJ* P = proj_create_argv(0, 3, args);
```

If there is a type=crs argument, then the arguments are interpreted as a CRS definition. In particular geographic CRS are assumed to have axis in the longitude, latitude order and with degree angular unit.

If there is no type=crs argument, then it is interpreted as a coordination operation / transformation.

If creation of the transformation object fails, the function returns 0 and the PROJ error number is updated. The error number can be read with `proj_errno()` or `proj_context_errno()`.

The returned `PJ`-pointer should be deallocated with `proj_destroy()`.

Parameters

- `ctx` (`PJ_CONTEXT*`) – Threading context
- `argc` (`int`) – Count of arguments in `argv`
- `argv` (`char**`) – Vector of strings with proj-string parameters, e.g. `+proj=merc`

Returns `PJ*`

```c
PJ* proj_create_crs_to_crs(PJ_CONTEXT *ctx, const char *source_crs, const char *target_crs, PJ_AREA *area)
```

Create a transformation object that is a pipeline between two known coordinate reference systems.

source_crs and target_crs can be:

- a “AUTHORITY:CODE”, like EPSG:25832. When using that syntax for a source CRS, the created pipeline will expect that the values passed to `proj_trans()` respect the axis order and axis unit of the official definition (so for example, for EPSG:4326, with latitude first and longitude next, in degrees). Similarly, when using that syntax for a target CRS, output values will be emitted according to the official definition of this CRS.
- a PROJ string, like “+proj=longlat +datum=WGS84”. When using that syntax, the axis order and unit for geographic CRS will be longitude, latitude, and the unit degrees.
- the name of a CRS as found in the PROJ database, e.g “WGS84”, “NAD27”, etc.
- more generally any string accepted by `proj_create()` representing a CRS

An “area of use” can be specified in area. When it is supplied, the more accurate transformation between two given systems can be chosen.

When no area of use is specific and several coordinate operations are possible depending on the area of use, this function will internally store those candidate coordinate operations in the return `PJ` object. Each subsequent coordinate transformation done with `proj_trans()` will then select the appropriate coordinate operation by comparing the input coordinates with the area of use of the candidate coordinate operations.

Example call:

```c
PJ *P = proj_create_crs_to_crs(0, "EPSG:25832", "EPSG:25833", 0);
```

If creation of the transformation object fails, the function returns 0 and the PROJ error number is updated. The error number can be read with `proj_errno()` or `proj_context_errno()`.

The returned `PJ`-pointer should be deallocated with `proj_destroy()`.

Parameters

- `ctx` (`PJ_CONTEXT*`) – Threading context.
PROJ coordinate transformation software library, Release 6.1.1

• source_crs (const char*) – Source CRS.
• target_crs (const char*) – Destination SRS.
• area (PJ_AREA) – Descriptor of the desired area for the transformation.

Returns PJ*

PJ *proj_normalize_for_visualization (PJ_CONTEXT *ctx, const PJ* obj)
New in version 6.1.0.
Returns a PJ* object whose axis order is the one expected for visualization purposes.
The input object must be a coordinate operation, that has been created with proj_create_crs_to_crs(). If the axis
order of its source or target CRS is northing,easting, then an axis swap operation will be inserted.
The returned PJ-pointer should be deallocated with proj_destroy().

Parameters
• ctx (PJ_CONTEXT*) – Threading context.
• obj – Object of type CoordinateOperation

Returns PJ*

PJ* proj_destroy (PJ *P)
Deallocation a PJ transformation object.

Parameters
• P (PJ*) –

Returns PJ*

10.5.2.3 Area of interest

New in version 6.0.0.

PJ_AREA* proj_area_create (void)
Create an area of use.

Such an area of use is to be passed to proj_create_crs_to_crs() to specify the area of use for the
choice of relevant coordinate operations.

Returns PJ_AREA* to be deallocated with proj_area_destroy()

void proj_area_set_bbox (PJ_AREA *area, double west_lon_degree, double south_lat_degree, dou-
dle east_lon_degree, double north_lat_degree)
Set the bounding box of the area of use
Such an area of use is to be passed to proj_create_crs_to_crs() to specify the area of use for the
choice of relevant coordinate operations.

In the case of an area of use crossing the antimeridian (longitude +/- 180 degrees), west_lon_degree will be
greater than east_lon_degree.

Parameters
• area – Pointer to an object returned by proj_area_create().
• west_lon_degree – West longitude, in degrees. In [-180,180] range.
• south_lat_degree – South latitude, in degrees. In [-90,90] range.
• east_lon_degree – East longitude, in degrees. In [-180,180] range.
• **north_lat_degree** – North latitude, in degrees. In [-90,90] range.

```c
void proj_area_destroy(PJ_AREA* area)
    Deallocate a PJ_AREA object.
    :param PJ_AREA* area
```

### 10.5.2.4 Coordinate transformation

**PJ_COORD proj_trans**(PJ *P, PJ_DIRECTION direction, PJ_COORD coord)

Transform a single PJ_COORD coordinate.

**Parameters**

- **P (PJ*)** –
- **direction (PJ_DIRECTION)** – Transformation direction.
- **coord (PJ_COORD)** – Coordinate that will be transformed.

**Returns** PJ_COORD

```c
size_t proj_trans_generic(PJ *P, PJ_DIRECTION direction, double *x, size_t sx, size_t nx, double *y, size_t sy, size_t ny, double *z, size_t sz, size_t nz, double *t, size_t st, size_t nt)
```

Transform a series of coordinates, where the individual coordinate dimension may be represented by an array that is either

1. fully populated
2. a null pointer and/or a length of zero, which will be treated as a fully populated array of zeroes
3. of length one, i.e. a constant, which will be treated as a fully populated array of that constant value

**Note:** Even though he coordinate components are named x, y, z and t, axis ordering of the to and from CRS is respected. Transformations exhibit the same behaviour as if they were gathered in a PJ_COORD struct.

The strides, sx, sy, sz, st, represent the step length, in bytes, between consecutive elements of the corresponding array. This makes it possible for `proj_trans_generic()` to handle transformation of a large class of application specific data structures, without necessarily understanding the data structure format, as in:

```c
typedef struct {
    double x, y;
    int quality_level;
    char surveyor_name[134];
} XYQS;

XYQS survey[345];
double height = 23.45;
size_t stride = sizeof (XYQS);
...

proj_trans_generic {
    P, PJ_INV, sizeof(XYQS),
    *(survey[0].x), stride, 345, /* We have 345 eastings */
    *(survey[0].y), stride, 345, /* ...and 345 northings. */
    &height, 1, /* The height is the constant 23.45 m */
```
This is similar to the inner workings of the deprecated `pj_transform()` function, but the stride functionality has been generalized to work for any size of basic unit, not just a fixed number of doubles.

In most cases, the stride will be identical for x, y, z, and t, since they will typically be either individual arrays (`stride = sizeof(double)`), or strided views into an array of application specific data structures (`stride = sizeof(...)`).

But in order to support cases where x, y, z, and t come from heterogeneous sources, individual strides, `sx`, `sy`, `sz`, `st`, are used.

**Note:** Since `proj_trans_generic()` does its work *in place*, this means that even the supposedly constants (i.e. length 1 arrays) will return from the call in altered state. Hence, remember to reinitialize between repeated calls.

**Parameters**

- `P (PJ*)` – Transformation object
- `direction` – Transformation direction
- `x (double*)` – Array of x-coordinates
- `y (double*)` – Array of y-coordinates
- `z (double*)` – Array of z-coordinates
- `t (double*)` – Array of t-coordinates
- `sx (size_t)` – Step length, in bytes, between consecutive elements of the corresponding array
- `nx (size_t)` – Number of elements in the corresponding array
- `sy (size_t)` – Step length, in bytes, between consecutive elements of the corresponding array
- `ny (size_t)` – Number of elements in the corresponding array
- `sz (size_t)` – Step length, in bytes, between consecutive elements of the corresponding array
- `nz (size_t)` – Number of elements in the corresponding array
- `st (size_t)` – Step length, in bytes, between consecutive elements of the corresponding array
- `nt (size_t)` – Number of elements in the corresponding array

**Returns**

Number of transformations successfully completed

```
size_t proj_trans_array (PJ *P, PJ_DIRECTION direction, size_t n, PJ_COORD *coord)
```

Batch transform an array of `PJ_COORD`.

**Parameters**

- `P (PJ*)` –
- `direction (PJ_DIRECTION)` – Transformation direction
10.5.2.5 Error reporting

int proj_errno (PJ *P)

Get a reading of the current error-state of P. An non-zero error codes indicates an error either with the transformation setup or during a transformation. In cases P is 0 the error number of the default context is read. A text representation of the error number can be retrieved with proj_errno_string().

Param PJ* P: Transformation object.

Returns int

int proj_context_errno (PJ_CONTEXT *ctx)

Get a reading of the current error-state of ctx. An non-zero error codes indicates an error either with the transformation setup or during a transformation. A text representation of the error number can be retrieved with proj_errno_string().

Param PJ_CONTEXT* ctx: threading context.

Returns int

void proj_errno_set (PJ *P, int err)

Change the error-state of P to err.

param PJ* P Transformation object.

param int err Error number.

int proj_errno_reset (PJ *P)

Clears the error number in P, and bubbles it up to the context.

Example:

```c
void foo (PJ *P) {
    int last_errno = proj_errno_reset (P);
    do_something_with_P (P);
    /* failure - keep latest error status */
    if (proj_errno(P))
        return;
    /* success - restore previous error status */
    proj_errno_restore (P, last_errno);
    return;
}
```

Param PJ* P: Transformation object.

Returns int Returns the previous value of the errno, for convenient reset/restore operations.

void proj_errno_restore (PJ *P, int err)

Reduce some mental impedance in the canonical reset/restore use case: Basically, proj_errno_restore() is a synonym for proj_errno_set(), but the use cases are very different: set indicate an error to higher level user code, restore passes previously set error indicators in case of no errors at this level.

Hence, although the inner working is identical, we provide both options, to avoid some rather confusing real world code.
See usage example under `proj_errno_reset()`

Parameters
- `P (PJ*)` – Transformation object.
- `err (int)` – Error code.

`const char* proj_errno_string (int err)`
New in version 5.1.0.
Get a text representation of an error number.

Parameters
- `err (int)` – Error number.

Returns `const char*` String with description of error.

### 10.5.2.6 Logging

`PJ_LOG_LEVEL proj_log_level (PJ_CONTEXT *ctx, PJ_LOG_LEVEL level)`
Get and set logging level for a given context. Changes the log level to `level` and returns the previous logging level. If called with `level` set to `PJ_LOG_TELL` the function returns the current logging level without changing it.

Parameters
- `ctx (PJ_CONTEXT*)` – Threading context.
- `level (PJ_LOG_LEVEL)` – New logging level.

Returns `PJ_LOG_LEVEL`
New in version 5.1.0.

void `proj_log_func (PJ_CONTEXT *ctx, void *app_data, PJ_LOG_FUNCTION logf)`
Override the internal log function of PROJ.

Parameters
- `ctx (PJ_CONTEXT*)` – Threading context.
- `app_data (void*)` – Pointer to data structure used by the calling application.
- `logf (PJ_LOG_FUNCTION)` – Log function that overrides the PROJ log function.

New in version 5.1.0.

### 10.5.2.7 Info functions

`PJ_INFO proj_info (void)`
Get information about the current instance of the PROJ library.

Returns `PJ_INFO`

`PJ_PROJ_INFO proj_pj_info (const PJ*)`
Get information about a specific transformation object, `P`.

Parameters
- `P (const PJ*)` – Transformation object

Returns `PJ_PROJ_INFO`
**PJ_GRID_INFO** `proj_grid_info` (const char *gridname)
Get information about a specific grid.

Parameters

- gridname (const char*) Gridname in the PROJ searchpath

Returns `PJ_GRID_INFO`

**PJ_INIT_INFO** `proj_init_info` (const char *initname)
Get information about a specific init file.

Parameters

- initname (const char*) Init file in the PROJ searchpath

Returns `PJ_INIT_INFO`

### 10.5.2.8 Lists

const `PJ_OPERATIONS*` `proj_list_operations` (void)
Get a pointer to an array of all operations in PROJ. The last entry of the returned array is a NULL-entry. The array is statically allocated and does not need to be freed after use.

Print a list of all operations in PROJ:

```c
PJ_OPERATIONS *ops;
for (ops = proj_list_operations(); ops->id; ++ops)
    printf("%s
", ops->id);
```

Returns `PJ_OPERATIONS*`

const `PJ_ELLPS*` `proj_list_ellps` (void)
Get a pointer to an array of ellipsoids defined in PROJ. The last entry of the returned array is a NULL-entry. The array is statically allocated and does not need to be freed after use.

Returns `PJ_ELLPS*`

const `PJ_UNITS*` `proj_list_units` (void)
Get a pointer to an array of distance units defined in PROJ. The last entry of the returned array is a NULL-entry. The array is statically allocated and does not need to be freed after use.

Returns `PJ_UNITS*`

const `PJ_PRIME_MERIDIANS*` `proj_list_prime_meridians` (void)
Get a pointer to an array of prime meridians defined in PROJ. The last entry of the returned array is a NULL-entry. The array is statically allocated and does not need to be freed after use.

Returns `PJ_PRIME_MERIDIANS*`
### 10.5.2.9 Distances

**double proj_lp_dist** (const *PJ*, *PJ_COORD a, PJ_COORD b)

Calculate geodesic distance between two points in geodetic coordinates. The calculated distance is between the two points located on the ellipsoid.

**Parameters**

- `P` (*PJ*) – Transformation object
- `a` (*PJ_COORD*) – Coordinate of first point
- `b` (*PJ_COORD*) – Coordinate of second point

**Returns** `double` Distance between `a` and `b` in meters.

**double proj_lpz_dist** (const *PJ*, *PJ_COORD a, PJ_COORD b)

Calculate geodesic distance between two points in geodetic coordinates. Similar to `proj_lp_dist()` but also takes the height above the ellipsoid into account.

**Parameters**

- `P` (*PJ*) – Transformation object
- `a` (*PJ_COORD*) – Coordinate of first point
- `b` (*PJ_COORD*) – Coordinate of second point

**Returns** `double` Distance between `a` and `b` in meters.

**double proj_xy_dist** (*PJ_COORD a, PJ_COORD b*)

Calculate 2-dimensional euclidean between two projected coordinates.

**Parameters**

- `a` (*PJCOORD*) – First coordinate
- `b` (*PJCOORD*) – Second coordinate

**Returns** `double` Distance between `a` and `b` in meters.

**double proj_xyz_dist** (*PJ_COORD a, PJ_COORD b*)

Calculate 3-dimensional euclidean between two projected coordinates.

**Parameters**

- `a` (*PJCOORD*) – First coordinate
- `b` (*PJCOORD*) – Second coordinate

**Returns** `double` Distance between `a` and `b` in meters.

### 10.5.2.10 Various

**PJ_COORD proj_coord** (double x, double y, double z, double t)

Initializer for the `PJ_COORD` union. The function is shorthand for the otherwise convoluted assignment. Equivalent to

```
PJ_COORD c = {{10.0, 20.0, 30.0, 40.0}};
```

or
Since \texttt{PJ\_COORD} is a union of structs, the above assignment can also be expressed in terms of the other types in the union, e.g. \texttt{PJ\_UVWT} or \texttt{PJ\_LPZT}.

**Parameters**

- \texttt{x (double)} – 1st component in a \texttt{PJ\_COORD}
- \texttt{y (double)} – 2nd component in a \texttt{PJ\_COORD}
- \texttt{z (double)} – 3rd component in a \texttt{PJ\_COORD}
- \texttt{t (double)} – 4th component in a \texttt{PJ\_COORD}

**Returns** \texttt{PJ\_COORD}

```
double \texttt{proj\_roundtrip} (\texttt{PJ \*P}, \texttt{PJ\_DIRECTION direction}, \texttt{int n}, \texttt{PJ\_COORD \*coord})
```

Measure internal consistency of a given transformation. The function performs \texttt{n} round trip transformations starting in either the forward or reverse direction. Returns the euclidean distance of the starting point \texttt{coo} and the resulting coordinate after \texttt{n} iterations back and forth.

**Parameters**

- \texttt{P (const PJ\*)} –
- \texttt{direction (PJ\_DIRECTION)} – Starting direction of transformation
- \texttt{n (int)} – Number of roundtrip transformations
- \texttt{coord (PJ\_COORD)} – Input coordinate

**Returns** double Distance between original coordinate and the resulting coordinate after \texttt{n} transformation iterations.

**PJ\_FACTORS** \texttt{proj\_factors} (\texttt{PJ \*P}, \texttt{PJ\_COORD lp})

Calculate various cartographic properties, such as scale factors, angular distortion and meridian convergence. Depending on the underlying projection values will be calculated either numerically (default) or analytically.

The function also calculates the partial derivatives of the given coordinate.

**Parameters**

- \texttt{P (const PJ\*)} – Transformation object
- \texttt{lp (const PJ\_COORD)} – Geodetic coordinate

**Returns** \texttt{PJ\_FACTORS}

```
double \texttt{proj\_torad} (double \texttt{angle\_in\_degrees})
```

Convert degrees to radians.

**Parameters**

- \texttt{angle\_in\_degrees (double)} – Degrees

**Returns** double Radians

```
double \texttt{proj\_todeg} (double \texttt{angle\_in\_radians})
```

Convert radians to degrees
Parameters

- `angle_in_radians(double)` – Radians

Returns `double` Degrees

double `proj_dmstor` (const char *is, char **rs)

Convert string of degrees, minutes and seconds to radians. Works similarly to the C standard library function `strtod()`.

Parameters

- `is` (const char*) – Value to be converted to radians
- `rs` – Reference to an already allocated char*, whose value is set by the function to the next character in `is` after the numerical value.

char *`proj_rtdms` (char *s, double r, int pos, int neg)

Convert radians to string representation of degrees, minutes and seconds.

Parameters

- `s` (char*) – Buffer that holds the output string
- `r` (double) – Value to convert to dms-representation
- `pos` (int) – Character denoting positive direction, typically ‘N’ or ‘E’.
- `neg` (int) – Character denoting negative direction, typically ‘S’ or ‘W’.

Returns char* Pointer to output buffer (same as `s`)

int `proj_angular_input` (PJ *P, enum PJ_DIRECTION dir)

Check if a operation expects input in radians or not.

Parameters

- `P` (const PJ*) – Transformation object
- `direction` (PJ_DIRECTION) – Starting direction of transformation

Returns int 1 if input units is expected in radians, otherwise 0

int `proj_angular_output` (PJ *P, enum PJ_DIRECTION dir)

Check if an operation returns output in radians or not.

Parameters

- `P` (const PJ*) – Transformation object
- `direction` (PJ_DIRECTION) – Starting direction of transformation

Returns int 1 if output units is expected in radians, otherwise 0

10.5.2.11 C API for ISO-19111 functionality

New in version 6.0.0.

The PJ* objects returned by `proj_create_from_wkt()`, `proj_create_from_database()` and other functions in that section will have generally minimal interaction with the functions declared in the previous sections (calling those functions on those objects will either return an error or default/non-sensical values). The exception is for ISO19111 objects of type CoordinateOperation that can be exported as a valid PROJ pipeline. In this case, objects will work for example with `proj_trans_generic()`. Conversely, objects returned by `proj_create()` and `proj_create_argv()`, which are not of type CRS (can be tested with `proj_is_crs()`), will return an error when used with functions of this section.

10.5. Reference
void proj_string_list_destroy (PROJ_STRING_LIST list)

Free a list of NULL terminated strings.

int proj_context_set_database_path (PJ_CONTEXT *ctx, const char *dbPath, const char *const *auxDbPaths, const char *const *options)

Explicitly point to the main PROJ CRS and coordinate operation definition database ("proj.db"), and potentially auxiliary databases with same structure.

Return  TRUE in case of success

Parameters

• ctx: PROJ context, or NULL for default context
• dbPath: Path to main database, or NULL for default.
• auxDbPaths: NULL-terminated list of auxiliary database filenames, or NULL.
• options: should be set to NULL for now

const char *proj_context_get_database_path (PJ_CONTEXT *ctx)

Returns the path to the database.

The returned pointer remains valid while ctx is valid, and until proj_context_set_database_path() is called.

Return  path, or nullptr

Parameters

• ctx: PROJ context, or NULL for default context

const char *proj_context_get_database_metadata (PJ_CONTEXT *ctx, const char *key)

Return a metadata from the database.

The returned pointer remains valid while ctx is valid, and until proj_context_get_database_metadata() is called.

Return  value, or nullptr

Parameters

• ctx: PROJ context, or NULL for default context
• key: Metadata key. Must not be NULL

PJ_GUESSED_WKT_DIALECT proj_context_guess_wkt_dialect (PJ_CONTEXT *ctx, const char *wkt)

Guess the “dialect” of the WKT string.

Parameters

• ctx: PROJ context, or NULL for default context
• wkt: String (must not be NULL)

PJ *proj_create_from_wkt (PJ_CONTEXT *ctx, const char *wkt, const char *const *options, PROJ_STRING_LIST *out_warnings, PROJ_STRING_LIST *out_grammar_errors)

Instantiate an object from a WKT string.

This function calls osgeo::proj::io::WKTParser::createFromWKT()

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.
Return Object that must be unreferenced with proj_destroy(), or NULL in case of error.

Parameters

- ctx: PROJ context, or NULL for default context
- wkt: WKT string (must not be NULL)
- options: null-terminated list of options, or NULL. Currently supported options are:
  - STRICT=YES/NO. Defaults to NO. When set to YES, strict validation will be enabled.
- out_warnings: Pointer to a PROJ_STRING_LIST object, or NULL. If provided, *out_warnings will contain a list of warnings, typically for non recognized projection method or parameters. It must be freed with proj_string_list_destroy().
- out_grammar_errors: Pointer to a PROJ_STRING_LIST object, or NULL. If provided, *out_grammar_errors will contain a list of errors regarding the WKT grammar. It must be freed with proj_string_list_destroy().

PJ *proj_create_from_database (PJ_CONTEXT *ctx, const char *auth_name, const char *code, PJ_CATEGORY category, int usePROJAlternativeGridNames, const char *const *options)

Instantiate an object from a database lookup.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.

Return Object that must be unreferenced with proj_destroy(), or NULL in case of error.

Parameters

- ctx: Context, or NULL for default context.
- auth_name: Authority name (must not be NULL)
- code: Object code (must not be NULL)
- category: Object category
- usePROJAlternativeGridNames: Whether PROJ alternative grid names should be substituted to the official grid names. Only used on transformations
- options: should be set to NULL for now

int proj_uom_get_info_from_database (PJ_CONTEXT *ctx, const char *auth_name, const char *code, const char **out_name, double *out_conv_factor, const char **out_category)

Get information for a unit of measure from a database lookup.

Return TRUE in case of success

Parameters

- ctx: Context, or NULL for default context.
- auth_name: Authority name (must not be NULL)
- code: Unit of measure code (must not be NULL)
- out_name: Pointer to a string value to store the parameter name. or NULL. This value remains valid until the next call to proj_uom_get_info_from_database() or the context destruction.
- out_conv_factor: Pointer to a value to store the conversion factor of the prime meridian longitude unit to radian. or NULL
PROJ coordinate transformation software library, Release 6.1.1

- out_category: Pointer to a string value to store the parameter name. or NULL. This value might be “unknown”, “none”, “linear”, “angular”, “scale”, “time” or “parametric”;

PJ *proj_clone (PJ_CONTEXT *ctx, const PJ *obj)

“Clone” an object.

Technically this just increases the reference counter on the object, since PJ objects are immutable.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.

Return Object that must be unreferenced with proj_destroy(), or NULL in case of error.

Parameters

- ctx: PROJ context, or NULL for default context
- obj: Object to clone. Must not be NULL.

PJ_OBJ_LIST *proj_create_from_name (PJ_CONTEXT *ctx, const char *auth_name, const char *searchedName, const PJ_TYPE *types, size_t typesCount, int approximateMatch, size_t limitResultCount, const char *const *options)

Return a list of objects by their name.

Return a result set that must be unreferenced with proj_list_destroy(), or NULL in case of error.

Parameters

- ctx: Context, or NULL for default context.
- auth_name: Authority name, used to restrict the search. Or NULL for all authorities.
- searchedName: Searched name. Must be at least 2 character long.
- types: List of object types into which to search. If NULL, all object types will be searched.
- typesCount: Number of elements in types, or 0 if types is NULL
- approximateMatch: Whether approximate name identification is allowed.
- limitResultCount: Maximum number of results to return. Or 0 for unlimited.
- options: should be set to NULL for now

PJ_TYPE proj_get_type (const PJ *obj)

Return the type of an object.

Return its type.

Parameters

- obj: Object (must not be NULL)

int proj_is_deprecated (const PJ *obj)

Return whether an object is deprecated.

Return TRUE if it is deprecated, FALSE otherwise

Parameters

- obj: Object (must not be NULL)
PJ_OBJ_LIST *proj_get_non_deprecated(PJ_CONTEXT *ctx, const PJ *obj)
Return a list of non-deprecated objects related to the passed one.

Parameters
• ctx: Context, or NULL for default context.
• obj: Object (of type CRS for now) for which non-deprecated objects must be searched. Must not be NULL.

int proj_is_equivalent_to(const PJ *obj, const PJ *other, PJ_COMPARISON_CRITERION criterion)
Return whether two objects are equivalent.

Return TRUE if they are equivalent

Parameters
• obj: Object (must not be NULL)
• other: Other object (must not be NULL)
• criterion: Comparison criterion

int proj_is_crs(const PJ *obj)
Return whether an object is a CRS.

Parameters
• obj: Object (must not be NULL)

const char *proj_get_name(const PJ *obj)
Get the name of an object.

The lifetime of the returned string is the same as the input obj parameter.

Return a string, or NULL in case of error or missing name.

Parameters
• obj: Object (must not be NULL)

const char *proj_get_id_auth_name(const PJ *obj, int index)
Get the authority name / codespace of an identifier of an object.

The lifetime of the returned string is the same as the input obj parameter.

Return a string, or NULL in case of error or missing name.

Parameters
• obj: Object (must not be NULL)
• index: Index of the identifier. 0 = first identifier

const char *proj_get_id_code(const PJ *obj, int index)
Get the code of an identifier of an object.

The lifetime of the returned string is the same as the input obj parameter.
Return a string, or NULL in case of error or missing name.

Parameters

- obj: Object (must not be NULL)
- index: Index of the identifier. 0 = first identifier

int proj_get_area_of_use (PJ_CONTEXT *ctx, const PJ *obj, double *out_west_lon_degree, double *out_south_lat_degree, double *out_east_lon_degree, double *out_north_lat_degree, const char **out_area_name)

Return the area of use of an object.

Return TRUE in case of success, FALSE in case of error or if the area of use is unknown.

Parameters

- ctx: PROJ context, or NULL for default context
- obj: Object (must not be NULL)
- out_west_lon_degree: Pointer to a double to receive the west longitude (in degrees). Or NULL. If the returned value is -1000, the bounding box is unknown.
- out_south_lat_degree: Pointer to a double to receive the south latitude (in degrees). Or NULL. If the returned value is -1000, the bounding box is unknown.
- out_east_lon_degree: Pointer to a double to receive the east longitude (in degrees). Or NULL. If the returned value is -1000, the bounding box is unknown.
- out_north_lat_degree: Pointer to a double to receive the north latitude (in degrees). Or NULL. If the returned value is -1000, the bounding box is unknown.
- out_area_name: Pointer to a string to receive the name of the area of use. Or NULL. *p_area_name is valid while obj is valid itself.

const char *proj_as_wkt (PJ_CONTEXT *ctx, const PJ *obj, PJ_WKT_TYPE type, const char *const *options)

Get a WKT representation of an object.

The returned string is valid while the input obj parameter is valid, and until a next call to proj_as_wkt() with the same input object.

This function calls osgeo::proj::io::IWKTExportable::exportToWKT().

This function may return NULL if the object is not compatible with an export to the requested type.

Return a string, or NULL in case of error.

Parameters

- ctx: PROJ context, or NULL for default context
- obj: Object (must not be NULL)
- type: WKT version.
- options: null-terminated list of options, or NULL. Currently supported options are:
  - MULTILINE=YES/NO. Defaults to YES, except for WKT1_ESRI
  - INDENTATION_WIDTH=number. Defaults to 4 (when multiline output is on).
– OUTPUT_AXIS=AUTO/YES/NO. In AUTO mode, axis will be output for WKT2 variants, for WKT1_GDAL for ProjectedCRS with easting/northing ordering (otherwise stripped), but not for WKT1_ESRI. Setting to YES will output them unconditionally, and to NO will omit them unconditionally.

```c
const char *proj_as_proj_string (PJ_CONTEXT *ctx, const PJ *obj, PJ_PROJ_STRING_TYPE type, const char *const *options)
```

Get a PROJ string representation of an object.

The returned string is valid while the input obj parameter is valid, and until a next call to `proj_as_proj_string()` with the same input object.

This function calls `osgeo::proj::io::IPROJStringExportable::exportToPROJString()`.

This function may return NULL if the object is not compatible with an export to the requested type.

**Return** a string, or NULL in case of error.

**Parameters**

- **ctx**: PROJ context, or NULL for default context
- **obj**: Object (must not be NULL)
- **type**: PROJ String version.
- **options**: NULL-terminated list of strings with “KEY=VALUE” format. or NULL. The currently recognized option is USE_APPROX_TMERC=YES to add the +approx flag to +proj=tmerc or +proj=utm

```c
PJ *proj_get_source_crs (PJ_CONTEXT *ctx, const PJ *obj)
```

Return the base CRS of a BoundCRS or a DerivedCRS/ProjectedCRS, or the source CRS of a CoordinateOperation.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.

**Return** Object that must be unreferenced with proj_destroy(), or NULL in case of error, or missing source CRS.

**Parameters**

- **ctx**: PROJ context, or NULL for default context
- **obj**: Object of type BoundCRS or CoordinateOperation (must not be NULL)

```c
PJ *proj_get_target_crs (PJ_CONTEXT *ctx, const PJ *obj)
```

Return the hub CRS of a BoundCRS or the target CRS of a CoordinateOperation.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.

**Return** Object that must be unreferenced with proj_destroy(), or NULL in case of error, or missing target CRS.

**Parameters**

- **ctx**: PROJ context, or NULL for default context
- **obj**: Object of type BoundCRS or CoordinateOperation (must not be NULL)
PJ_OBJ_LIST *proj_identify (PJ_CONTEXT *ctx, const PJ *obj, const char *auth_name, const char *const *options, int **out_confidence)

Identify the CRS with reference CRSs.

The candidate CRSs are either hard-coded, or looked in the database when it is available.

The method returns a list of matching reference CRS, and the percentage (0-100) of confidence in the match. The list is sorted by decreasing confidence.

100% means that the name of the reference entry perfectly matches the CRS name, and both are equivalent. In which case a single result is returned. 90% means that CRS are equivalent, but the names are not exactly the same. 70% means that CRS are equivalent, but the names do not match at all. 25% means that the CRS are not equivalent, but there is some similarity in the names. Other confidence values may be returned by some specialized implementations.

This is implemented for GeodeticCRS, ProjectedCRS, VerticalCRS and CompoundCRS.

Return a list of matching reference CRS, or nullptr in case of error.

Parameters

- ctx: PROJ context, or NULL for default context
- obj: Object of type CRS. Must not be NULL
- auth_name: Authority name, or NULL for all authorities
- options: Placeholder for future options. Should be set to NULL.
- out_confidence: Output parameter. Pointer to an array of integers that will be allocated by the function and filled with the confidence values (0-100). There are as many elements in this array as proj_list_get_count() returns on the return value of this function. *confidence should be released with proj_int_list_destroy().

void proj_int_list_destroy (int *list)

Free an array of integer.

PROJ_STRING_LIST proj_get_authorities_from_database (PJ_CONTEXT *ctx)

Return the list of authorities used in the database.

The returned list is NULL terminated and must be freed with proj_string_list_destroy().

Return a NULL terminated list of NUL-terminated strings that must be freed with proj_string_list_destroy(), or NULL in case of error.

Parameters

- ctx: PROJ context, or NULL for default context

PROJ_STRING_LIST proj_get_codes_from_database (PJ_CONTEXT *ctx, const char *auth_name, PJ_TYPE type, int allow_deprecated)

Returns the set of authority codes of the given object type.

The returned list is NULL terminated and must be freed with proj_string_list_destroy().

Return a NULL terminated list of NUL-terminated strings that must be freed with proj_string_list_destroy(), or NULL in case of error.

See proj_get_crs_info_list_from_database()
• ctx: PROJ context, or NULL for default context.
• auth_name: Authority name (must not be NULL)
• type: Object type.
• allow Deprecated: whether we should return deprecated objects as well.

```c
PROJ_CRS_LIST_PARAMETERS *proj_get_crs_list_parameters_create (void)
```
Instantiate a default set of parameters to be used by proj_get_crs_list().

**Return** a new object to free with proj_get_crs_list_parameters_destroy().

```c
void proj_get_crs_list_parameters_destroy (PROJ_CRS_LIST_PARAMETERS *params)
```
Destroy an object returned by proj_get_crs_list_parameters_create().

```c
PROJ_CRS_INFO **proj_get_crs_info_list_from_database (PJ_CONTEXT *ctx, const char *auth_name, const PROJ_CRS_LIST_PARAMETERS *params, int *out_result_count)
```
Enumerate CRS objects from the database, taking into account various criteria.
The returned object is an array of PROJ_CRS_INFO* pointers, whose last entry is NULL. This array should be freed with proj_crs_info_list_destroy().

When no filter parameters are set, this is functionally equivalent to proj_get_crs_info_list_from_database(), instantiating a PJ* object for each of the proj_create_from_database() and retrieving information with the various getters. However this function will be much faster.

**Return** an array of PROJ_CRS_INFO* pointers to be freed with proj_crs_info_list_destroy(), or NULL in case of error.

**Parameters**

• ctx: PROJ context, or NULL for default context
• auth_name: Authority name, used to restrict the search. Or NULL for all authorities.
• params: Additional criteria, or NULL. If not-NULl, params SHOULD have been allocated by proj_get_crs_list_parameters_create(), as the PROJ_CRS_LIST_PARAMETERS structure might grow over time.
• out_result_count: Output parameter pointing to an integer to receive the size of the result list. Might be NULL.

```c
void proj_crs_info_list_destroy (PROJ_CRS_INFO **list)
```
Destroy the result returned by proj_get_crs_info_list_from_database().

```c
PJ_OPERATION_FACTORY_CONTEXT *proj_create_operation_factory_context (PJ_CONTEXT *ctx, const char *authority)
```
Instantiate a context for building coordinate operations between two CRS.
The returned object must be unreferenced with proj_operation_factory_context_destroy() after use.

If authority is NULL or the empty string, then coordinate operations from any authority will be searched, with the restrictions set in the authority_to_authority_preference database table. If authority is set to “any”, then coordinate operations from any authority will be searched. If authority is a non-empty string different of “any”, then coordinate operations will be searched only in that authority namespace.
**Return** Object that must be unreferenced with `proj_operation_factory_context_destroy()`, or NULL in case of error.

**Parameters**
- `ctx`: Context, or NULL for default context.
- `authority`: Name of authority to which to restrict the search of candidate operations.

```c
void proj_operation_factory_context_destroy(PJ_OPERATION_FACTORY_CONTEXT *ctx)
```
Drops a reference on an object.

This method should be called one and exactly one for each function returning a `PJ_OPERATION_FACTORY_CONTEXT`.

**Parameters**
- `ctx`: Object, or NULL.

```c
void proj_operation_factory_context_set_desired_accuracy(PJ_CONTEXT *ctx, PJ_OPERATION_FACTORY_CONTEXT *factory_ctx, double accuracy)
```
Set the desired accuracy of the resulting coordinate transformations.

**Parameters**
- `ctx`: PROJ context, or NULL for default context
- `factory_ctx`: Operation factory context. must not be NULL
- `accuracy`: Accuracy in meter (or 0 to disable the filter).

```c
void proj_operation_factory_context_set_area_of_interest(PJ_CONTEXT *ctx, PJ_OPERATION_FACTORY_CONTEXT *factory_ctx, double west_lon_degree, double south_lat_degree, double east_lon_degree, double north_lat_degree)
```
Set the desired area of interest for the resulting coordinate transformations.

For an area of interest crossing the anti-meridian, `west_lon_degree` will be greater than `east_lon_degree`.

**Parameters**
- `ctx`: PROJ context, or NULL for default context
- `factory_ctx`: Operation factory context. must not be NULL
- `west_lon_degree`: West longitude (in degrees).
- `south_lat_degree`: South latitude (in degrees).
- `east_lon_degree`: East longitude (in degrees).
- `north_lat_degree`: North latitude (in degrees).
void proj_operation_factory_context_set_crs_extent_use (PJ_CONTEXT *ctx,
        PJ_OPERATION_FACTORY_CONTEXT *factory_ctx,
        PROJ_CRS_EXTENT_USE use)

Set how source and target CRS extent should be used when considering if a transformation can be used (only takes effect if no area of interest is explicitly defined).

The default is PJ_CRS_EXTENT_SMALLEST.

**Parameters**

- **ctx**: PROJ context, or NULL for default context
- **factory_ctx**: Operation factory context. must not be NULL
- **use**: How source and target CRS extent should be used.

void proj_operation_factory_context_set_spatial_criterion (PJ_CONTEXT *ctx,
        PJ_OPERATION_FACTORY_CONTEXT *factory_ctx,
        PROJ_SPATIAL_CRITERION criterion)

Set the spatial criterion to use when comparing the area of validity of coordinate operations with the area of interest / area of validity of source and target CRS.

The default is PROJ_SPATIAL_CRITERION_STRICT_CONTAINMENT.

**Parameters**

- **ctx**: PROJ context, or NULL for default context
- **factory_ctx**: Operation factory context. must not be NULL
- **criterion**: Spatial criterion to use

void proj_operation_factory_context_set_grid_availability_use (PJ_CONTEXT *ctx,
        PJ_OPERATION_FACTORY_CONTEXT *factory_ctx,
        PROJ_GRID_AVAILABILITY_USE use)

Set how grid availability is used.

The default is USE_FOR_SORTING.

**Parameters**

- **ctx**: PROJ context, or NULL for default context
- **factory_ctx**: Operation factory context. must not be NULL
- **use**: How grid availability is used.
void `proj_operation_factory_context_set_use_proj_alternative_grid_names` (PJ_CONTEXT `*ctx`, PJOPERATION_FACTORY_CONTEXT `*factory_ctx`, int `usePROJNames`)

Set whether PROJ alternative grid names should be substituted to the official authority names.

The default is true.

**Parameters**
- `ctx`: PROJ context, or NULL for default context
- `factory_ctx`: Operation factory context. must not be NULL
- `usePROJNames`: whether PROJ alternative grid names should be used

void `proj_operation_factory_context_set_allow_use_intermediate_crs` (PJ_CONTEXT `*ctx`, PJOPERATION_FACTORY_CONTEXT `*factory_ctx`, PROJ_INTERMEDIATE_CRS_USE `use`)

Set whether an intermediate pivot CRS can be used for researching coordinate operations between a source and target CRS.

Concretely if in the database there is an operation from A to C (or C to A), and another one from C to B (or B to C), but no direct operation between A and B, setting this parameter to true, allow chaining both operations.

The current implementation is limited to researching one intermediate step.

By default, with the IF_NO_DIRECT_TRANSFORMATION strategy, all potential C candidates will be used if there is no direct transformation.

**Parameters**
- `ctx`: PROJ context, or NULL for default context
- `factory_ctx`: Operation factory context. must not be NULL
- `use`: whether and how intermediate CRS may be used.

void `proj_operation_factory_context_set_allowed_intermediate_crs` (PJ_CONTEXT `*ctx`, PJOPERATION_FACTORY_CONTEXT `*factory_ctx`, const char `*const*list_of_auth_name_codes`)

Restrict the potential pivot CRSs that can be used when trying to build a coordinate operation between two CRS that have no direct operation.

**Parameters**
- `ctx`: PROJ context, or NULL for default context
• factory_ctx: Operation factory context. must not be NULL
• list_of_auth_name_codes: an array of strings NLL terminated, with the format { “auth_name1”, “code1”, “auth_name2”, “code2”, ... NULL }

PJ_OBJ_LIST *proj_create_operations(PJ_CONTEXT *ctx, const PJ *source_crs, const PJ *target_crs, const PJ_OPERATION_FACTORY_CONTEXT *operationContext)

Find a list of CoordinateOperation from source_crs to target_crs.

The operations are sorted with the most relevant ones first: by descending area (intersection of the transformation area with the area of interest, or intersection of the transformation with the area of use of the CRS), and by increasing accuracy. Operations with unknown accuracy are sorted last, whatever their area.

Return a result set that must be unreferenced with proj_list_destroy(), or NULL in case of error.

Parameters

• ctx: PROJ context, or NULL for default context
• source_crs: source CRS. Must not be NULL.
• target_crs: source CRS. Must not be NULL.
• operationContext: Search context. Must not be NULL.

int proj_list_get_count(const PJ_OBJ_LIST *result)

Return the number of objects in the result set.

Parameters

• result: Object of type PJ_OBJ_LIST (must not be NULL)

PJ *proj_list_get(PJ_CONTEXT *ctx, const PJ_OBJ_LIST *result, int index)

Return an object from the result set.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.

Return a new object that must be unreferenced with proj_destroy(), or nullptr in case of error.

Parameters

• ctx: PROJ context, or NULL for default context
• result: Object of type PJ_OBJ_LIST (must not be NULL)
• index: Index

void proj_list_destroy(PJ_OBJ_LIST *result)

Drops a reference on the result set.

This method should be called one and exactly one for each function returning a PJ_OBJ_LIST*

Parameters

• result: Object, or NULL.
PJ *proj_crs_get_geodetic_crs (PJ_CONTEXT *ctx, const PJ *crs)
Get the geodeticCRS / geographicCRS from a CRS.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.

Return  Object that must be unreferenced with proj_destroy(), or NULL in case of error.

Parameters
• ctx: PROJ context, or NULL for default context
• crs: Object of type CRS (must not be NULL)

PJ *proj_crs_get_horizontal_datum (PJ_CONTEXT *ctx, const PJ *crs)
Get the horizontal datum from a CRS.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.

Return  Object that must be unreferenced with proj_destroy(), or NULL in case of error.

Parameters
• ctx: PROJ context, or NULL for default context
• crs: Object of type CRS (must not be NULL)

PJ *proj_crs_get_sub_crs (PJ_CONTEXT *ctx, const PJ *crs, int index)
Get a CRS component from a CompoundCRS.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.

Return  Object that must be unreferenced with proj_destroy(), or NULL in case of error.

Parameters
• ctx: PROJ context, or NULL for default context
• crs: Object of type CRS (must not be NULL)
• index: Index of the CRS component (typically 0 = horizontal, 1 = vertical)

PJ *proj_crs_get_datum (PJ_CONTEXT *ctx, const PJ *crs)
Returns the datum of a SingleCRS.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.

Return  Object that must be unreferenced with proj_destroy(), or NULL in case of error (or if there is no datum)

Parameters
• ctx: PROJ context, or NULL for default context
• crs: Object of type SingleCRS (must not be NULL)

PJ *proj_crs_get_coordinate_system (PJ_CONTEXT *ctx, const PJ *crs)
Returns the coordinate system of a SingleCRS.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.
Return Object that must be unreferenced with proj_destroy(), or NULL in case of error.

Parameters

- ctx: PROJ context, or NULL for default context
- crs: Object of type SingleCRS (must not be NULL)

PJ_COORDINATE_SYSTEM_TYPE proj_cs_get_type (PJ_CONTEXT *ctx, const PJ *cs)

Returns the type of the coordinate system.

Return type, or PJ_CS_TYPE_UNKNOWN in case of error.

Parameters

- ctx: PROJ context, or NULL for default context
- cs: Object of type CoordinateSystem (must not be NULL)

int proj_cs_get_axis_count (PJ_CONTEXT *ctx, const PJ *cs)

Returns the number of axis of the coordinate system.

Return number of axis, or -1 in case of error.

Parameters

- ctx: PROJ context, or NULL for default context
- cs: Object of type CoordinateSystem (must not be NULL)

int proj_cs_get_axis_info (PJ_CONTEXT *ctx, const PJ *cs, int index, const char **out_name, const char **out_abbrev, const char **out_direction, double *out_unit_conv_factor, const char **out_unit_name, const char **out_unit_auth_name, const char **out_unit_code)

Returns information on an axis.

Return TRUE in case of success

Parameters

- ctx: PROJ context, or NULL for default context
- cs: Object of type CoordinateSystem (must not be NULL)
- index: Index of the coordinate system (between 0 and proj_cs_get_axis_count() - 1)
- out_name: Pointer to a string value to store the axis name. or NULL
- out_abbrev: Pointer to a string value to store the axis abbreviation. or NULL
- out_direction: Pointer to a string value to store the axis direction. or NULL
- out_unit_conv_factor: Pointer to a double value to store the axis unit conversion factor. or NULL
- out_unit_name: Pointer to a string value to store the axis unit name. or NULL
- out_unit_auth_name: Pointer to a string value to store the axis unit authority name. or NULL
- out_unit_code: Pointer to a string value to store the axis unit code. or NULL
PJ *proj_get_ellipsoid(PJ_CONTEXT *ctx, const PJ *obj)
Get the ellipsoid from a CRS or a GeodeticReferenceFrame.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.

**Return** Object that must be unreferenced with proj_destroy(), or NULL in case of error.

**Parameters**
- *ctx*: PROJ context, or NULL for default context
- *obj*: Object of type CRS or GeodeticReferenceFrame (must not be NULL)

int proj_ellipsoid_get_parameters(PJ_CONTEXT *ctx, const PJ *ellipsoid, double *out_semi_major_metre, double *out_semi_minor_metre, int *out_is_semi_minor_computed, double *out_inv_flattening)

Return ellipsoid parameters.

**Return** TRUE in case of success.

**Parameters**
- *ctx*: PROJ context, or NULL for default context
- *ellipsoid*: Object of type Ellipsoid (must not be NULL)
- *out_semi_major_metre*: Pointer to a value to store the semi-major axis in metre. or NULL
- *out_semi_minor_metre*: Pointer to a value to store the semi-minor axis in metre. or NULL
- *out_is_semi_minor_computed*: Pointer to a boolean value to indicate if the semi-minor value was computed. If FALSE, its value comes from the definition. or NULL
- *out_inv_flattening*: Pointer to a value to store the inverse flattening. or NULL

PJ *proj_get_prime_meridian(PJ_CONTEXT *ctx, const PJ *obj)
Get the prime meridian of a CRS or a GeodeticReferenceFrame.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread at a time.

**Return** Object that must be unreferenced with proj_destroy(), or NULL in case of error.

**Parameters**
- *ctx*: PROJ context, or NULL for default context
- *obj*: Object of type CRS or GeodeticReferenceFrame (must not be NULL)

int proj_prime_meridian_get_parameters(PJ_CONTEXT *ctx, const PJ *prime_meridian, double *out_longitude, double *out_unit_conv_factor, const char **out_unit_name)

Return prime meridian parameters.

**Return** TRUE in case of success.

**Parameters**
- *ctx*: PROJ context, or NULL for default context
- *prime_meridian*: Object of type PrimeMeridian (must not be NULL)
• out_longitude: Pointer to a value to store the longitude of the prime meridian, in its native unit.
or NULL
• out_unit_conv_factor: Pointer to a value to store the conversion factor of the prime meridian
longitude unit to radian. or NULL
• out_unit_name: Pointer to a string value to store the unit name. or NULL

PJ *proj_crs_get_coordoperation(PJ_CONTEXT *ctx, const PJ *crs)

Return the Conversion of a DerivedCRS (such as a ProjectedCRS), or the Transformation from the baseCRS to
the hubCRS of a BoundCRS.

The returned object must be unreferenced with proj_destroy() after use. It should be used by at most one thread
at a time.

Return Object of type SingleOperation that must be unreferenced with proj_destroy(), or NULL in case of
error.

Parameters

• ctx: PROJ context, or NULL for default context
• crs: Object of type DerivedCRS or BoundCRSs (must not be NULL)

int proj_coordoperation_get_method_info(PJ_CONTEXT *ctx, const PJ *coordoperation,
const char **out_method_name, const char **out_method_auth_name,
const char **out_method_code)

Return information on the operation method of the SingleOperation.

Return TRUE in case of success.

Parameters

• ctx: PROJ context, or NULL for default context
• coordoperation: Object of type SingleOperation (typically a Conversion or Transformation)
(must not be NULL)
• out_method_name: Pointer to a string value to store the method (projection) name. or NULL
• out_method_auth_name: Pointer to a string value to store the method authority name. or NULL
• out_method_code: Pointer to a string value to store the method code. or NULL

int proj_coordoperation_is_instantiable(PJ_CONTEXT *ctx, const PJ *coordoperation)

Return whether a coordinate operation can be instantiated as a PROJ pipeline, checking in particular that refer-
enced grids are available.

Return TRUE or FALSE.

Parameters

• ctx: PROJ context, or NULL for default context
• coordoperation: Object of type CoordinateOperation or derived classes (must not be NULL)

int proj_coordoperation_has_ballpark_transformation(PJ_CONTEXT *ctx, const PJ
*coordoperation)

Return whether a coordinate operation has a “ballpark” transformation, that is a very approximate one, due to
lack of more accurate transformations.
Typically a null geographic offset between two horizontal datum, or a null vertical offset (or limited to unit changes) between two vertical datum. Errors of several tens to one hundred meters might be expected, compared to more accurate transformations.

**Return** TRUE or FALSE.

**Parameters**

- `ctx`: PROJ context, or NULL for default context
- `coordoperation`: Object of type CoordinateOperation or derived classes (must not be NULL)

```c
int proj_coordoperation_get_param_count (PJ_CONTEXT *ctx, const PJ *coordoperation)
```

Return the number of parameters of a SingleOperation.

**Parameters**

- `ctx`: PROJ context, or NULL for default context
- `coordoperation`: Object of type SingleOperation or derived classes (must not be NULL)

```c
int proj_coordoperation_get_param_index (PJ_CONTEXT *ctx, const PJ *coordoperation, const char *name)
```

Return the index of a parameter of a SingleOperation.

**Return** index (>=0), or -1 in case of error.

**Parameters**

- `ctx`: PROJ context, or NULL for default context
- `coordoperation`: Object of type SingleOperation or derived classes (must not be NULL)
- `name`: Parameter name. Must not be NULL

```c
int proj_coordoperation_get_param (PJ_CONTEXT *ctx, const PJ *coordoperation, int index, const char **out_name, const char **out_auth_name, const char **out_code, double *out_value, const char **out_value_string, double *out_unit_conv_factor, const char **out_unit_name, const char **out_unit_auth_name, const char **out_unit_code, const char **out_unit_category)
```

Return a parameter of a SingleOperation.

**Return** TRUE in case of success.

**Parameters**

- `ctx`: PROJ context, or NULL for default context
- `coordoperation`: Object of type SingleOperation or derived classes (must not be NULL)
- `index`: Parameter index.
- `out_name`: Pointer to a string value to store the parameter name. or NULL
- `out_auth_name`: Pointer to a string value to store the parameter authority name. or NULL
- `out_code`: Pointer to a string value to store the parameter code. or NULL
- `out_value`: Pointer to a double value to store the parameter value (if numeric). or NULL
• out_value_string: Pointer to a string value to store the parameter value (if of type string). or NULL
• out_unit_conv_factor: Pointer to a double value to store the parameter unit conversion factor. or NULL
• out_unit_name: Pointer to a string value to store the parameter unit name. or NULL
• out_unit_auth_name: Pointer to a string value to store the unit authority name. or NULL
• out_unit_code: Pointer to a string value to store the unit code. or NULL
• out_unit_category: Pointer to a string value to store the parameter name. or NULL. This value might be “unknown”, “none”, “linear”, “angular”, “scale”, “time” or “parametric”;

int proj_coordoperation_get_grid_used_count (PJ_CONTEXT *ctx, const PJ *coordoperation)
Return the number of grids used by a CoordinateOperation.

Parameters
• ctx: PROJ context, or NULL for default context
• coordoperation: Object of type CoordinateOperation or derived classes (must not be NULL)

int proj_coordoperation_get_grid_used (PJ_CONTEXT *ctx, const PJ *coordoperation, int index, const char **out_short_name, const char **out_full_name, const char **out_package_name, const char **out_url, int *out_direct_download, int *out_open_license, int *out_available)
Return a parameter of a SingleOperation.

Return TRUE in case of success.

Parameters
• ctx: PROJ context, or NULL for default context
• coordoperation: Object of type SingleOperation or derived classes (must not be NULL)
• index: Parameter index.
• out_short_name: Pointer to a string value to store the grid short name. or NULL
• out_full_name: Pointer to a string value to store the grid full filename. or NULL
• out_package_name: Pointer to a string value to store the package name where the grid might be found. or NULL
• out_url: Pointer to a string value to store the grid URL or the package URL where the grid might be found. or NULL
• out_direct_download: Pointer to a int (boolean) value to store whether *out_url can be downloaded directly. or NULL
• out_open_license: Pointer to a int (boolean) value to store whether the grid is released with an open license. or NULL
• out_available: Pointer to a int (boolean) value to store whether the grid is available at runtime. or NULL

double proj_coordoperation_get_accuracy (PJ_CONTEXT *ctx, const PJ *obj)
Return the accuracy (in metre) of a coordinate operation.

10.5. Reference
Return the accuracy, or a negative value if unknown or in case of error.

Parameters

- `ctx`: PROJ context, or NULL for default context
- `coordoperation`: Coordinate operation. Must not be NULL.

```c
int proj_coordoperation_get_towgs84_values(PJ_CONTEXT *ctx, const PJ *coordoperation, double *out_values, int value_count, int emit_error_if_incompatible)
```

Return the parameters of a Helmert transformation as WKT1 TOWGS84 values.

Return TRUE in case of success, or FALSE if coordoperation is not compatible with a WKT1 TOWGS84 representation.

Parameters

- `ctx`: PROJ context, or NULL for default context
- `coordoperation`: Object of type Transformation, that can be represented as a WKT1 TOWGS84 node (must not be NULL)
- `out_values`: Pointer to an array of value_count double values.
- `value_count`: Size of out_values array. The suggested size is 7 to get translation, rotation and scale difference parameters. Rotation and scale difference terms might be zero if the transformation only includes translation parameters. In that case, value_count could be set to 3.
- `emit_error_if_incompatible`: Boolean to indicate if an error must be logged if coordoperation is not compatible with a WKT1 TOWGS84 representation.

### 10.5.3 C++ API

#### 10.5.3.1 General documentation

```c
namespace general_api_design
```
General API design.

The design of the class hierarchy is strongly derived from ISO_19111_2019.

Classes for which the constructors are not directly accessible have their instances constructed with create() methods. The returned object is a non-null shared pointer. Such objects are immutable, and thread-safe.

```c
namespace general_properties
```
General properties.

All classes deriving from IdentifiedObject have general properties that can be defined at creation time. Those properties are:

- `osgeo::proj::metadata::Identifier::DESCRIPTION_KEY` ("description"): the natural language description of the meaning of the code value, provided as a string.
- `osgeo::proj::metadata::Identifier::CODE_KEY` ("code"): a numeric or alphanumeric code, provided as an integer or a string. For example 4326, for the EPSG:4326 "WGS84" GeographicalCRS
- `osgeo::proj::metadata::Identifier::CODESPACE_KEY` ("codespace"): the organization responsible for definition and maintenance of the code., provided as a string. For example "EPSG".
PROJ coordinate transformation software library, Release 6.1.1

- osgeo::proj::metadata::Identifier::VERSION_KEY ("version"): the version identifier for the namespace, provided as a string.
- osgeo::proj::metadata::Identifier::AUTHORITY_KEY ("authority"): a citation for the authority, provided as a string or an osgeo::proj::metadata::Citation object. Often unused.
- osgeo::proj::metadata::Identifier::URI_KEY ("uri"): the URI of the identifier, provided as a string. Often unused.
- osgeo::proj::common::IdentifiedObject::NAME_KEY ("name"): the name of an osgeo::proj::common::IdentifiedObject, provided as a string or osgeo::proj::metadata::IdentifierNNPtr.
- osgeo::proj::common::IdentifiedObject::IDENTIFIERS_KEY ("identifiers"): the identifier(s) of an osgeo::proj::common::IdentifiedObject, provided as osgeo::proj::common::IdentifierNNPtr or an osgeo::proj::util::ArrayOfBaseObjectNNPtr of osgeo::proj::metadata::IdentifierNNPtr.
- osgeo::proj::common::IdentifiedObject::ALIAS_KEY ("alias"): the alias(es) of an osgeo::proj::common::IdentifiedObject, provided as a string or osgeo::proj::util::GenericNameNNPtr or an osgeo::proj::util::ArrayOfBaseObjectNNPtr of osgeo::proj::util::GenericNameNNPtr.
- osgeo::proj::common::IdentifiedObject::REMARKS_KEY ("remarks"): the remarks of an osgeo::proj::common::IdentifiedObject, provided as a string.
- osgeo::proj::common::IdentifiedObject::DEPRECATED_KEY ("deprecated"): the deprecation flag of an osgeo::proj::common::IdentifiedObject, provided as a boolean.
- osgeo::proj::common::ObjectUsage::SCOPE_KEY ("scope"): the scope of an osgeo::proj::common::ObjectUsage, provided as a string.
- osgeo::proj::common::ObjectUsage::DOMAIN_OF_VALIDITY_KEY ("domainOfValidity"): the domain of validity of an osgeo::proj::common::ObjectUsage, provided as osgeo::proj::metadata::ExtentNNPtr.
- osgeo::proj::common::ObjectUsage::OBJECT_DOMAIN_KEY ("objectDomain"): the object domain(s) of an osgeo::proj::common::ObjectUsage, provided as an osgeo::proj::common::ObjectDomainNNPtr or an osgeo::proj::util::ArrayOfBaseObjectNNPtr of osgeo::proj::common::ObjectDomainNNPtr.

namespace standards  
Applicable standards.

namespace ISO_19111  

Topic 2 - Spatial referencing by coordinates.
This is an Abstract Specification describes the data elements, relationships and associated metadata required for spatial referencing by coordinates. It describes Coordinate Reference Systems (CRS), coordinate systems (CS) and coordinate transformation or coordinate conversion between two different coordinate reference systems.

namespace ISO_19111_2019  

This is the revision mostly used for PROJ C++ modelling.

OGC 18-005r4, 2019-02-08, ISO 19111:2019

namespace ISO_19111_2007  

The precedent version of the specification was: OGC 08-015r2, 2010-04-27, ISO 19111:2007

namespace WKT2  
WKT2 standard.

Well-known text representation of coordinate reference systems.

10.5. Reference
Well-known Text (WKT) offers a compact machine- and human-readable representation of the critical elements of coordinate reference system (CRS) definitions, and coordinate operations. This is an implementation of ISO_19111

PROJ implements the two following revisions of the standard:

```plaintext
namespace WKT2_2018  
  OGC 18-010r1, 2018-06-08, WKT2-2018 (not yet adopted, at time of writing)

namespace WKT2_2015  
  WKT2:2015.

namespace WKT1
  WKT1 specification.

Older specifications of well-known text representation of coordinate reference systems are also supported by PROJ, mostly for compatibility with legacy systems, or older versions of GDAL.

GDAL v2.3 and earlier mostly implements:

OGC 01-009, 2001-01-12, OpenGIS Coordinate Transformation Service Implementation Specification

The GDAL documentation, OGC WKT Coordinate System Issues discusses issues, and GDAL implementation choices.

An older specification of WKT1 is/was used by some software packages:

OGC 99-049, 1999-05-05, OpenGIS Simple Features Specification For SQL v1.1

namespace ISO_19115
  ISO 19115 (Metadata)

Defines the schema required for describing geographic information and services. It provides information about the identification, the extent, the quality, the spatial and temporal schema, spatial reference, and distribution of digital geographic data.

PROJ implements a simplified subset of ISO 19115.

namespace GeoAPI
  GeoAPI.

A set of Java and Python language programming interfaces for geospatial applications.

GeoAPI main page
GeoAPI Javadoc
OGC GeoAPI Implementation Specification

10.5.3.2 common namespace

namespace common
  Common classes.

  osgeo.proj.common namespace
**Typedefs**

```cpp
typedef std::shared_ptr<UnitOfMeasure> UnitOfMeasurePtr
Shared pointer of UnitOfMeasure.

typedef util::nn<UnitOfMeasurePtr> UnitOfMeasureNNPtr
Non-null shared pointer of UnitOfMeasure.

typedef std::shared_ptr<IdentifiedObject> IdentifiedObjectPtr
Shared pointer of IdentifiedObject.

typedef util::nn<IdentifiedObjectPtr> IdentifiedObjectNNPtr
Non-null shared pointer of IdentifiedObject.

using ObjectDomainPtr = std::shared_ptr<ObjectDomain>
Shared pointer of ObjectDomain.

using ObjectDomainNNPtr = util::nn<ObjectDomainPtr>
Non-null shared pointer of ObjectDomain.

using ObjectUsagePtr = std::shared_ptr<ObjectUsage>
Shared pointer of ObjectUsage.

using ObjectUsageNNPtr = util::nn<ObjectUsagePtr>
Non-null shared pointer of ObjectUsage.
```

**class Angle:**

```cpp
#include <common.hpp> Numeric value, with a angular unit of measure.

**Public Functions**

```cpp
Angle (double valueIn = 0.0)
Instantiate a Angle.

Parameters

- valueIn: value

Angle (double valueIn, const UnitOfMeasure &unitIn)
Instantiate a Angle.

Parameters

- valueIn: value
- unitIn: unit. Constraint: unit.type() == UnitOfMeasure::Type::ANGULAR
```

**class DataEpoch**

```cpp
#include <common.hpp> Data epoch.

**Public Functions**

```cpp
const Measure &coordinateEpoch () const
Return the coordinate epoch, as a measure in decimal year.

**class DateTime**

```cpp
#include <common.hpp> Date-time value, as a ISO:8601 encoded string, or other string encoding.
Public Functions

bool isISO_8601() const
Return whether the DateTime is ISO:8601 compliant.

Remark The current implementation is really simplistic, and aimed at detecting date-times that are
not ISO:8601 compliant.

std::string toString() const
Return the DateTime as a string.

Public Static Functions

DateTime create(const std::string &str)
Instantiate a DateTime.

class IdentifiedObject : public osgeo::proj::util::BaseObject, public osgeo::proj::IComparable, public osgeo::proj::io::IWKTExportable
#include <common.hpp> Abstract class representing a CRS-related object that has an identification.

Remark Implements IdentifiedObject from ISO_19111_2019

Subclassed by osgeo::proj::common::ObjectUsage, osgeo::proj::cs::CoordinateSystem, osgeo::proj::cs::CoordinateSystemAxis, osgeo::proj::cs::Meridian, osgeo::proj::datum::DatumEnsemble, osgeo::proj::datum::Ellipsoid, osgeo::proj::datum::PrimeMeridian, osgeo::proj::operation::GeneralOperationParameter, osgeo::proj::operation::OperationMethod

Public Functions

const IdentifierNNPtr &name()
Return the name of the object.

Generally, the only interesting field of the name will be name()->description().

const std::string &nameStr()
Return the name of the object.

Return *(name()->description())

const std::vector<IdentifierNNPtr> &identifiers()
Return the identifier(s) of the object.

Generally, those will have Identifier::code() and Identifier::codeSpace() filled.

const std::vector<GenericNameNNPtr> &aliases()
Return the alias(es) of the object.

const std::string &remarks()
Return the remarks.

bool is Deprecated()
Return whether the object is deprecated.

Remark Extension of ISO_19111_2019
std::string alias ()
    Return the (first) alias of the object as a string.
    Shortcut for aliases()[0]->fullyQualifiedNames()->toString()

int getEPSGCode ()
    Return the EPSG code.
    Return code, or 0 if not found

Public Static Attributes

const std::string NAME_KEY
    Key to set the name of a common::IdentifiedObject.
    The value is to be provided as a string or metadata::IdentifierNNPtr.

const std::string IDENTIFIERS_KEY
    Key to set the identifier(s) of a common::IdentifiedObject.
    The value is to be provided as a common::IdentifierNNPtr or a util::ArrayOfBaseObjectNNPtr of common::IdentifierNNPtr.

const std::string ALIAS_KEY
    Key to set the alias(es) of a common::IdentifiedObject.
    The value is to be provided as string, a util::GenericNameNNPtr or a util::ArrayOfBaseObjectNNPtr of util::GenericNameNNPtr.

const std::string REMARKS_KEY
    Key to set the remarks of a common::IdentifiedObject.
    The value is to be provided as a string.

const std::string DEPRECATED_KEY
    Key to set the deprecation flag of a common::IdentifiedObject.
    The value is to be provided as a boolean.

class Length : public osgeo::proj::common::Measure
    #include <common.hpp> Numeric value, with a linear unit of measure.

Public Functions

Length (double valueIn = 0.0)
    Instantiate a Length.
    Parameters
        • valueIn: value

Length (double valueIn, const UnitOfMeasure &unitIn)
    Instantiate a Length.
    Parameters
        • valueIn: value
        • unitIn: unit. Constraint: unit.type() == UnitOfMeasure::Type::LINEAR

class Measure : public osgeo::proj::util::BaseObject
    #include <common.hpp> Numeric value associated with a UnitOfMeasure.
    Subclassed by osgeo::proj::common::Angle, osgeo::proj::common::Length, osgeo::proj::common::Scale
Public Functions

**Measure** (double `valueIn = 0.0`, const `UnitOfMeasure &unitIn = UnitOfMeasure()`)  
Instantiate a Measure.

const `UnitOfMeasure &unit()`  
Return the unit of the Measure.

double `getSIValue()`  
Return the value of the Measure, after conversion to the corresponding unit of the International System.

double `value()`  
Return the value of the measure, expressed in the `unit()`

double `convertToUnit` (const `UnitOfMeasure &otherUnit`)  
Return the value of this measure expressed into the provided unit.

bool `operator==` (const `Measure &other`)  
Return whether two measures are equal.  
The comparison is done both on the value and the unit.

bool `_isEqualTo` (const `Measure &other`, util::IComparable::Criterion `criterion = util::IComparable::Criterion::STRICT`, double `maxRelativeError = DEFAULT_MAX_REL_ERROR`) const  
Returns whether an object is equivalent to another one.

    Return true if objects are equivalent.
    Parameters
    • `other`: other object to compare to
    • `criterion`: comparaison criterion.
    • `maxRelativeError`: Maximum relative error allowed.

Public Static Attributes

constexpr double `DEFAULT_MAX_REL_ERROR` = 1e-10  
Default maximum resulative error.

class `ObjectDomain` : public `osgeo::proj::util::BaseObject`, public `osgeo::proj::util::IComparable`  
#include `<common.hpp>` The scope and validity of a CRS-related object.

Remark  Implements `ObjectDomain` from `ISO_19111_2019`

Public Functions

const optional<std::string> &`scope` ()  
Return the scope.

    Return the scope, or empty.

const `ExtentPtr &domainOfValidity` ()  
Return the domain of validity.

    Return the domain of validity, or nullptr.
Public Static Functions

```cpp
ObjectDomainNNPtr create (const util::optional<std::string> &scopeIn, const metaData::ExtentPtr &extent)
```

Instantiate a `ObjectDomain`.

**class ObjectUsage : public osgeo::proj::common::IdentifiedObject**

#include <common.hpp> Abstract class of a CRS-related object that has usages.

**Remark** Implements `ObjectUsage` from ISO_19111_2019

Subclassed by osgeo::proj::crs::CRS, osgeo::proj::datum::Datum, osgeo::proj::operation::CoordinateOperation

**Public Functions**

```cpp
const std::vector<ObjectDomainNNPtr> &domains ()
```

Return the domains of the object.

**Public Static Attributes**

```cpp
const std::string SCOPE_KEY
```

Key to set the scope of a `common::ObjectUsage`.

The value is to be provided as a string.

```cpp
const std::string DOMAIN_OF_VALIDITY_KEY
```

Key to set the domain of validity of a `common::ObjectUsage`.

The value is to be provided as a `common::ExtentNNPtr`.

```cpp
const std::string OBJECT_DOMAIN_KEY
```

Key to set the object domain(s) of a `common::ObjectUsage`.

The value is to be provided as a `common::ObjectDomainNNPtr` or a `util::ArrayOfBaseObjectNNPtr` of `common::ObjectDomainNNPtr`.

**class Scale : public osgeo::proj::common::Measure**

#include <common.hpp> Numeric value, without a physical unit of measure.

**Public Functions**

```cpp
Scale (double valueIn = 0.0)
```

Instantiate a `Scale`.

**Parameters**

- `valueIn`: value

```cpp
Scale (double valueIn, const UnitOfMeasure &unitIn)
```

Instantiate a `Scale`.

**Parameters**

- `valueIn`: value
- `unitIn`: unit. Constraint: `unit.type() == UnitOfMeasure::Type::SCALE`
class UnitOfMeasure : public osgeo::proj::util::BaseObject
#include <common.hpp> Unit of measure.

This is a mutable object.

**Public Types**

```cpp
enum Type
Type of unit of measure.

Values:

UNKNOWN
Unknown unit of measure

NONE
No unit of measure

ANGULAR
Angular unit of measure

LINEAR
Linear unit of measure

SCALE
Scale unit of measure

TIME
Time unit of measure

PARAMETRIC
Parametric unit of measure
```

**Public Functions**

```cpp
UnitOfMeasure(const std::string &nameIn = std::string(), double toSIIn = 1.0, Type typeIn = Type::UNKNOWN, const std::string &codeSpaceIn = std::string(), const std::string &codeIn = std::string())

Creates a UnitOfMeasure.

const std::string &name()  
Return the name of the unit of measure.

double conversionToSI()  
Return the conversion factor to the unit of the International System of Units of the same Type.

For example, for foot, this would be 0.3048 (metre)

Return the conversion factor, or 0 if no conversion exists.
```

```cpp
UnitOfMeasure::Type type()  
Return the type of the unit of measure.

const std::string &codeSpace()  
Return the code space of the unit of measure.

For example “EPSG”

Return the code space, or empty string.
const std::string &code ()
    Return the code of the unit of measure.
    
    Return the code, or empty string.

bool operator== (const UnitOfMeasure &other)
    Returns whether two units of measures are equal.
    The comparison is based on the name.

bool operator!= (const UnitOfMeasure &other)
    Returns whether two units of measures are different.
    The comparison is based on the name.

Public Static Attributes

const UnitOfMeasure NONE
    “Empty”/”None”, unit of measure of type NONE.

const UnitOfMeasure SCALE_UNITY
    Scale unity, unit of measure of type SCALE.

const UnitOfMeasure PARTS_PER_MILLION
    Parts-per-million, unit of measure of type SCALE.

const UnitOfMeasure PPM_PER_YEAR
    Part-per-million per year, unit of measure of type SCALE.

const UnitOfMeasure METRE
    Metre, unit of measure of type LINEAR (SI unit).

const UnitOfMeasure METRE_PER_YEAR
    Metre per year, unit of measure of type LINEAR.

const UnitOfMeasure RADIAN
    Radian, unit of measure of type ANGULAR (SI unit).

const UnitOfMeasure MICRORADIAN
    Microradian, unit of measure of type ANGULAR.

const UnitOfMeasure DEGREE
    Degree, unit of measure of type ANGULAR.

const UnitOfMeasure ARC_SECOND
    Arc-second, unit of measure of type ANGULAR.

const UnitOfMeasure GRAD
    Grad, unit of measure of type ANGULAR.

const UnitOfMeasure ARC_SECOND_PER_YEAR
    Arc-second per year, unit of measure of type ANGULAR.

const UnitOfMeasure SECOND
    Second, unit of measure of type TIME (SI unit).

const UnitOfMeasure YEAR
    Year, unit of measure of type TIME.
10.5.3.3 util namespace

namespace util
A set of base types from ISO 19103, GeoAPI and other PROJ specific classes.
 easy-proj::util namespace.

Typedefs

using BaseObjectPtr = std::shared_ptr<BaseObject>
    Shared pointer of BaseObject.

using BoxedValuePtr = std::shared_ptr<BoxedValue>
    Shared pointer of BoxedValue.

using BoxedValueNNPtr = util::nn<BoxedValuePtr>
    Non-null shared pointer of BoxedValue.

using ArrayOfBaseObjectPtr = std::shared_ptr<ArrayOfBaseObject>
    Shared pointer of ArrayOfBaseObject.

using ArrayOfBaseObjectNNPtr = util::nn<ArrayOfBaseObjectPtr>
    Non-null shared pointer of ArrayOfBaseObject.

using LocalNamePtr = std::shared_ptr<LocalName>
    Shared pointer of LocalName.

using LocalNameNNPtr = util::nn<LocalNamePtr>
    Non-null shared pointer of LocalName.

using NameSpacePtr = std::shared_ptr<NameSpace>
    Shared pointer of NameSpace.

using NameSpaceNNPtr = util::nn<NameSpacePtr>
    Non-null shared pointer of NameSpace.

using GenericNamePtr = std::shared_ptr<GenericName>
    Shared pointer of GenericName.

using GenericNameNNPtr = util::nn<GenericNamePtr>
    Non-null shared pointer of GenericName.

class ArrayOfBaseObject : public osgeo::proj::util::BaseObject
    #include <util.hpp> Array of BaseObject.

Public Functions

void add (const BaseObjectNNPtr &obj)
    Adds an object to the array.

Parameters
    • obj: the object to add.
Public Static Functions

ArrayOfBaseObjectNNPtr create()  
Instantiate a ArrayOfBaseObject.

Return a new ArrayOfBaseObject.

class BaseObject  
#include <util.hpp>  
Class that can be derived from, to emulate Java’s Object behaviour.

Subclassed by osgeo::proj::common::IdentifiedObject, osgeo::proj::common::Measure, osgeo::proj::common::ObjectDomain, osgeo::proj::common::UnitOfMeasure, osgeo::proj::metadata::Citation, osgeo::proj::metadata::Extent, osgeo::proj::metadata::GeographicExtent, osgeo::proj::metadata::Identifier, osgeo::proj::metadata::PositionalAccuracy, osgeo::proj::metadata::TemporalExtent, osgeo::proj::metadata::VerticalExtent, osgeo::proj::operation::GeneralParameterValue, osgeo::proj::operation::ParameterValue, osgeo::proj::util::ArrayOfBaseObject, osgeo::proj::util::BoxedValue, osgeo::proj::util::GenericName

struct BaseObjectNNPtr: public util::nn<BaseObjectPtr>  
#include <util.hpp>  
Non-null shared pointer of BaseObject.

class BoxedValue: public osgeo::proj::util::BaseObject  
#include <util.hpp>  
Encapsulate standard datatypes in an object.

Public Functions

BoxedValue(const char *stringValueIn)  
Constructs a BoxedValue from a string.

BoxedValue(const std::string &stringValueIn)  
Constructs a BoxedValue from a string.

BoxedValue(int integerValueIn)  
Constructs a BoxedValue from an integer.

BoxedValue(bool booleanValueIn)  
Constructs a BoxedValue from a boolean.

class CodeList  
#include <util.hpp>  
Abstract class to define an enumeration of values.

Subclassed by osgeo::proj::cs::AxisDirection, osgeo::proj::datum::RealizationMethod

Public Functions

const std::string &toString()  
Return the CodeList item as a string.

operator std::string()  
Return the CodeList item as a string.

class Exception: public exception  
#include <util.hpp>  
Root exception class.

Subclassed by osgeo::proj::io::FactoryException, osgeo::proj::io::FormattingException, osgeo::proj::io::ParsingException, osgeo::proj::operation::InvalidOperation, osgeo::proj::util::InvalidValueTypeException, osgeo::proj::util::UnsupportedOperationException
Public Functions

```c
const char *what() const
Return the exception text.
```

class GenericName : public osgeo::proj::util::BaseObject
#include <util.hpp>
A sequence of identifiers rooted within the context of a namespace.

Remark  Simplified version of GenericName from GeoAPI

Subclassed by osgeo::proj::util::LocalName

Public Functions

```c
virtual const NameSpacePtr scope() const = 0
Return the scope of the object, possibly a global one.
```

```c
virtual std::string toString() const = 0
Return the LocalName as a string.
```

```c
virtual GenericNameNNPtr toFullyQualifiedName() const = 0
Return a fully qualified name corresponding to the local name.
The namespace of the resulting name is a global one.
```

class IComparable
#include <util.hpp>
Interface for an object that can be compared to another.

Subclassed by osgeo::proj::common::IdentifiedObject, osgeo::proj::common::ObjectDomain, osgeo::proj::metadata::Extent, osgeo::proj::metadata::GeographicExtent, osgeo::proj::metadata::TemporalExtent, osgeo::proj::metadata::VerticalExtent, osgeo::proj::operation::GeneralParameterValue, osgeo::proj::operation::ParameterValue

Public Types

```c
enum Criterion
Comparison criterion.

Values:

STRICT
All properties are identical.

EQUIVALENT
The objects are equivalent for the purpose of coordinate operations. They can differ by the name of their objects, identifiers, other metadata. Parameters may be expressed in different units, provided that the value is (with some tolerance) the same once expressed in a common unit.

EQUIVALENT_EXCEPT_AXIS_ORDER_GEOGCRS
Same as EQUIVALENT, relaxed with an exception that the axis order of the base CRS of a DerivedCRS/ProjectedCRS or the axis order of a GeographicCRS is ignored. Only to be used with DerivedCRS/ProjectedCRS/GeographicCRS
```
Public Functions

bool isEquivalentTo(const IComparable *other, Criterion criterion = Criterion::STRICT)

  Returns whether an object is equivalent to another one.

Parameters
  • other: other object to compare to
  • criterion: comparaison criterion.

class InvalidValueTypeException : public osgeo::proj::util::Exception

#include <util.hpp> Exception thrown when an invalid value type is set as the value of a key of a PropertyMap.

class LocalName : public osgeo::proj::util::GenericName

#include <util.hpp> Identifier within a NameSpace for a local object.

Local names are names which are directly accessible to and maintained by a NameSpace within which they are local, indicated by the scope.

Remark  Simplified version of LocalName from GeoAPI

Public Functions

const NameSpacePtr scope () const

  Return the scope of the object, possibly a global one.

std::string toString () const

  Return the LocalName as a string.

GenericNameNNPtr toFullyQualifiedName () const

  Return a fully qualified name corresponding to the local name.

  The namespace of the resulting name is a global one.

class NameFactory

#include <util.hpp> Factory for generic names.

Remark  Simplified version of NameFactory from GeoAPI

Public Static Functions

NameSpaceNNPtr createNameSpace(const GenericNameNNPtr &name, const PropertyMap &properties)

  Instantiate a NameSpace.

  Return a new NameFactory.

Parameters
  • name: name of the namespace.
  • properties: Properties. Allowed keys are “separator” and “separator.head”.

LocalStorageNNPtr createLocalName(const NameSpacePtr &scope, const std::string &name)

  Instantiate a LocalName.

  Return a new LocalName.
GenericNameNNPtr createGenericName(const NameSpacePtr &scope, const std::vector<std::string> &parsedNames)

Instantiate a GenericName.

Return a new GenericName.

Parameters
• scope: scope.
• parsedNames: the components of the name.

class NameSpace
#include <util.hpp> A domain in which names given by strings are defined.

Remark Simplified version of NameSpace from GeoAPI

Public Functions

bool isGlobal () const
Returns whether this is a global namespace.

const GenericNamePtr &name () const
Returns the name of this namespace.

template<class T>
class optional
#include <util.hpp> Loose transposition of std::optional available from C++17.

Public Functions

const T *operator-> () const
Returns a pointer to the contained value.

const T &operator* () const
Returns a reference to the contained value.

operator bool () const
Return whether the optional has a value

bool has_value () const
Return whether the optional has a value

class PropertyMap
#include <util.hpp> Wrapper of a std::map<std::string, BaseObjectNNPtr>
Public Functions

PropertyMap &set (const std::string &key, const BaseObjectNNPtr &val)
Set a BaseObjectNNPtr as the value of a key.

PropertyMap &set (const std::string &key, const char *val)
Set a string as the value of a key.

PropertyMap &set (const std::string &key, const std::string &val)
Set a string as the value of a key.

PropertyMap &set (const std::string &key, int val)
Set an integer as the value of a key.

PropertyMap &set (const std::string &key, bool val)
Set a boolean as the value of a key.

PropertyMap &set (const std::string &key, const std::vector<std::string> &array)
Set a vector of strings as the value of a key.

class UnsupportedOperationException : public osgeo::proj::util::Exception
#include <util.hpp> Exception Thrown to indicate that the requested operation is not supported.

10.5.3.4 metadata namespace

namespace metadata
Common classes from ISO_19115 standard.

osgeo.proj.metadata namespace

Typedefs

typedef std::shared_ptr<Extent> ExtentPtr
Shared pointer of Extent.

typedef util::nn<ExtentPtr> ExtentNNPtr
Non-null shared pointer of Extent.

using GeographicExtentPtr = std::shared_ptr<GeographicExtent>
Shared pointer of GeographicExtent.

using GeographicExtentNNPtr = util::nn<GeographicExtentPtr>
Non-null shared pointer of GeographicExtent.

using GeographicBoundingBoxPtr = std::shared_ptr<GeographicBoundingBox>
Shared pointer of GeographicBoundingBox.

using GeographicBoundingBoxNNPtr = util::nn<GeographicBoundingBoxPtr>
Non-null shared pointer of GeographicBoundingBox.

using TemporalExtentPtr = std::shared_ptr<TemporalExtent>
Shared pointer of TemporalExtent.

using TemporalExtentNNPtr = util::nn<TemporalExtentPtr>
Non-null shared pointer of TemporalExtent.

using VerticalExtentPtr = std::shared_ptr<VerticalExtent>
Shared pointer of VerticalExtent.
using VerticalExtentNNPtr = util::nn<VerticalExtentPtr>
Non-null shared pointer of VerticalExtent.

using IdentifierPtr = std::shared_ptr<Identifier>
Shared pointer of Identifier.

using IdentifierNNPtr = util::nn<IdentifierPtr>
Non-null shared pointer of Identifier.

using PositionalAccuracyPtr = std::shared_ptr<PositionalAccuracy>
Shared pointer of PositionalAccuracy.

using PositionalAccuracyNNPtr = util::nn<PositionalAccuracyPtr>
Non-null shared pointer of PositionalAccuracy.

class Citation : public osgeo::proj::BaseObject
#include <metadata.hpp> Standardized resource reference.

Local names are names which are directly accessible to and maintained by a NameSpace within which they are local, indicated by the scope.

**Remark** Simplified version of Citation from GeoAPI

**Public Functions**

**Citation** (const std::string &titleIn)
Constructs a citation by its title.

const optional<std::string> &title ()
Returns the name by which the cited resource is known.

class Extent : public osgeo::proj::BaseObject, public osgeo::proj::IComparable
#include <metadata.hpp> Information about spatial, vertical, and temporal extent.

**Remark** Simplified version of Extent from GeoAPI

**Public Functions**

const optional<std::string> &description ()
Return a textual description of the extent.

Return the description, or empty.

const std::vector<GeographicExtentNNPtr> &geographicElements ()
Return the geographic element(s) of the extent

Return the geographic element(s), or empty.

const std::vector<TemporalExtentNNPtr> &temporalElements ()
Return the temporal element(s) of the extent

Return the temporal element(s), or empty.

const std::vector<VerticalExtentNNPtr> &verticalElements ()
Return the vertical element(s) of the extent

Return the vertical element(s), or empty.
bool contains (const ExtentNNPtr &other) const
   Returns whether this extent contains the other one.
   Behaviour only well specified if each sub-extent category as at most one element.

bool intersects (const ExtentNNPtr &other) const
   Returns whether this extent intersects the other one.
   Behaviour only well specified if each sub-extent category as at most one element.

ExtentPtr intersection (const ExtentNNPtr &other) const
   Returns the intersection of this extent with another one.
   Behaviour only well specified if there is one single GeographicExtent in each object. Returns nullptr otherwise.

Public Static Functions

ExtentNNPtr create (const util::optional<std::string> &descriptionIn, const std::vector<GeographicExtentNNPtr> &geographicElementsIn, const std::vector<VerticalExtentNNPtr> &verticalElementsIn, const std::vector<TemporalExtentNNPtr> &temporalElementsIn)
   Instantiate a Extent.
   Return a new Extent.
   Parameters
       • descriptionIn: Textual description, or empty.
       • geographicElementsIn: Geographic element(s), or empty.
       • verticalElementsIn: Vertical element(s), or empty.
       • temporalElementsIn: Temporal element(s), or empty.

ExtentNNPtrcreateFromBBOX (double west, double south, double east, double north, const util::optional<std::string> &descriptionIn = util::optional<std::string>())
   Instantiate a Extent from a bounding box.
   Return a new Extent.
   Parameters
       • west: Western-most coordinate of the limit of the dataset extent (in degrees).
       • south: Southern-most coordinate of the limit of the dataset extent (in degrees).
       • east: Eastern-most coordinate of the limit of the dataset extent (in degrees).
       • north: Northern-most coordinate of the limit of the dataset extent (in degrees).
       • descriptionIn: Textual description, or empty.

Public Static Attributes

const ExtentNNPtr WORLD
   World extent.

class GeographicBoundingBox : public osgeo::proj::metadata::GeographicExtent
#include <metadata.hpp> Geographic position of the dataset.
   This is only an approximate so specifying the co-ordinate reference system is unnecessary.

Remark Implements GeographicBoundingBox from GeoAPI
**Public Functions**

double *westBoundLongitude* ()
   Returns the western-most coordinate of the limit of the dataset extent.
   The unit is degrees.
   If eastBoundLongitude < westBoundLongitude(), then the bounding box crosses the anti-meridian.

double *southBoundLatitude* ()
   Returns the southern-most coordinate of the limit of the dataset extent.
   The unit is degrees.

double *eastBoundLongitude* ()
   Returns the eastern-most coordinate of the limit of the dataset extent.
   The unit is degrees.
   If eastBoundLongitude < westBoundLongitude(), then the bounding box crosses the anti-meridian.

double *northBoundLatitude* ()
   Returns the northern-most coordinate of the limit of the dataset extent.
   The unit is degrees.

bool *contains* (const GeographicExtentNNPtr &other) const
   Returns whether this extent contains the other one.

bool *intersects* (const GeographicExtentNNPtr &other) const
   Returns whether this extent intersects the other one.

GeographicExtentPtr *intersection* (const GeographicExtentNNPtr &other) const
   Returns the intersection of this extent with another one.

**Public Static Functions**

GeographicBoundingBoxNNPtr *create* (double *west*, double *south*, double *east*, double *north*)
   Instantiate a GeographicBoundingBox.
   If east < west, then the bounding box crosses the anti-meridian.

   Return a new GeographicBoundingBox.

Parameters

- *west*: Western-most coordinate of the limit of the dataset extent (in degrees).
- *south*: Southern-most coordinate of the limit of the dataset extent (in degrees).
- *east*: Eastern-most coordinate of the limit of the dataset extent (in degrees).
- *north*: Northern-most coordinate of the limit of the dataset extent (in degrees).

**class GeographicExtent : public** osgeo::proj::util::BaseObject, public osgeo::proj::util::IComparable #include <metadata.hpp> Base interface for geographic area of the dataset.

Remark Simplified version of GeographicExtent from GeoAPI

Subclassed by osgeo::proj::metadata::GeographicBoundingBox
**Public Functions**

```cpp
virtual bool contains (const GeographicExtentNNPtr &other) const = 0
```
Returns whether this extent contains the other one.

```cpp
virtual bool intersects (const GeographicExtentNNPtr &other) const = 0
```
Returns whether this extent intersects the other one.

```cpp
virtual GeographicExtentPtr intersection (const GeographicExtentNNPtr &other) const = 0
```
Returns the intersection of this extent with another one.

**class Identifier :** public osgeo::proj::util::BaseObject, public osgeo::proj::io::IWKTExportable

`#include <metadata.hpp>`

Value uniquely identifying an object within a namespace.

**Remark** Implements `Identifier` as described in `ISO_19111_2019` but which originates from `ISO_19115`

**Public Functions**

```cpp
const optional<Citation> &authority ()
```
Return a citation for the organization responsible for definition and maintenance of the code.

Return the citation for the authority, or empty.

```cpp
const std::string &code ()
```
Return the alphanumeric value identifying an instance in the codespace.

e.g. “4326” (for EPSG:4326 WGS 84 GeographicCRS)

Return the code.

```cpp
const optional<std::string> &codeSpace ()
```
Return the organization responsible for definition and maintenance of the code.

E.g “EPSG”

Return the authority codespace, or empty.

```cpp
const optional<std::string> &version ()
```
Return the version identifier for the namespace.

When appropriate, the edition is identified by the effective date, coded using ISO 8601 date format.

Return the version or empty.

```cpp
const optional<std::string> &description ()
```
Return the natural language description of the meaning of the code value.

Return the description or empty.

```cpp
const optional<std::string> &uri ()
```
Return the URI of the identifier.

Return the URI or empty.
Public Static Functions

`IdentifierNNPtr create(const std::string &codeIn = std::string(), const util::PropertyMap &properties = util::PropertyMap())`

Instantiate a `Identifier`.

Return a new `Identifier`.

Parameters
- `codeIn`: Alphanumeric value identifying an instance in the codespace
- `properties`: See `general_properties`. Generally, the `Identifier::CODESPACE_KEY` should be set.

`bool isEquivalentName(const char *a, const char *b)`

Returns whether two names are considered equivalent.

Two names are equivalent by removing any space, underscore, dash, slash, { or } character from them, and comparing in a case insensitive way.

Public Static Attributes

`const std::string AUTHORITY_KEY`

Key to set the authority citation of a `metadata::Identifier`.

The value is to be provided as a string or a `metadata::Citation`.

`const std::string CODE_KEY`

Key to set the code of a `metadata::Identifier`.

The value is to be provided as an integer or a string.

`const std::string CODESPACE_KEY`

Key to set the organization responsible for definition and maintenance of the code of a `metadata::Identifier`.

The value is to be provided as a string.

`const std::string VERSION_KEY`

Key to set the version identifier for the namespace of a `metadata::Identifier`.

The value is to be provided as a string.

`const std::string DESCRIPTION_KEY`

Key to set the natural language description of the meaning of the code value of a `metadata::Identifier`.

The value is to be provided as a string.

`const std::string URI_KEY`

Key to set the URI of a `metadata::Identifier`.

The value is to be provided as a string.

`const std::string EPSG`

EPSG codespace.

`const std::string OGC`

OGC codespace.

class `PositionalAccuracy`: public osgeo::proj::util::BaseObject

#include `<metadata.hpp>` Accuracy of the position of features.

Remark Simplified version of `PositionalAccuracy` from `GeoAPI`, which originates from `ISO_19115`
**Public Functions**

```cpp
const std::string & value ()
    Return the value of the positional accuracy.
```

**Public Static Functions**

```cpp
PositionalAccuracyNNPtr create (const std::string & valueIn)
    Instantiate a PositionalAccuracy.

Parameters
    • valueIn: positional accuracy value.
```

```cpp
class TemporalExtent : public osgeo::proj::util::BaseObject, public osgeo::proj::util::IComparable
    include <metadata.hpp> Time period covered by the content of the dataset.
```

**Remark** Simplified version of TemporalExtent from GeoAPI

**Public Functions**

```cpp
const std::string & start ()
    Returns the start of the temporal extent.

const std::string & stop ()
    Returns the end of the temporal extent.
```

```cpp
bool contains (const TemporalExtentNNPtr & other) const
    Returns whether this extent contains the other one.

bool intersects (const TemporalExtentNNPtr & other) const
    Returns whether this extent intersects the other one.
```

**Public Static Functions**

```cpp
TemporalExtentNNPtr create (const std::string & start, const std::string & stop)
    Instantiate a TemporalExtent.

Parameters
    • start: start.
    • stop: stop.
```

```cpp
class VerticalExtent : public osgeo::proj::util::BaseObject, public osgeo::proj::util::IComparable
    include <metadata.hpp> Vertical domain of dataset.
```

**Remark** Simplified version of VerticalExtent from GeoAPI
**Public Functions**

double `minimumValue()`  
Returns the minimum of the vertical extent.

double `maximumValue()`  
Returns the maximum of the vertical extent.

`common::UnitOfMeasureNNPtr &unit()`  
Returns the unit of the vertical extent.

bool `contains(const VerticalExtentNNPtr &other) const`  
Returns whether this extent contains the other one.

bool `intersects(const VerticalExtentNNPtr &other) const`  
Returns whether this extent intersects the other one.

**Public Static Functions**

`VerticalExtentNNPtr create(double minimumValue, double maximumValue, const common::UnitOfMeasureNNPtr &unitIn)`  
Instantiate a `VerticalExtent`.  
Return a new `VerticalExtent`.  
Parameters
  - `minimumIn`: minimum.  
  - `maximumIn`: maximum.  
  - `unitIn`: unit.

### 10.5.3.5 cs namespace

```cpp
namespace cs
 Coordinate systems and their axis.
```

```cpp
osgeo.proj.cs namespace
```

**Typedefs**

```cpp
using MeridianPtr = std::shared_ptr<Meridian>  
Shared pointer of `Meridian`.
```

```cpp
using MeridianNNPtr = util::nn<MeridianPtr>  
Non-null shared pointer of `Meridian`.
```

```cpp
using CoordinateSystemAxisPtr = std::shared_ptr<CoordinateSystemAxis>  
Shared pointer of `CoordinateSystemAxis`.
```

```cpp
using CoordinateSystemAxisNNPtr = util::nn<CoordinateSystemAxisPtr>  
Non-null shared pointer of `CoordinateSystemAxis`.
```

```cpp
typedef std::shared_ptr<CoordinateSystem> CoordinateSystemPtr  
Shared pointer of `CoordinateSystem`.
```

```cpp
typedef util::nn<CoordinateSystemPtr> CoordinateSystemNNPtr  
Non-null shared pointer of `CoordinateSystem`.
```
using SphericalCSPtr = std::shared_ptr<SphericalCS>
    Shared pointer of SphericalCS.

using SphericalCSNNPtr = util::nn<SphericalCSPtr>
    Non-null shared pointer of SphericalCS.

using EllipsoidalCSPtr = std::shared_ptr<EllipsoidalCS>
    Shared pointer of EllipsoidalCS.

using EllipsoidalCSNNPtr = util::nn<EllipsoidalCSPtr>
    Non-null shared pointer of EllipsoidalCS.

using VerticalCSPtr = std::shared_ptr<VerticalCS>
    Shared pointer of VerticalCS.

using VerticalCSNNPtr = util::nn<VerticalCSPtr>
    Non-null shared pointer of VerticalCS.

using CartesianCSPtr = std::shared_ptr<CartesianCS>
    Shared pointer of CartesianCS.

using CartesianCSNNPtr = util::nn<CartesianCSPtr>
    Non-null shared pointer of CartesianCS.

using OrdinalCSPtr = std::shared_ptr<OrdinalCS>
    Shared pointer of OrdinalCS.

using OrdinalCSNNPtr = util::nn<OrdinalCSPtr>
    Non-null shared pointer of OrdinalCS.

using ParametricCSPtr = std::shared_ptr<ParametricCS>
    Shared pointer of ParametricCS.

using ParametricCSNNPtr = util::nn<ParametricCSPtr>
    Non-null shared pointer of ParametricCS.

using TemporalCSPtr = std::shared_ptr<TemporalCS>
    Shared pointer of TemporalCS.

using TemporalCSNNPtr = util::nn<TemporalCSPtr>
    Non-null shared pointer of TemporalCS.

using DateTimeTemporalCSPtr = std::shared_ptr<DateTimeTemporalCS>
    Shared pointer of DateTimeTemporalCS.

using DateTimeTemporalCSNNPtr = util::nn<DateTimeTemporalCSPtr>
    Non-null shared pointer of DateTimeTemporalCS.

using TemporalCountCSPtr = std::shared_ptr<TemporalCountCS>
    Shared pointer of TemporalCountCS.

using TemporalCountCSNNPtr = util::nn<TemporalCountCSPtr>
    Non-null shared pointer of TemporalCountCS.

using TemporalMeasureCSPtr = std::shared_ptr<TemporalMeasureCS>
    Shared pointer of TemporalMeasureCS.

using TemporalMeasureCSNNPtr = util::nn<TemporalMeasureCSPtr>
    Non-null shared pointer of TemporalMeasureCS.

class AxisDirection : public osgeo::proj::util::CodeList
    #include <coordinatesystem.hpp> The direction of positive increase in the coordinate value for a coordinate system axis.
Remark  Implements AxisDirection from ISO_19111_2019

Public Static Attributes

const AxisDirection NORTH
   Axis positive direction is north. In a geodetic or projected CRS, north is defined through the geodetic reference frame. In an engineering CRS, north may be defined with respect to an engineering object rather than a geographical direction.

const AxisDirection NORTH_NORTH_EAST
   Axis positive direction is approximately north-north-east.

const AxisDirection NORTH_EAST
   Axis positive direction is approximately north-east.

const AxisDirection EAST_NORTH_EAST
   Axis positive direction is approximately east-north-east.

const AxisDirection EAST
   Axis positive direction is 90deg clockwise from north.

const AxisDirection EAST_SOUTH_EAST
   Axis positive direction is approximately east-south-east.

const AxisDirection SOUTH_EAST
   Axis positive direction is approximately south-east.

const AxisDirection SOUTH_SOUTH_EAST
   Axis positive direction is approximately south-south-east.

const AxisDirection SOUTH
   Axis positive direction is 180deg clockwise from north.

const AxisDirection SOUTH_SOUTH_WEST
   Axis positive direction is approximately south-south-west.

const AxisDirection SOUTH_WEST
   Axis positive direction is approximately south-west.

const AxisDirection WEST_SOUTH_WEST
   Axis positive direction is approximately west-south-west.

const AxisDirection WEST
   Axis positive direction is 270deg clockwise from north.

const AxisDirection WEST_NORTH_WEST
   Axis positive direction is approximately west-north-west.

const AxisDirection NORTH_WEST
   Axis positive direction is approximately north-west.

const AxisDirection NORTH_NORTH_WEST
   Axis positive direction is approximately north-north-west.

const AxisDirection UP
   Axis positive direction is up relative to gravity.

const AxisDirection DOWN
   Axis positive direction is down relative to gravity.
const AxisDirection GEOCENTRIC_X
  Axis positive direction is in the equatorial plane from the centre of the modelled Earth towards the
  intersection of the equator with the prime meridian.

const AxisDirection GEOCENTRIC_Y
  Axis positive direction is in the equatorial plane from the centre of the modelled Earth towards the
  intersection of the equator and the meridian 90deg eastwards from the prime meridian.

const AxisDirection GEOCENTRIC_Z
  Axis positive direction is from the centre of the modelled Earth parallel to its rotation axis and towards
  its north pole.

const AxisDirection COLUMN_POSITIVE
  Axis positive direction is towards higher pixel column.

const AxisDirection COLUMN_NEGATIVE
  Axis positive direction is towards lower pixel column.

const AxisDirection ROW_POSITIVE
  Axis positive direction is towards higher pixel row.

const AxisDirection ROW_NEGATIVE
  Axis positive direction is towards lower pixel row.

const AxisDirection DISPLAY_RIGHT
  Axis positive direction is right in display.

const AxisDirection DISPLAY_LEFT
  Axis positive direction is left in display.

const AxisDirection DISPLAY_UP
  Axis positive direction is towards top of approximately vertical display surface.

const AxisDirection DISPLAY_DOWN
  Axis positive direction is towards bottom of approximately vertical display surface.

const AxisDirection FORWARD
  Axis positive direction is forward; for an observer at the centre of the object this is will be towards its
  front, bow or nose.

const AxisDirection AFT
  Axis positive direction is aft; for an observer at the centre of the object this will be towards its back,
  stern or tail.

const AxisDirection PORT
  Axis positive direction is port; for an observer at the centre of the object this will be towards its left.

const AxisDirection STARBOARD
  Axis positive direction is starboard; for an observer at the centre of the object this will be towards its
  right.

const AxisDirection CLOCKWISE
  Axis positive direction is clockwise from a specified direction.

const AxisDirection COUNTER_CLOCKWISE
  Axis positive direction is counter clockwise from a specified direction.

const AxisDirection TOWARDS
  Axis positive direction is towards the object.

const AxisDirection AWAY_FROM
  Axis positive direction is away from the object.
**const AxisDirection FUTURE**
Temporal axis positive direction is towards the future.

**const AxisDirection PAST**
Temporal axis positive direction is towards the past.

**const AxisDirection UNSPECIFIED**
Axis positive direction is unspecified.

**class CartesianCS : public osgeo::proj::cs::CoordinateSystem**

#include <coordinatesystem.hpp>

A two- or three-dimensional coordinate system in Euclidean space with orthogonal straight axes.

All axes shall have the same length unit. A *CartesianCS* shall have two or three axis associations; the number of associations shall equal the dimension of the CS.

**Remark** Implements *CartesianCS* from ISO_19111_2019

**Public Static Functions**

**CartesianCSNNPtr create (const util::PropertyMap &properties, const CoordinateSystemAxisNNPtr &axis1, const CoordinateSystemAxisNNPtr &axis2)**

Instantiate a *CartesianCS*.

**Return** a new *CartesianCS*.

**Parameters**
- *properties*: See *general_properties*.
- *axis1*: The first axis.
- *axis2*: The second axis.

**CartesianCSNNPtr create (const util::PropertyMap &properties, const CoordinateSystemAxisNNPtr &axis1, const CoordinateSystemAxisNNPtr &axis2, const CoordinateSystemAxisNNPtr &axis3)**

Instantiate a *CartesianCS*.

**Return** a new *CartesianCS*.

**Parameters**
- *properties*: See *general_properties*.
- *axis1*: The first axis.
- *axis2*: The second axis.
- *axis3*: The third axis.

**CartesianCSNNPtr createEastingNorthing (const common::UnitOfMeasure &unit)**

Instantiate a *CartesianCS* with a Easting (first) and Northing (second) axis.

**Return** a new *CartesianCS*.

**Parameters**
- *unit*: Linear unit of the axes.

**CartesianCSNNPtr createNorthingEasting (const common::UnitOfMeasure &unit)**

Instantiate a *CartesianCS* with a Northing (first) and Easting (second) axis.

**Return** a new *CartesianCS*.

**Parameters**
- *unit*: Linear unit of the axes.
CartesianCSNNPtr createNorthPoleEastingSouthNorthingSouth (const common::UnitOfMeasure &unit)

Instantiate a CartesianCS, north-pole centered, with a Easting (first) South-Oriented and Northing (second) South-Oriented axis.

Return a new CartesianCS.
Parameters
  • unit: Linear unit of the axes.

CartesianCSNNPtr createSouthPoleEastingNorthNorthingNorth (const common::UnitOfMeasure &unit)

Instantiate a CartesianCS, south-pole centered, with a Easting (first) North-Oriented and Northing (second) North-Oriented axis.

Return a new CartesianCS.
Parameters
  • unit: Linear unit of the axes.

CartesianCSNNPtr createWestingSouthing (const common::UnitOfMeasure &unit)

Instantiate a CartesianCS with a Westing (first) and Southing (second) axis.

Return a new CartesianCS.
Parameters
  • unit: Linear unit of the axes.

CartesianCSNNPtr createGeocentric (const common::UnitOfMeasure &unit)

Instantiate a CartesianCS with the three geocentric axes.

Return a new CartesianCS.
Parameters
  • unit: Linear unit of the axes.

class CoordinateSystem : public osgeo::proj::common::IdentifiedObject
#include <coordinate-system.hpp> Abstract class modelling a coordinate system (CS)

A CS is the non-repeating sequence of coordinate system axes that spans a given coordinate space. A CS is derived from a set of mathematical rules for specifying how coordinates in a given space are to be assigned to points. The coordinate values in a coordinate tuple shall be recorded in the order in which the coordinate system axes associations are recorded.

Remark Implements CoordinateSystem from ISO_19111_2019

Subclassed by osgeo::proj::cs::CartesianCS, osgeo::proj::cs::EllipsoidalCS, osgeo::proj::cs::OrdinalCS, osgeo::proj::cs::ParametricCS, osgeo::proj::cs::SphericalCS, osgeo::proj::cs::TemporalCS, osgeo::proj::cs::VerticalCS

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Public Functions

`const std::vector<CoordinateSystemAxisNNPtr> &axisList()`  
Return the list of axes of this coordinate system.

`class CoordinateSystemAxis : public osgeo::proj::common::IdentifiedObject`  
#include <coordinatesystem.hpp> The definition of a coordinate system axis.

Remark  Implements `CoordinateSystemAxis` from `ISO_19111_2019`

Public Functions

`const std::string &abbreviation()`  
Return the axis abbreviation.

The abbreviation used for this coordinate system axis; this abbreviation is also used to identify the coordinates in the coordinate tuple. Examples are X and Y.

Return the abbreviation.

`const AxisDirection &direction()`  
Return the axis direction.

The direction of this coordinate system axis (or in the case of Cartesian projected coordinates, the direction of this coordinate system axis locally) Examples: north or south, east or west, up or down. Within any set of coordinate system axes, only one of each pair of terms can be used. For Earth-fixed CRSs, this direction is often approximate and intended to provide a human interpretable meaning to the axis. When a geodetic reference frame is used, the precise directions of the axes may therefore vary slightly from this approximate direction. Note that an EngineeringCRS often requires specific descriptions of the directions of its coordinate system axes.

Return the direction.

`const common::UnitOfMeasure &unit()`  
Return the axis unit.

This is the spatial unit or temporal quantity used for this coordinate system axis. The value of a coordinate in a coordinate tuple shall be recorded using this unit.

Return the axis unit.

`const util::optional<double> &minimumValue()`  
Return the minimum value normally allowed for this axis, in the unit for the axis.

Return the minimum value, or empty.

`const util::optional<double> &maximumValue()`  
Return the maximum value normally allowed for this axis, in the unit for the axis.

Return the maximum value, or empty.

`const MeridianPtr &meridian()`  
Return the meridian that the axis follows from the pole, for a coordinate reference system centered on a pole.

Return the meridian, or null.
Public Static Functions

CoordinateSystemAxisNNPtr create(const util::PropertyMap &properties, const std::string &abbreviationIn, const AxisDirection &directionIn, const common::UnitOfMeasure &unitIn, const MeridianPtr &meridianIn = nullptr)

Instantiate a CoordinateSystemAxis.

Return a new CoordinateSystemAxis.

Parameters
• properties: See general_properties. The name should generally be defined.
• abbreviationIn: Axis abbreviation (might be empty)
• directionIn: Axis direction
• unitIn: Axis unit
• meridianIn: The meridian that the axis follows from the pole, for a coordinate reference system centered on a pole, or nullptr

class DateTimeTemporalCS: public osgeo::proj::cs::TemporalCS
#include <coordinatesystem.hpp> A one-dimensional coordinate system used to record time in dateTime representation as defined in ISO 8601.

A DateTimeTemporalCS shall have one axis association. It does not use axisUnitID; the temporal quantities are defined through the ISO 8601 representation.

Remark Implements DateTimeTemporalCS from ISO_19111_2019

Public Static Functions

DateTimeTemporalCSNNPtr create(const util::PropertyMap &properties, const CoordinateSystemAxisNNPtr &axis)

Instantiate a DateTimeTemporalCS.

Return a new DateTimeTemporalCS.

Parameters
• properties: See general_properties.
• axisIn: The axis.

class EllipsoidalCS: public osgeo::proj::cs::CoordinateSystem
#include <coordinatesystem.hpp> A two- or three-dimensional coordinate system in which position is specified by geodetic latitude, geodetic longitude, and (in the three-dimensional case) ellipsoidal height.

An EllipsoidalCS shall have two or three associations.

Remark Implements EllipsoidalCS from ISO_19111_2019

Public Static Functions

EllipsoidalCSNNPtr create(const util::PropertyMap &properties, const CoordinateSystemAxisNNPtr &axis1, const CoordinateSystemAxisNNPtr &axis2)

Instantiate a EllipsoidalCS.

Return a new EllipsoidalCS.

Parameters
• properties: See general_properties.
• axis1: The first axis.
• axis2: The second axis.

`EllipsoidalCSNNPtr create(const util::PropertyMap &properties, const CoordinateSystemAxisNNPtr &axis1, const CoordinateSystemAxisNNPtr &axis2, const CoordinateSystemAxisNNPtr &axis3)`

Instantiate a `EllipsoidalCS`.

**Return** a new `EllipsoidalCS`.

**Parameters**
- `properties`: See `general_properties`.
- `axis1`: The first axis.
- `axis2`: The second axis.
- `axis3`: The third axis.

`EllipsoidalCSNNPtr createLatitudeLongitude(const common::UnitOfMeasure &unit)`

Instantiate a `EllipsoidalCS` with a Latitude (first) and Longitude (second) axis.

**Return** a new `EllipsoidalCS`.

**Parameters**
- `unit`: Angular unit of the axes.

`EllipsoidalCSNNPtr createLatitudeLongitudeEllipsoidalHeight(const common::UnitOfMeasure &angularUnit, const common::UnitOfMeasure &linearUnit)`

Instantiate a `EllipsoidalCS` with a Latitude (first), Longitude (second) axis and ellipsoidal height (third) axis.

**Return** a new `EllipsoidalCS`.

**Parameters**
- `angularUnit`: Angular unit of the latitude and longitude axes.
- `linearUnit`: Linear unit of the ellipsoidal height axis.

`EllipsoidalCSNNPtr createLongitudeLatitude(const common::UnitOfMeasure &unit)`

Instantiate a `EllipsoidalCS` with a Longitude (first) and Latitude (second) axis.

**Return** a new `EllipsoidalCS`.

**Parameters**
- `unit`: Angular unit of the axes.

**class Meridian**

```cpp
#include <coordinatesystem.hpp>
```

The meridian that the axis follows from the pole, for a coordinate reference system centered on a pole.

**Note** There is no modelling for this concept in `ISO_19111_2019`

**Remark** Implements MERIDIAN from `WKT2`
Public Functions

```cpp
const common::Angle &longitude()
```

Return the longitude of the meridian that the axis follows from the pole.

Return the longitude.

Public Static Functions

```cpp
MeridianNNPtr create(const common::Angle &longitudeIn)
```

Instantiate a Meridian.

Return new Meridian.

Parameters

- `longitudeIn`: longitude of the meridian that the axis follows from the pole.

```cpp
class OrdinalCS : public osgeo::proj::cs::CoordinateSystem
```

#include <coordinatesystem.hpp>

n-dimensional coordinate system in which every axis uses integers.

The number of associations shall equal the dimension of the CS.

Remark Implements OrdinalCS from ISO_19111_2019

Public Static Functions

```cpp
OrdinalCSNNPtr create(const util::PropertyMap &properties,
                      const std::vector<CoordinateSystemAxisNNPtr> &axisIn)
```

Instantiate a OrdinalCS.

Return a new OrdinalCS.

Parameters

- `properties`: See general_properties.
- `axisIn`: List of axis.

```cpp
class ParametricCS : public osgeo::proj::cs::CoordinateSystem
```

#include <coordinatesystem.hpp>

one-dimensional coordinate reference system which uses parameter values or functions that may vary monotonically with height.

Remark Implements ParametricCS from ISO_19111_2019

Public Static Functions

```cpp
ParametricCSNNPtr create(const util::PropertyMap &properties,
                          const CoordinateSystemAxisNNPtr &axisIn)
```

Instantiate a ParametricCS.

Return a new ParametricCS.

Parameters

- `properties`: See general_properties.
- `axisIn`: Axis.

```cpp
class SphericalCS : public osgeo::proj::cs::CoordinateSystem
```

#include <coordinatesystem.hpp>

A three-dimensional coordinate system in Euclidean space with one distance measured from the origin and two angular coordinates.
Not to be confused with an ellipsoidal coordinate system based on an ellipsoid “degenerated” into a sphere. A SphericalCS shall have three axis associations.

**Remark** Implements SphericalCS from ISO_19111_2019

### Public Static Functions

*SphericalCS* NNPtr create(const util::PropertyMap &properties, const CoordinateSystemAxisNNPtr &axis1, const CoordinateSystemAxisNNPtr &axis2, const CoordinateSystemAxisNNPtr &axis3)

Instantiate a SphericalCS.

**Return** a new SphericalCS.

**Parameters**

- *properties*: See general_properties.
- *axis1*: The first axis.
- *axis2*: The second axis.
- *axis3*: The third axis.

#### class TemporalCountCS: public osgeo::proj::cs::TemporalCS

#include <coordinatesystem.hpp> A one-dimensional coordinate system used to record time as an integer count.

A TemporalCountCS shall have one axis association.

**Remark** Implements TemporalCountCS from ISO_19111_2019

### Public Static Functions

*TemporalCountCS* NNPtr create(const util::PropertyMap &properties, const CoordinateSystemAxisNNPtr &axis)

Instantiate a TemporalCountCS.

**Return** a new TemporalCountCS.

**Parameters**

- *properties*: See general_properties.
- *axis*: The axis.

#### class TemporalCS: public osgeo::proj::cs::TemporalCS

#include <coordinatesystem.hpp> (Abstract class) A one-dimensional coordinate system used to record time.

A TemporalCS shall have one axis association.

**Remark** Implements TemporalCS from ISO_19111_2019

Subclassed by osgeo::proj::cs::DateTimeTemporalCS, osgeo::proj::cs::TemporalCountCS, osgeo::proj::cs::TemporalMeasureCS

#### class TemporalMeasureCS: public osgeo::proj::cs::TemporalCS

#include <coordinatesystem.hpp> A one-dimensional coordinate system used to record a time as a real number.

A TemporalMeasureCS shall have one axis association.

**Remark** Implements TemporalMeasureCS from ISO_19111_2019
Public Static Functions

*TemporalMeasureCSNNPtr create(const util::PropertyMap &properties, const CoordinateSystemAxisNNPtr &axis)*

Instantiate a TemporalMeasureCS.

Return a new TemporalMeasureCS.

Parameters

- properties: See general_properties.
- axis: The axis.

class VerticalCS: public osgeo::proj::cs::CoordinateSystem

#include <coordinatesystem.hpp> A one-dimensional coordinate system used to record the heights or depths of points.

Such a coordinate system is usually dependent on the Earth’s gravity field. A VerticalCS shall have one axis association.

Remark Implements VerticalCS from ISO_19111_2019

Public Static Functions

*VerticalCSNNPtr create(const util::PropertyMap &properties, const CoordinateSystemAxisNNPtr &axis)*

Instantiate a VerticalCS.

Return a new VerticalCS.

Parameters

- properties: See general_properties.
- axis: The axis.

*VerticalCSNNPtr createGravityRelatedHeight(const common::UnitOfMeasure &unit)*

Instantiate a VerticalCS with a Gravity-related height axis.

Return a new VerticalCS.

Parameters

- unit: linear unit.

10.5.3.6 datum namespace

namespace datum

Datum (the relationship of a coordinate system to the body).

osgeo.proj.datum namespace

Typedefs

typedef std::shared_ptr<Datum> DatumPtr

Shared pointer of Datum

typedef util::nn<DatumPtr> DatumNNPtr

Non-null shared pointer of Datum

using DatumEnsemblePtr = std::shared_ptr<DatumEnsemble>

Shared pointer of DatumEnsemble
using DatumEnsembleNNPtr = util::nn<DatumEnsemblePtr>
Non-null shared pointer of DatumEnsemble

typedef std::shared_ptr<PrimeMeridian> PrimeMeridianPtr
Shared pointer of PrimeMeridian

typedef util::nn<PrimeMeridianPtr> PrimeMeridianNNPtr
Non-null shared pointer of PrimeMeridian

typedef std::shared_ptr<Ellipsoid> EllipsoidPtr
Shared pointer of Ellipsoid

typedef util::nn<EllipsoidPtr> EllipsoidNNPtr
Non-null shared pointer of Ellipsoid

typedef std::shared_ptr<GeodeticReferenceFrame> GeodeticReferenceFramePtr
Shared pointer of GeodeticReferenceFrame

typedef util::nn<GeodeticReferenceFramePtr> GeodeticReferenceFrameNNPtr
Non-null shared pointer of GeodeticReferenceFrame

using DynamicGeodeticReferenceFramePtr = std::shared_ptr<DynamicGeodeticReferenceFrame>
Shared pointer of DynamicGeodeticReferenceFrame

using DynamicGeodeticReferenceFrameNNPtr = util::nn<DynamicGeodeticReferenceFramePtr>
Non-null shared pointer of DynamicGeodeticReferenceFrame

typedef std::shared_ptr<VerticalReferenceFrame> VerticalReferenceFramePtr
Shared pointer of VerticalReferenceFrame

using DynamicVerticalReferenceFramePtr = std::shared_ptr<DynamicVerticalReferenceFrame>
Shared pointer of DynamicVerticalReferenceFrame

using DynamicVerticalReferenceFrameNNPtr = util::nn<DynamicVerticalReferenceFramePtr>
Non-null shared pointer of DynamicVerticalReferenceFrame

using TemporalDatumPtr = std::shared_ptr<TemporalDatum>
Shared pointer of TemporalDatum

using TemporalDatumNNPtr = util::nn<TemporalDatumPtr>
Non-null shared pointer of TemporalDatum

using EngineeringDatumPtr = std::shared_ptr<EngineeringDatum>
Shared pointer of EngineeringDatum

using EngineeringDatumNNPtr = util::nn<EngineeringDatumPtr>
Non-null shared pointer of EngineeringDatum

using ParametricDatumPtr = std::shared_ptr<ParametricDatum>
Shared pointer of ParametricDatum

using ParametricDatumNNPtr = util::nn<ParametricDatumPtr>
Non-null shared pointer of ParametricDatum

class Datum : public osgeo::proj::common::ObjectUsage
#include <datum.hpp> Abstract class of the relationship of a coordinate system to an object, thus creating a coordinate reference system.

For geodetic and vertical coordinate reference systems, it relates a coordinate system to the Earth (or the celestial body considered). With other types of coordinate reference systems, the datum may relate the coordinate system to another physical or virtual object. A datum uses a parameter or set of parameters
that determine the location of the origin of the coordinate reference system. Each datum subtype can be associated with only specific types of coordinate reference systems.

**Remark** Implements *Datum* from *ISO_19111_2019*

Subclassed by *osgeo::proj::datum::EngineeringDatum*, *osgeo::proj::datum::GeodeticReferenceFrame*, *osgeo::proj::datum::ParametricDatum*, *osgeo::proj::datum::TemporalDatum*, *osgeo::proj::datum::VerticalReferenceFrame*

**Public Functions**

```cpp
const util::optional<std::string> & anchorDefinition() const
```
Return the anchor definition.

A description - possibly including coordinates of an identified point or points - of the relationship used to anchor a coordinate system to the Earth or alternate object.

- For modern geodetic reference frames the anchor may be a set of station coordinates; if the reference frame is dynamic it will also include coordinate velocities. For a traditional geodetic datum, this anchor may be a point known as the fundamental point, which is traditionally the point where the relationship between geoid and ellipsoid is defined, together with a direction from that point.
- For a vertical reference frame the anchor may be the zero level at one or more defined locations or a conventionally defined surface.
- For an engineering datum, the anchor may be an identified physical point with the orientation defined relative to the object.

Return the anchor definition, or empty.

```cpp
const util::optional<common::DateTime> & publicationDate() const
```
Return the date on which the datum definition was published.

**Note** Departure from *ISO_19111_2019* : we return a DateTime instead of a Citation::Date.

Return the publication date, or empty.

```cpp
const common::IdentifiedObjectPtr & conventionalRS() const
```
Return the conventional reference system.

This is the name, identifier, alias and remarks for the terrestrial reference system or vertical reference system realized by this reference frame, for example “ITRS” for ITRF88 through ITRF2008 and ITRF2014, or “EVRS” for EVRF2000 and EVRF2007.

Return the conventional reference system, or nullptr.

**class DatumEnsemble**: public *osgeo::proj::common::IdentifiedObject*

A collection of two or more geodetic or vertical reference frames (or if not geodetic or vertical reference frame, a collection of two or more datums) which for all but the highest accuracy requirements may be considered to be insignificantly different from each other.

Every frame within the datum ensemble must be a realizations of the same Terrestrial Reference System or Vertical Reference System.

**Remark** Implements *DatumEnsemble* from *ISO_19111_2019*
Public Functions

```cpp
const std::vector<DatumNNPtr> &datums () const
    Return the set of datums which may be considered to be insignificantly different from each other.
    Return the set of datums of the DatumEnsemble.

const metadata::PositionalAccuracyNNPtr &positionalAccuracy () const
    Return the inaccuracy introduced through use of this collection of datums.
    It is an indication of the differences in coordinate values at all points between the various realizations
    that have been grouped into this datum ensemble.
    Return the accuracy.
```

Public Static Functions

```cpp
DatumEnsembleNNPtr create (const util::PropertyMap &properties, const std::vector<DatumNNPtr> &datumsIn, const metadata::PositionalAccuracyNNPtr &accuracy)
    Instantiate a DatumEnsemble.
    Return new DatumEnsemble.
    Parameters
    • properties: See general_properties. At minimum the name should be defined.
    • datumsIn: Array of at least 2 datums.
    • accuracy: Accuracy of the datum ensemble
    Exceptions
    • util::Exception:
```

```cpp
class DynamicGeodeticReferenceFrame : public osgeo::proj::datum::GeodeticReferenceFrame
    #include <datum.hpp> A geodetic reference frame in which some of the parameters describe time evolution
    of defining station coordinates.
    For example defining station coordinates having linear velocities to account for crustal motion.

    Remark Implements DynamicGeodeticReferenceFrame from ISO_19111_2019
```

Public Functions

```cpp
const common::Measure &frameReferenceEpoch () const
    Return the epoch to which the coordinates of stations defining the dynamic geodetic reference frame
    are referenced.
    Usually given as a decimal year e.g. 2016.47.
    Return the frame reference epoch.

const util::optional<std::string> &deformationModelName () const
    Return the name of the deformation model.
    Note This is an extension to the ISO_19111_2019 modeling, to hold the content of the DYNAMIC.MODEL WKT2 node.
    Return the name of the deformation model.
Public Static Functions

DynamicGeodeticReferenceFrameNNPtr create(const util::PropertyMap &properties, const EllipsoidNNPtr &ellipsoid, const util::optional<std::string> &anchor, const PrimeMeridianNNPtr &primeMeridian, const common::Measure &frameReferenceEpochIn, const util::optional<std::string> &deformationModelNameIn)

Instantiate a DynamicGeodeticReferenceFrame.

Return a new DynamicGeodeticReferenceFrame.

Parameters

- properties: See general_properties. At minimum the name should be defined.
- ellipsoid: the Ellipsoid.
- anchor: the anchor definition, or empty.
- primeMeridian: the PrimeMeridian.
- frameReferenceEpochIn: the frame reference epoch.
- deformationModelNameIn: deformation model name, or empty

class DynamicVerticalReferenceFrame : public osgeo::proj::datum::VerticalReferenceFrame

/include <datum.hpp> A vertical reference frame in which some of the defining parameters have time dependency.

For example defining station heights have velocity to account for post-glacial isostatic rebound motion.

Remark Implements DynamicVerticalReferenceFrame from ISO_19111_2019

Public Functions

const common::Measure &frameReferenceEpoch() const

Return the epoch to which the coordinates of stations defining the dynamic geodetic reference frame are referenced.

Usually given as a decimal year e.g. 2016.47.

Return the frame reference epoch.

const util::optional<std::string> &deformationModelName() const

Return the name of the deformation model.

Note This is an extension to the ISO_19111_2019 modeling, to hold the content of the DYNAMIC.MODEL WKT2 node.

Return the name of the deformation model.

Public Static Functions

DynamicVerticalReferenceFrameNNPtr create(const util::PropertyMap &properties, const util::optional<std::string> &anchor, const util::optional<RealizationMethod> &realizationMethodIn, const common::Measure &frameReferenceEpochIn, const util::optional<std::string> &deformationModelNameIn)

Instantiate a DynamicVerticalReferenceFrame.

Return a new DynamicVerticalReferenceFrame.
Parameters

- **properties**: See *general_properties*. At minimum the name should be defined.
- **anchor**: the anchor definition, or empty.
- **realizationMethodIn**: the realization method, or empty.
- **frameReferenceEpochIn**: the frame reference epoch.
- **deformationModelNameIn**: deformation model name, or empty

class Ellipsoid : public osgeo::proj::common::IdentifiedObject, public osgeo::proj::io::IPROJStringExportable

```cpp
#include <datum.hpp>
```

A geometric figure that can be used to describe the approximate shape of an object.

For the Earth an oblate biaxial ellipsoid is used: in mathematical terms, it is a surface formed by the rotation of an ellipse about its minor axis.

**Remark** Implements *Ellipsoid* from *ISO_19111_2019*

**Public Functions**

```cpp
class Ellipsoid : public osgeo::proj::common::IdentifiedObject, public osgeo::proj::io::IPROJStringExportable

const common::Length &semiMajorAxis ()
    Return the length of the semi-major axis of the ellipsoid.

    Return the semi-major axis.

const util::optional<common::Scale> &inverseFlattening ()
    Return the inverse flattening value of the ellipsoid, if the ellipsoid has been defined with this value.

    See `computeInverseFlattening()` that will always return a valid value of the inverse flattening, whether the ellipsoid has been defined through inverse flattening or semi-minor axis.

    Return the inverse flattening value of the ellipsoid, or empty.

const util::optional<common::Length> &semiMinorAxis ()
    Return the length of the semi-minor axis of the ellipsoid, if the ellipsoid has been defined with this value.

    See `computeSemiMinorAxis()` that will always return a valid value of the inverse flattening, whether the ellipsoid has been defined through inverse flattening or semi-minor axis.

    Return the semi-minor axis of the ellipsoid, or empty.

bool isSphere ()
    Return whether the ellipsoid is spherical.

    That is to say is `semiMajorAxis() == computeSemiMinorAxis()`. A sphere is completely defined by the semi-major axis, which is the radius of the sphere.

    Return true if the ellipsoid is spherical.

const util::optional<common::Length> &semiMedianAxis ()
    Return the length of the semi-median axis of a triaxial ellipsoid.

    This parameter is not required for a biaxial ellipsoid.

    Return the semi-median axis of the ellipsoid, or empty.

double computedInverseFlattening ()
    Return or compute the inverse flattening value of the ellipsoid.

    If computed, the inverse flattening is the result of `a / (a - b)`, where a is the semi-major axis and b the semi-minor axis.

    Return the inverse flattening value of the ellipsoid, or 0 for a sphere.
```
double squaredEccentricity()  
    Return the squared eccentricity of the ellipsoid.

Return the squared eccentricity, or a negative value if invalid.

common::Length computeSemiMinorAxis() const  
    Return or compute the length of the semi-minor axis of the ellipsoid.

If computed, the semi-minor axis is the result of a \ast (1 - 1 / rf) where a is the semi-major axis and rf the reverse/inverse flattening.

Return the semi-minor axis of the ellipsoid.

const std::string &celestialBody()  
    Return the name of the celestial body on which the ellipsoid refers to.

EllipsoidNNPtr identify() const  
    Return a Ellipsoid object where some parameters are better identified.

Return a new Ellipsoid.

Public Static Functions

EllipsoidNNPtr createSphere(const util::PropertyMap &properties, const common::Length &radius, const std::string &celestialBody = EARTH)  
    Instantiate a Ellipsoid as a sphere.

Return new Ellipsoid.

Parameters
    • properties: See general_properties. At minimum the name should be defined.
    • radius: the sphere radius (semi-major axis).
    • celestialBody: Name of the celestial body on which the ellipsoid refers to.

EllipsoidNNPtr createFlattenedSphere(const util::PropertyMap &properties, const common::Length &semiMajorAxisIn, const common::Scale &invFlattening, const std::string &celestialBody = EARTH)  
    Instantiate a Ellipsoid from its inverse/reverse flattening.

Return new Ellipsoid.

Parameters
    • properties: See general_properties. At minimum the name should be defined.
    • semiMajorAxisIn: the semi-major axis.
    • invFlattening: the inverse/reverse flattening. If set to 0, this will be considered as a sphere.
    • celestialBody: Name of the celestial body on which the ellipsoid refers to.

EllipsoidNNPtr createTwoAxis(const util::PropertyMap &properties, const common::Length &semiMajorAxisIn, const common::Length &semiMinorAxisIn, const std::string &celestialBody = EARTH)  
    Instantiate a Ellipsoid from the value of its two semi axis.

Return new Ellipsoid.

Parameters
    • properties: See general_properties. At minimum the name should be defined.
    • semiMajorAxisIn: the semi-major axis.
    • semiMinorAxisIn: the semi-minor axis.
    • celestialBody: Name of the celestial body on which the ellipsoid refers to.
**Public Static Attributes**

```
const std::string EARTH
   Earth celestial body.

const EllipsoidNNPtr CLARKE_1866
   The EPSG:7008 / “Clarke 1866” Ellipsoid.

const EllipsoidNNPtr WGS84
   The EPSG:7030 / “WGS 84” Ellipsoid.

const EllipsoidNNPtr GRS1980
```

**class EngineeringDatum : public osgeo::proj::datum::Datum**

```
#include <datum.hpp>
The definition of the origin and orientation of an engineering coordinate reference system.
```

**Note** The origin can be fixed with respect to the Earth (such as a defined point at a construction site), or be a defined point on a moving vehicle (such as on a ship or satellite), or a defined point of an image.

**Remark** Implements *EngineeringDatum* from *ISO_19111_2019*

**Public Static Functions**

```
EngineeringDatumNNPtr create(const util::PropertyMap &properties,
   const util::optional<std::string> &anchor = util::optional<std::string>())
```

Instantiates a *EngineeringDatum*.

**Return** new *EngineeringDatum*.

**Parameters**

- `properties`: See *general_properties*. At minimum the name should be defined.
- `anchor`: the anchor definition, or empty.

**class GeodeticReferenceFrame : public osgeo::proj::datum::Datum**

```
#include <datum.hpp>
The definition of the position, scale and orientation of a geocentric Cartesian 3D coordinate system relative to the Earth.
```

It may also identify a defined ellipsoid (or sphere) that approximates the shape of the Earth and which is centred on and aligned to this geocentric coordinate system. Older geodetic datums define the location and orientation of a defined ellipsoid (or sphere) that approximates the shape of the earth.

**Note** The terminology “Datum” is often used to mean a *GeodeticReferenceFrame*.

**Note** In *ISO_19111_2007*, this class was called GeodeticDatum.

**Remark** Implements *GeodeticReferenceFrame* from *ISO_19111_2019*

**Subclassed by** osgeo::proj::datum::DynamicGeodeticReferenceFrame
**Public Functions**

```c++
const PrimeMeridianNNPtr &primeMeridian()
```

Return the `PrimeMeridian` associated with a `GeodeticReferenceFrame`.

- **Return**: the `PrimeMeridian`.

```c++
const EllipsoidNNPtr &ellipsoid()
```

Return the `Ellipsoid` associated with a `GeodeticReferenceFrame`.

- **Note**: The `ISO_19111_2019` modelling allows (but discourages) a `GeodeticReferenceFrame` to not be associated with a `Ellipsoid` in the case where it is used by a geocentric `crs::GeodeticCRS`. We have made the choice of making the ellipsoid specification compulsory.

- **Return**: the `Ellipsoid`.

**Public Static Functions**

```c++
GeodeticReferenceFrameNNPtr create(const util::PropertyMap &properties, const EllipsoidNNPtr &ellipsoid, const util::optional<std::string> &anchor, const PrimeMeridianNNPtr &primeMeridian)
```

Instantiate a `GeodeticReferenceFrame`.

- **Return**: new `GeodeticReferenceFrame`.

- **Parameters**:
  - `properties`: See `general_properties`. At minimum the name should be defined.
  - `ellipsoid`: the `Ellipsoid`.
  - `anchor`: the anchor definition, or empty.
  - `primeMeridian`: the `PrimeMeridian`.

**Public Static Attributes**

```c++
const GeodeticReferenceFrameNNPtr EPSG_6267
```

The EPSG:6267 / “North_American_Datum_1927” `GeodeticReferenceFrame`.

```c++
const GeodeticReferenceFrameNNPtr EPSG_6269
```


```c++
const GeodeticReferenceFrameNNPtr EPSG_6326
```


**class ParametricDatum**: public osgeo::proj::Datum

`#include <datum.hpp>` Textual description and/or a set of parameters identifying a particular reference surface used as the origin of a parametric coordinate system, including its position with respect to the Earth.

- **Remark**: Implements `ParametricDatum` from `ISO_19111_2019`
Public Static Functions

\[
\text{ParametricDatumNNPtr create(const } \text{PropertyMap} \&\text{properties, const } \text{optional<} \text{string} \&\text{anchor} = \text{util::optional<string>()})
\]

Instantiate a \textit{ParametricDatum}.

Return new \textit{ParametricDatum}.

Parameters

- \text{properties}: See \textit{general_properties}. At minimum the name should be defined.
- \text{anchor}: the anchor definition, or empty.

\textbf{class PrimeMeridian: public} osgeo::proj::IdentifiedObject, public osgeo::proj::IProjStringExportable

\textbf{#include <datum.hpp>} The origin meridian from which longitude values are determined.

\textbf{Note} The default value for prime meridian name is “Greenwich”. When the default applies, the value for the longitude shall be 0 (degrees).

\textbf{Remark} Implements \textit{PrimeMeridian} from ISO_19111_2019

Public Functions

\[
\text{const } \text{common::Angle } \&\text{longitude}()
\]

Return the longitude of the prime meridian.

It is measured from the internationally-recognised reference meridian (‘Greenwich meridian’), positive eastward. The default value is 0 degrees.

Return the longitude of the prime meridian.

Public Static Functions

\[
\text{PrimeMeridianNNPtr create(const } \text{PropertyMap} \&\text{properties, const } \text{common::Angle } \&\text{longitudeIn})
\]

Instantiate a \textit{PrimeMeridian}.

Return new \textit{PrimeMeridian}.

Parameters

- \text{properties}: See \textit{general_properties}. At minimum the name should be defined.
- \text{longitudeIn}: the longitude of the prime meridian.

Public Static Attributes

\[
\text{const PrimeMeridianNNPtr GREENWICH}
\]

The Greenwich \textit{PrimeMeridian}.

\[
\text{const PrimeMeridianNNPtr REFERENCE_MERIDIAN}
\]

The “Reference Meridian” \textit{PrimeMeridian}.

This is a meridian of longitude 0 to be used with non-Earth bodies.

\[
\text{const PrimeMeridianNNPtr PARIS}
\]

The Paris \textit{PrimeMeridian}.

\textbf{class RealizationMethod: public} osgeo::proj::CodeList

\textbf{#include <datum.hpp>} The specification of the method by which the vertical reference frame is realized.
Remark  Implements \textit{RealizationMethod} from \textit{ISO\_19111\_2019}

Public Static Attributes

\texttt{const RealizationMethod LEVELLING}

The realization is by adjustment of a levelling network fixed to one or more tide gauges.

\texttt{const RealizationMethod GEOID}

The realization is through a geoid height model or a height correction model. This is applied to a specified geodetic CRS.

\texttt{const RealizationMethod TIDAL}

The realization is through a tidal model or by tidal predictions.

class TemporalDatum: public osgeo::proj::datum::Datum

\#include <datum.hpp> The definition of the relationship of a temporal coordinate system to an object. The object is normally time on the Earth.

Remark  Implements \textit{TemporalDatum} from \textit{ISO\_19111\_2019}

Public Functions

\texttt{const common::DateTime &temporalOrigin() const}

Return the date and time to which temporal coordinates are referenced, expressed in conformance with ISO 8601.

Return the temporal origin.

\texttt{const std::string &calendar() const}

Return the calendar to which the temporal origin is referenced.

Default value: \textit{TemporalDatum::CALENDAR\_PROLEPTIC\_GREGORIAN}.

Return the calendar.

Public Static Functions

\texttt{TemporalDatumNNPtr create(const util::PropertyMap &properties, const common::DateTime &temporalOriginIn, const std::string &calendarIn)}

Instantiate a \textit{TemporalDatum}.

Return new \textit{TemporalDatum}.

Parameters

- \texttt{properties}: See \textit{general\_properties}. At minimum the name should be defined.
- \texttt{temporalOriginIn}: the temporal origin into which temporal coordinates are referenced.
- \texttt{calendarIn}: the calendar (generally \textit{TemporalDatum::CALENDAR\_PROLEPTIC\_GREGORIAN})
**Public Static Attributes**

```cpp
class VerticalReferenceFrame : public osgeo::proj::datum::Datum
#include <datum.hpp> A textual description and/or a set of parameters identifying a particular reference level surface used as a zero-height or zero-depth surface, including its position with respect to the Earth.
```

**Note** In ISO_19111_2007, this class was called VerticalDatum.

**Remark** Implements VerticalReferenceFrame from ISO_19111_2019

Subclassed by osgeo::proj::datum::DynamicVerticalReferenceFrame

**Public Functions**

```cpp
const util::optional<RealizationMethod> &realizationMethod() const
Return the method through which this vertical reference frame is realized.
```

**Public Static Functions**

```cpp
VerticalReferenceFrameNNPtr create(const util::PropertyMap &properties,
const util::optional<std::string> &anchor = util::optional<std::string>(),
const util::optional<RealizationMethod> &realizationMethodIn
= util::optional<RealizationMethod>())
Instantiate a VerticalReferenceFrame.
Return new VerticalReferenceFrame.
```

**Parameters**

- **properties**: See general_properties. At minimum the name should be defined.
- **anchor**: the anchor definition, or empty.
- **realizationMethodIn**: the realization method, or empty.

**10.5.3.7 crs namespace**

```cpp
namespace crs
CRS (coordinate reference system = coordinate system with a datum).
oosgeo.proj.crs namespace
```
**Typedefs**

```cpp
typedef std::shared_ptr<CRS> CRSPtr
   Shared pointer of CRS

typedef util::nn<CRSPtr> CRSNNPtr
   Non-null shared pointer of CRS

typedef std::shared_ptr<GeographicCRS> GeographicCRSPtr
   Shared pointer of GeographicCRS

typedef util::nn<GeographicCRSPtr> GeographicCRSNNPtr
   Non-null shared pointer of GeographicCRS

typedef std::shared_ptr<VerticalCRS> VerticalCRSPtr
   Shared pointer of VerticalCRS

typedef util::nn<VerticalCRSPtr> VerticalCRSNNPtr
   Non-null shared pointer of VerticalCRS

using BoundCRSPtr = std::shared_ptr<BoundCRS>
   Shared pointer of BoundCRS

using BoundCRSNNPtr = util::nn<BoundCRSPtr>
   Non-null shared pointer of BoundCRS

using SingleCRSPtr = std::shared_ptr<SingleCRS>
   Shared pointer of SingleCRS

using SingleCRSNNPtr = util::nn<SingleCRSPtr>
   Non-null shared pointer of SingleCRS

typedef std::shared_ptr<GeodeticCRS> GeodeticCRSPtr
   Shared pointer of GeodeticCRS

typedef util::nn<GeodeticCRSPtr> GeodeticCRSNNPtr
   Non-null shared pointer of GeodeticCRS

using DerivedCRSPtr = std::shared_ptr<DerivedCRS>
   Shared pointer of DerivedCRS

using DerivedCRSNNPtr = util::nn<DerivedCRSPtr>
   Non-null shared pointer of DerivedCRS

typedef std::shared_ptr<ProjectedCRS> ProjectedCRSPtr
   Shared pointer of ProjectedCRS

typedef util::nn<ProjectedCRSPtr> ProjectedCRSNNPtr
   Non-null shared pointer of ProjectedCRS

using TemporalCRSPtr = std::shared_ptr<TemporalCRS>
   Shared pointer of TemporalCRS

using TemporalCRSNNPtr = util::nn<TemporalCRSPtr>
   Non-null shared pointer of TemporalCRS

using EngineeringCRSPtr = std::shared_ptr<EngineeringCRS>
   Shared pointer of EngineeringCRS

using EngineeringCRSNNPtr = util::nn<EngineeringCRSPtr>
   Non-null shared pointer of EngineeringCRS

using ParametricCRSPtr = std::shared_ptr<ParametricCRS>
   Shared pointer of ParametricCRS
```
using ParametricCRSNNPtr = util::nn<ParametricCRSPtr>
    Non-null shared pointer of ParametricCRS

typedef std::shared_ptr<CompoundCRS> CompoundCRSPtr
    Shared pointer of CompoundCRS

typedef util::nn<CompoundCRSPtr> CompoundCRSNNPtr
    Non-null shared pointer of CompoundCRS

using DerivedGeodeticCRSPPtr = std::shared_ptr<DerivedGeodeticCRS>
    Shared pointer of DerivedGeodeticCRS

using DerivedGeodeticCRSNNPtr = util::nn<DerivedGeodeticCRSPtr>
    Non-null shared pointer of DerivedGeodeticCRS

using DerivedGeographicCRSPPtr = std::shared_ptr<DerivedGeographicCRS>
    Shared pointer of DerivedGeographicCRS

using DerivedGeographicCRSNNPtr = util::nn<DerivedGeographicCRSPtr>
    Non-null shared pointer of DerivedGeographicCRS

using DerivedProjectedCRSPPtr = std::shared_ptr<DerivedProjectedCRS>
    Shared pointer of DerivedProjectedCRS

using DerivedProjectedCRSNNPtr = util::nn<DerivedProjectedCRSPtr>
    Non-null shared pointer of DerivedProjectedCRS

using DerivedVerticalCRSPPtr = std::shared_ptr<DerivedVerticalCRS>
    Shared pointer of DerivedVerticalCRS

using DerivedVerticalCRSNNPtr = util::nn<DerivedVerticalCRSPtr>
    Non-null shared pointer of DerivedVerticalCRS

using DerivedEngineeringCRSPPtr = std::shared_ptr<DerivedEngineeringCRS>
    Shared pointer of DerivedEngineeringCRS

using DerivedEngineeringCRSNNPtr = util::nn<DerivedEngineeringCRSPtr>
    Non-null shared pointer of DerivedEngineeringCRS

using DerivedParametricCRSPPtr = std::shared_ptr<DerivedParametricCRS>
    Shared pointer of DerivedParametricCRS

using DerivedParametricCRSNNPtr = util::nn<DerivedParametricCRSPtr>
    Non-null shared pointer of DerivedParametricCRS

using DerivedTemporalCRSPPtr = std::shared_ptr<DerivedTemporalCRS>
    Shared pointer of DerivedTemporalCRS

using DerivedTemporalCRSNNPtr = util::nn<DerivedTemporalCRSPtr>
    Non-null shared pointer of DerivedTemporalCRS

class BoundCRS : public osgeo::proj::crs::CRS, public osgeo::proj::io::IPROJStringExportable
    #include <crs.hpp> A coordinate reference system with an associated transformation to a target/hub CRS.

The definition of a CRS is not dependent upon any relationship to an independent CRS. However in an implementation that merges datasets referenced to differing CRSs, it is sometimes useful to associate the definition of the transformation that has been used with the CRS definition. This facilitates the interrelationship of CRS by concatenating transformations via a common or hub CRS. This is sometimes referred to as “early-binding”. WKT2 permits the association of an abridged coordinate transformation description with a coordinate reference system description in a single text string. In a BoundCRS, the abridged coordinate transformation is applied to the source CRS with the target CRS being the common or hub system.
Coordinates referring to a `BoundCRS` are expressed into its source/base `CRS`.

This abstraction can for example model the concept of TOWGS84 datum shift present in `WKT1`.

**Note** Contrary to other `CRS` classes of this package, there is no `ISO_19111_2019` modelling of a `BoundCRS`.

**Remark** Implements `BoundCRS` from `WKT2`

### Public Functions

```cpp
const CRSNNPtr &baseCRS() const
```

Return the base `CRS`.

This is the `CRS` into which coordinates of the `BoundCRS` are expressed.

**Return** the base `CRS`.

```cpp
CRSNNPtr baseCRSWITHCanonicalBoundCRS() const
```

Return a shallow clone of the base `CRS` that points to a shallow clone of this `BoundCRS`.

The base `CRS` is the `CRS` into which coordinates of the `BoundCRS` are expressed.

The returned `CRS` will actually be a shallow clone of the actual base `CRS`, with the extra property that `CRS::canonicalBoundCRS()` will point to a shallow clone of this `BoundCRS`. Use this only if you want to work with the base `CRS` object rather than the `BoundCRS`, but wanting to be able to retrieve the `BoundCRS` later.

**Return** the base `CRS`.

```cpp
const CRSNNPtr &hubCRS() const
```

Return the target / hub `CRS`.

**Return** the hub `CRS`.

```cpp
const operation::TransformationNNPtr &transformation() const
```

Return the transformation to the hub RS.

**Return** transformation.

### Public Static Functions

```cpp
BoundCRSNNPtr create(const CRSNNPtr &baseCRSIn, const CRSNNPtr &hubCRSIn, const operation::TransformationNNPtr &transformationIn)
```

Instantiate a `BoundCRS` from a base `CRS`, a hub `CRS` and a transformation.

**Return** new `BoundCRS`.

**Parameters**

- `baseCRSIn`: base `CRS`.
- `hubCRSIn`: hub `CRS`.
- `transformationIn`: transformation from base `CRS` to hub `CRS`.

```cpp
BoundCRSNNPtr createFromTOWGS84(const CRSNNPtr &baseCRSIn, const std::vector<double> &TOWGS84Parameters)
```

Instantiate a `BoundCRS` from a base `CRS` and TOWGS84 parameters.

**Return** new `BoundCRS`.

**Parameters**

- `baseCRSIn`: base `CRS`.
• **TOWGS84Parameters**: a vector of 3 or 7 double values representing WKT1 TOWGS84 parameter.

```cpp
BoundCRSNNPtrcreateFromNadgrids(const CRSNNPtr &baseCRSIn, const std::string &filename)
```

Instantiates a `BoundCRS` from a base `CRS` and nadgrids parameters.

**Parameters**
- `baseCRSIn`: base `CRS`.
- `filename`: Horizontal grid filename

```cpp
class CompoundCRS : public osgeo::proj::crs::CRS, public osgeo::proj::io::IPROJStringExportable
```

A coordinate reference system describing the position of points through two or more independent single coordinate reference systems.

**Note** Two coordinate reference systems are independent of each other if coordinate values in one cannot be converted or transformed into coordinate values in the other.

**Note** As a departure to *ISO_19111_2019*, we allow to build a `CompoundCRS` from `CRS` objects, whereas ISO19111:2019 restricts the components to `SingleCRS`.

**Remark** Implements `CompoundCRS` from *ISO_19111_2019*

### Public Functions

```cpp
const std::vector<CRSNNPtr> &componentReferenceSystems() const
```

Returns the components of a `CompoundCRS`.

**Return** the components.

```cpp
std::list<std::pair<CompoundCRSNNPtr, int>> identify(const io::AuthorityFactoryPtr &authorityFactory) const
```

Identifies the `CRS` with reference CRSs.

The candidate CRSs are looked in the database when `authorityFactory` is not null.

The method returns a list of matching reference `CRS`, and the percentage (0-100) of confidence in the match. The list is sorted by decreasing confidence.

100% means that the name of the reference entry perfectly matches the `CRS` name, and both are equivalent. In which case a single result is returned. 90% means that `CRS` are equivalent, but the names are not exactly the same. 70% means that `CRS` are equivalent (equivalent horizontal and vertical `CRS`), but the names do not match at all. 25% means that the `CRS` are not equivalent, but there is some similarity in the names.

**Return** a list of matching reference `CRS`, and the percentage (0-100) of confidence in the match.

**Parameters**
- `authorityFactory`: Authority factory (if null, will return an empty list)
Public Static Functions

\[
\text{CompoundCRSNNPtr create(const util::PropertyMap &properties, const std::vector<CompoundCRSNNPtr> &components)}
\]

Instantiates a \text{CompoundCRS} from a vector of \text{CRS}.

Return new \text{CompoundCRS}.

Parameters

- \text{properties}: See \text{general_properties}. At minimum the name should be defined.
- \text{components}: the component \text{CRS} of the \text{CompoundCRS}.

\text{class CRS: public osgeo::proj::common::ObjectUsage}

\#include <crs.hpp> Abstract class modelling a coordinate reference system which is usually single but may be compound.

Remark Implements \text{CRS} from \text{ISO_19111_2019}

Subclassed by \text{osgeo::proj::crs::BoundCRS, osgeo::proj::crs::CompoundCRS, osgeo::proj::crs::SingleCRS}

Public Functions

\text{GeodeticCRSPtr extractGeodeticCRS () const}

Return the \text{GeodeticCRS} of the \text{CRS}.

Returns the \text{GeodeticCRS} contained in a \text{CRS}. This works currently with input parameters of type \text{GeodeticCRS} or derived, \text{ProjectedCRS}, \text{CompoundCRS} or \text{BoundCRS}.

Return a \text{GeodeticCRSPtr}, that might be null.

\text{GeographicCRSPtr extractGeographicCRS () const}

Return the \text{GeographicCRS} of the \text{CRS}.

Returns the \text{GeographicCRS} contained in a \text{CRS}. This works currently with input parameters of type \text{GeographicCRS} or derived, \text{ProjectedCRS}, \text{CompoundCRS} or \text{BoundCRS}.

Return a \text{GeographicCRSPtr}, that might be null.

\text{VerticalCRSPtr extractVerticalCRS () const}

Return the \text{VerticalCRS} of the \text{CRS}.

Returns the \text{VerticalCRS} contained in a \text{CRS}. This works currently with input parameters of type \text{VerticalCRS} or derived, \text{CompoundCRS} or \text{BoundCRS}.

Return a \text{VerticalCRSPtr}, that might be null.

\text{CRSNNPtr createBoundCRSToWGS84IfPossible (const io::DatabaseContextPtr &dbContext, operation::CoordinateOperationContext::IntermediateCRSUse allowIntermediateCRSUse) const}

Returns potentially a \text{BoundCRS}, with a transformation to EPSG:4326, wrapping this \text{CRS}.

If no such \text{BoundCRS} is possible, the object will be returned.

The purpose of this method is to be able to format a PROJ.4 string with a +towgs84 parameter or a \text{WKT1:GDAL} string with a TOWGS node.

This method will fetch the \text{GeographicCRS} of this \text{CRS} and find a transformation to EPSG:4326 using the domain of the validity of the main \text{CRS}.

10.5. Reference
Return a CRS.

CRSNNPtr stripVerticalComponent() const

Returns a CRS whose coordinate system does not contain a vertical component.

Return a CRS.

const BoundCRSPtr &canonicalBoundCRS()

Return the BoundCRS potentially attached to this CRS.

In the case this method is called on a object returned by BoundCRS::baseCRSWithCanonicalBoundCRS(), this method will return this BoundCRS

Return a BoundCRSPtr, that might be null.

std::list<std::pair<CRSNNPtr, int>> identify(const io::AuthorityFactoryPtr &authorityFactory) const

Identify the CRS with reference CRSs.

The candidate CRSs are either hard-coded, or looked in the database when authorityFactory is not null.

The method returns a list of matching reference CRS, and the percentage (0-100) of confidence in the match. The list is sorted by decreasing confidence.

100% means that the name of the reference entry perfectly matches the CRS name, and both are equivalent. In which case a single result is returned. 90% means that CRS are equivalent, but the names are not exactly the same. 70% means that CRS are equivalent), but the names do not match at all. 25% means that the CRS are not equivalent, but there is some similarity in the names. Other confidence values may be returned by some specialized implementations.

This is implemented for GeodeticCRS, ProjectedCRS, VerticalCRS and CompoundCRS.

Return a list of matching reference CRS, and the percentage (0-100) of confidence in the match.

Parameters

• authorityFactory: Authority factory (or null, but degraded functionality)

std::list<CRSNNPtr> getNonDeprecated(const io::DatabaseContextNNPtr &dbContext) const

Return CRSs that are non-deprecated substitutes for the current CRS.

class DerivedCRS : public virtual osgeo::proj::crs::SingleCRS
#include <crs.hpp> Abstract class modelling a single coordinate reference system that is defined through the application of a specified coordinate conversion to the definition of a previously established single coordinate reference system referred to as the base CRS.

A derived coordinate reference system inherits its datum (or datum ensemble) from its base CRS. The coordinate conversion between the base and derived coordinate reference system is implemented using the parameters and formula(s) specified in the definition of the coordinate conversion.

Remark Implements DerivedCRS from ISO_19111_2019

Subclassed by osgeo::proj::crs::DerivedCRSTemplate< DerivedEngineeringCRSTraits >, osgeo::proj::crs::DerivedCRSTemplate< DerivedParametricCRSTraits >, osgeo::proj::crs::DerivedCRSTemplate< DerivedTemporalCRSTraits >, osgeo::proj::crs::DerivedGeodeticCRS, osgeo::proj::crs::DerivedGeographicCRS, osgeo::proj::crs::DerivedProjectedCRS, osgeo::proj::crs::DerivedVerticalCRS, osgeo::proj::crs::ProjectedCRS
Public Functions

```cpp
const SingleCRSNNPtr &baseCRS ()
    Return the base CRS of a DerivedCRS.
```

```cpp
const operation::ConversionNNPtr derivingConversion () const
    Return the deriving conversion from the base CRS to this CRS.
```

```cpp
template<class DerivedCRSTraits>
class DerivedCRSTemplate : public BaseType, public osgeo::proj::crs::DerivedCRS
    #include <crs.hpp> Template representing a derived coordinate reference system.
```

Public Types

```cpp
typedef util::nn<std::shared_ptr<DerivedCRSTemplate>> NNPtr
    Non-null shared pointer of DerivedCRSTemplate
```

```cpp
typedef util::nn<std::shared_ptr<BaseType>> BaseNNPtr
    Non-null shared pointer of BaseType
```

```cpp
typedef util::nn<std::shared_ptr<CSType>> CSNNPtr
    Non-null shared pointer of CSType
```

Public Functions

```cpp
const DerivedCRSTemplate<DerivedCRSTraits>::BaseNNPtr baseCRS () const
    Return the base CRS of a DerivedCRSTemplate.
```

Public Static Functions

```cpp
static NNPtr create (const util::PropertyMap &properties, const BaseNNPtr &baseCRSIn,
                     const operation::ConversionNNPtr &derivingConversionIn, const CSNNPtr &csIn)
    Instantiate a DerivedCRSTemplate from a base CRS, a deriving conversion and a
    cs::CoordinateSystem.
```

Remark

Implements DerivedEngineeringCRS from ISO_19111_2019
class DerivedGeodeticCRS : public osgeo::proj::crs::GeodeticCRS, public osgeo::proj::crs::DerivedCRS

#include <crs.hpp>

A derived coordinate reference system which has either a geodetic or a geographic coordinate reference system as its base CRS, thereby inheriting a geodetic reference frame, and associated with a 3D Cartesian or spherical coordinate system.

Remark Implements DerivedGeodeticCRS from ISO_19111_2019

Public Functions

const GeodeticCRSNPtr baseCRS () const

Return the base CRS (a GeodeticCRS) of a DerivedGeodeticCRS.

Public Static Functions

DerivedGeodeticCRSNPtr create (const util::PropertyMap &properties, const GeodeticCRSNPtr &baseCRSIn, const operation::ConversionNPtr &derivingConversionIn, const cs::CartesianCSNPtr &csIn)

Instantiate a DerivedGeodeticCRS from a base CRS, a deriving conversion and a cs::CartesianCS.

Return new DerivedGeodeticCRS.

Parameters

• properties: See general_properties. At minimum the name should be defined.
• baseCRSIn: base CRS.
• derivingConversionIn: the deriving conversion from the base CRS to this CRS.
• csIn: the coordinate system.

DerivedGeodeticCRSNPtr create (const util::PropertyMap &properties, const GeodeticCRSNPtr &baseCRSIn, const operation::ConversionNPtr &derivingConversionIn, const cs::SphericalCSNPtr &csIn)

Instantiate a DerivedGeodeticCRS from a base CRS, a deriving conversion and a cs::SphericalCS.

Return new DerivedGeodeticCRS.

Parameters

• properties: See general_properties. At minimum the name should be defined.
• baseCRSIn: base CRS.
• derivingConversionIn: the deriving conversion from the base CRS to this CRS.
• csIn: the coordinate system.

class DerivedGeographicCRS : public osgeo::proj::crs::GeographicCRS, public osgeo::proj::crs::DerivedCRS

#include <crs.hpp>

A derived coordinate reference system which has either a geodetic or a geographic coordinate reference system as its base CRS, thereby inheriting a geodetic reference frame, and an ellipsoidal coordinate system.

A derived geographic CRS can be based on a geodetic CRS only if that geodetic CRS definition includes an ellipsoid.

Remark Implements DerivedGeographicCRS from ISO_19111_2019
Public Functions

\textbf{const GeodeticCRSNNPtr baseCRS () const}

Return the base \textit{CRS} (a \textit{GeodeticCRS}) of a \textit{DerivedGeographicCRS}.

\textbf{Public Static Functions}

\textbf{DerivedGeographicCRSNNPtr create (const util::PropertyMap &properties, const GeodeticCRSNNPtr &baseCRSIn, const operation::ConversionNNPtr &derivingConversionIn, const cs::EllipsoidalCSNNPtr &csIn)}

Instantiate a \textit{DerivedGeographicCRS} from a base \textit{CRS}, a deriving conversion and a \textit{cs::EllipsoidalCS}.

Return new \textit{DerivedGeographicCRS}.

\textbf{Parameters}

- \textit{properties}: See \textit{general_properties}. At minimum the name should be defined.
- \textit{baseCRSIn}: base \textit{CRS}.
- \textit{derivingConversionIn}: the deriving conversion from the base \textit{CRS} to this \textit{CRS}.
- \textit{csIn}: the coordinate system.

\textbf{class DerivedParametricCRS : public osgeo::proj::crs::DerivedCRSTemplate<DerivedParametricCRSTraits>}

\textit{#include <crs.hpp>} A derived coordinate reference system which has a parametric coordinate reference system as its base \textit{CRS}, thereby inheriting a parametric datum, and a parametric coordinate system.

\textbf{Remark} Implements \textit{DerivedParametricCRS} from \textit{ISO\_19111\_2019}

\textbf{class DerivedProjectedCRS : public osgeo::proj::crs::DerivedCRS}

\textit{#include <crs.hpp>} A derived coordinate reference system which has a projected coordinate reference system as its base \textit{CRS}, thereby inheriting a geodetic reference frame, but also inheriting the distortion characteristics of the base projected \textit{CRS}.

A \textit{DerivedProjectedCRS} is not a \textit{ProjectedCRS}.

\textbf{Remark} Implements \textit{DerivedProjectedCRS} from \textit{ISO\_19111\_2019}

Public Functions

\textbf{const ProjectedCRSNNPtr baseCRS () const}

Return the base \textit{CRS} (a \textit{ProjectedCRS}) of a \textit{DerivedProjectedCRS}.

Return the base \textit{CRS}.
Public Static Functions

```
DerivedProjectedCRSNNPtr create(const util::PropertyMap &properties, const ProjectedCRSNNPtr &baseCRSIn, const operation::ConversionNNPtr &derivingConversionIn, const cs::CoordinateSystemNNPtr &csIn)
```

Instantiate a `DerivedProjectedCRS` from a base `CRS`, a deriving conversion and a `cs::CS`.

Return new `DerivedProjectedCRS`.

Parameters
- `properties`: See `general_properties`. At minimum the name should be defined.
- `baseCRSIn`: base `CRS`.
- `derivingConversionIn`: the deriving conversion from the base `CRS` to this `CRS`.
- `csIn`: the coordinate system.

```
class DerivedTemporalCRS : public osgeo::proj::crs::DerivedCRSTemplate<DerivedTemporalCRSTraits>
```

#include `<crs.hpp>`

A derived coordinate reference system which has a temporal coordinate reference system as its base `CRS`, thereby inheriting a temporal datum, and a temporal coordinate system.

**Remark** Implements `DerivedTemporalCRS` from `ISO_19111_2019`

```
class DerivedVerticalCRS : public osgeo::proj::crs::VerticalCRS, public osgeo::proj::crs::DerivedCRS
```

#include `<crs.hpp>`

A derived coordinate reference system which has a vertical coordinate reference system as its base `CRS`, thereby inheriting a vertical reference frame, and a vertical coordinate system.

**Remark** Implements `DerivedVerticalCRS` from `ISO_19111_2019`

Public Functions

```
const VerticalCRSNNPtr baseCRS() const
```

Return the base `CRS` (a `VerticalCRS`) of a `DerivedVerticalCRS`.

Return the base `CRS`.

Public Static Functions

```
DerivedVerticalCRSNNPtr create(const util::PropertyMap &properties, const VerticalCRSNNPtr &baseCRSIn, const operation::ConversionNNPtr &derivingConversionIn, const cs::VerticalCSNNPtr &csIn)
```

Instantiate a `DerivedVerticalCRS` from a base `CRS`, a deriving conversion and a `cs::VerticalCS`.

Return new `DerivedVerticalCRS`.

Parameters
- `properties`: See `general_properties`. At minimum the name should be defined.
- `baseCRSIn`: base `CRS`.
- `derivingConversionIn`: the deriving conversion from the base `CRS` to this `CRS`.
- `csIn`: the coordinate system.

```
class EngineeringCRS : public virtual osgeo::proj::crs::SingleCRS
```

#include `<crs.hpp>`

Contextually local coordinate reference system associated with an engineering datum.

It is applied either to activities on or near the surface of the Earth without geodetic corrections, or on moving platforms such as road vehicles, vessels, aircraft or spacecraft, or as the internal `CRS` of an image.
In *WKT2*, it maps to a ENGINEERINGCRS / ENGCRS keyword. In *WKT1*, it maps to a LOCAL_CS keyword.

**Remark** Implements *EngineeringCRS* from *ISO_19111_2019*

**Public Functions**

```cpp
const datum::EngineeringDatumNNPtr datum() const
Return the *datum::EngineeringDatum* associated with the *CRS*.
```

**Public Static Functions**

```cpp
EngineeringCRSNNPtr create(const util::PropertyMap &properties, const datum::EngineeringDatumNNPtr &datumIn, const cs::CoordinateSystemNNPtr &csIn)
Instantiate a *EngineeringCRS* from a datum and a coordinate system.
Return new *EngineeringCRS*.
Parameters
• properties: See *general_properties*. At minimum the name should be defined.
• datumIn: the datum.
• csIn: the coordinate system.
```

**class GeodeticCRS**

```cpp
#include <crs.hpp>
A coordinate reference system associated with a geodetic reference frame and a three-dimensional Cartesian or spherical coordinate system.

If the geodetic reference frame is dynamic or if the geodetic *CRS* has an association to a velocity model then the geodetic *CRS* is dynamic, else it is static.

**Remark** Implements *GeodeticCRS* from *ISO_19111_2019*

Subclassed by *osgeo::proj::crs::DerivedGeodeticCRS, osgeo::proj::crs::GeographicCRS*

**Public Functions**

```cpp
const datum::GeodeticReferenceFramePtr &datum() 
Return the *datum::GeodeticReferenceFrame* associated with the *CRS*.
Return a GeodeticReferenceFrame or null (in which case *datumEnsemble* should return a non-null pointer.)
```

```cpp
const datum::PrimeMeridianNNPtr &primeMeridian() 
Return the PrimeMeridian associated with the GeodeticReferenceFrame or with one of the GeodeticReferenceFrame of the *datumEnsemble*.
Return the PrimeMeridian.
```

```cpp
const datum::EllipsoidNNPtr &ellipsoid() 
Return the ellipsoid associated with the GeodeticReferenceFrame or with one of the GeodeticReferenceFrame of the *datumEnsemble*.
Return the PrimeMeridian.
```
const std::vector<operation::PointMotionOperationNNPtr> &velocityModel()

Return the velocity model associated with the CRS.

Return a velocity model. might be null.

bool isGeocentric()

Return whether the CRS is a geocentric one.

A geocentric CRS is a geodetic CRS that has a Cartesian coordinate system with three axis, whose direction is respectively cs::AxisDirection::GEOCENTRIC_X, cs::AxisDirection::GEOCENTRIC_Y and cs::AxisDirection::GEOCENTRIC_Z.

Return true if the CRS is a geocentric CRS.

std::list<std::pair<GeodeticCRSNNPtr, int>> identify(const io::AuthorityFactoryPtr &authorityFactory) const

Identify the CRS with reference CRSs.

The candidate CRSs are either hard-coded, or looked in the database when authorityFactory is not null.

The method returns a list of matching reference CRS, and the percentage (0-100) of confidence in the match. 100% means that the name of the reference entry perfectly matches the CRS name, and both are equivalent. In which case a single result is returned. 90% means that CRS are equivalent, but the names are not exactly the same. 70% means that CRS are equivalent (equivalent datum and coordinate system), but the names do not match at all. 60% means that ellipsoid, prime meridian and coordinate systems are equivalent, but the CRS and datum names do not match. 25% means that the CRS are not equivalent, but there is some similarity in the names.

Return a list of matching reference CRS, and the percentage (0-100) of confidence in the match.

Parameters
• authorityFactory: Authority factory (or null, but degraded functionality)

Public Static Functions

GeodeticCRSNNPtr create(const util::PropertyMap &properties, const datum::GeodeticReferenceFrameNNPtr &datum, const cs::SphericalCSNNPtr &cs)

Instantiate a GeodeticCRS from a datum::GeodeticReferenceFrame and a cs::SphericalCS.

Return new GeodeticCRS.

Parameters
• properties: See general_properties. At minimum the name should be defined.
• datum: The datum of the CRS.
• cs: a SphericalCS.

GeodeticCRSNNPtr create(const util::PropertyMap &properties, const datum::GeodeticReferenceFrameNNPtr &datum, const cs::CartesianCSNNPtr &cs)

Instantiate a GeodeticCRS from a datum::GeodeticReferenceFrame and a cs::CartesianCS.

Return new GeodeticCRS.

Parameters
• properties: See general_properties. At minimum the name should be defined.
• datum: The datum of the CRS.
• cs: a CartesianCS.
PROJ coordinate transformation software library, Release 6.1.1

GeodeticCRSNPtr create(const util::PropertyMap &properties, const datum::GeodeticReferenceFramePtr &datum, const datum::DatumEnsemblePtr &datumEnsemble, const cs::SphericalCSNNPtr &cs)

Instantiate a GeodeticCRS from a datum::GeodeticReferenceFrame or datum::DatumEnsemble and a cs::SphericalCS.

One and only one of datum or datumEnsemble should be set to a non-null value.

Return new GeodeticCRS.

Parameters

- properties: See general_properties. At minimum the name should be defined.
- datum: The datum of the CRS, or nullptr
- datumEnsemble: The datum ensemble of the CRS, or nullptr.
- cs: a SphericalCS.

GeodeticCRSNPtr create(const util::PropertyMap &properties, const datum::GeodeticReferenceFramePtr &datum, const datum::DatumEnsemblePtr &datumEnsemble, const cs::CartesianCSNNPtr &cs)

Instantiate a GeodeticCRS from a datum::GeodeticReferenceFrame or datum::DatumEnsemble and a cs::CartesianCS.

One and only one of datum or datumEnsemble should be set to a non-null value.

Return new GeodeticCRS.

Parameters

- properties: See general_properties. At minimum the name should be defined.
- datum: The datum of the CRS, or nullptr
- datumEnsemble: The datum ensemble of the CRS, or nullptr.
- cs: a CartesianCS

Public Static Attributes

const GeodeticCRSNPtr EPSG_4978

EPSG:4978 / “WGS 84” Geocentric.

class GeographicCRS : public osgeo::proj::crs::GeodeticCRS

#include <crs.hpp> A coordinate reference system associated with a geodetic reference frame and a two- or three-dimensional ellipsoidal coordinate system.

If the geodetic reference frame is dynamic or if the geographic CRS has an association to a velocity model then the geodetic CRS is dynamic, else it is static.

Remark Implements GeographicCRS from ISO_19111_2019

Subclassed by osgeo::proj::crs::DerivedGeographicCRS
Public Functions

\texttt{const \texttt{cs::EllipsoidalCSNNPtr \&coordinateSystem()}}

Return the \texttt{cs::EllipsoidalCS} associated with the \texttt{CPS}.

Return a EllipsoidalCS.

Public Static Functions

\texttt{GeographicCRSNNPtr create(const util::PropertyMap \&properties, const datum::GeodeticReferenceFrameNNPtr \&datum, const \texttt{cs::EllipsoidalCSNNPtr \&cs)}}

Instantiate a \texttt{GeographicCRS} from a \texttt{datum::GeodeticReferenceFrameNNPtr} and a \texttt{cs::EllipsoidalCS}.

Return new \texttt{GeographicCRS}.

Parameters

- \texttt{properties}: See \texttt{general_properties}. At minimum the name should be defined.
- \texttt{datum}: The datum of the \texttt{CPS}.
- \texttt{cs}: a EllipsoidalCS.

\texttt{GeographicCRSNNPtr create(const util::PropertyMap \&properties, const datum::GeodeticReferenceFramePtr \&datum, const datum::DatumEnsemblePtr \&datumEnsemble, const \texttt{cs::EllipsoidalCSNNPtr \&cs)}}

Instantiate a \texttt{GeographicCRS} from a \texttt{datum::GeodeticReferenceFramePtr} or \texttt{datum::DatumEnsemble} and a \texttt{cs::EllipsoidalCS}.

One and only one of datum or datumEnsemble should be set to a non-null value.

Return new \texttt{GeographicCRS}.

Parameters

- \texttt{properties}: See \texttt{general_properties}. At minimum the name should be defined.
- \texttt{datum}: The datum of the \texttt{CPS}, or nullptr.
- \texttt{datumEnsemble}: The datum ensemble of the \texttt{CPS}, or nullptr.
- \texttt{cs}: a EllipsoidalCS.

Public Static Attributes

\texttt{const GeographicCRSNNPtr EPSG_4267}

EPSG:4267 / “NAD27” 2D \texttt{GeographicCRS}.

\texttt{const GeographicCRSNNPtr EPSG_4269}

EPSG:4269 / “NAD83” 2D \texttt{GeographicCRS}.

\texttt{const GeographicCRSNNPtr EPSG_4326}

EPSG:4326 / “WGS 84” 2D \texttt{GeographicCRS}.

\texttt{const GeographicCRSNNPtr EPSG_4807}

EPSG:4807 / “NTF (Paris)” 2D \texttt{GeographicCRS}.

\texttt{const GeographicCRSNNPtr EPSG_4979}

EPSG:4979 / “WGS 84” 3D \texttt{GeographicCRS}.
class ParametricCRS: public virtual osgeo::proj::SingleCRS
#include <crs.hpp> Contextually local coordinate reference system associated with an engineering datum. This is applied either to activities on or near the surface of the Earth without geodetic corrections, or on moving platforms such as road vehicles vessels, aircraft or spacecraft, or as the internal CRS of an image.

Remark Implements ParametricCRS from ISO_19111_2019

Public Functions

const datum::ParametricDatumNNPtr datum() const
Return the datum::ParametricDatum associated with the CRS.

Return a ParametricDatum

const cs::ParametricCSNNPtr coordinateSystem() const
Return the cs::TemporalCS associated with the CRS.

Return a TemporalCS

Public Static Functions

ParametricCRSNNPtr create(const util::PropertyMap &properties, const datum::ParametricDatumNNPtr &datumIn, const cs::ParametricCSNNPtr &csIn)
Instantiate a ParametricCRS from a datum and a coordinate system.

Return new ParametricCRS.

Parameters
• properties: See general_properties. At minimum the name should be defined.
• datumIn: the datum.
• csIn: the coordinate system.

class ProjectedCRS: public osgeo::proj::DerivedCRS, public osgeo::proj::IPROJStringExportable
#include <crs.hpp> A derived coordinate reference system which has a geodetic (usually geographic) coordinate reference system as its base CRS, thereby inheriting a geodetic reference frame, and is converted using a map projection.

It has a Cartesian coordinate system, usually two-dimensional but may be three-dimensional; in the 3D case the base geographic CRSs ellipsoidal height is passed through unchanged and forms the vertical axis of the projected CRS's Cartesian coordinate system.

Remark Implements ProjectedCRS from ISO_19111_2019

Public Functions

const GeodeticCRSNNPtr &baseCRS ()
Return the base CRS (a GeodeticCRS, which is generally a GeographicCRS) of the ProjectedCRS.

Return the base CRS.

const cs::CartesianCSNNPtr &coordinateSystem ()
Return the cs::CartesianCS associated with the CRS.

Return a CartesianCS
std::list<std::pair<ProjectedCRSNNPtr, int>> identify(const io::AuthorityFactoryPtr &authorityFactory) const

Identify the CRS with reference CRSs.

The candidate CRSs are either hard-coded, or looked in the database when authorityFactory is not null.

The method returns a list of matching reference CRS, and the percentage (0-100) of confidence in the match. The list is sorted by decreasing confidence.

100% means that the name of the reference entry perfectly matches the CRS name, and both are equivalent. In which case a single result is returned. 90% means that CRS are equivalent, but the names are not exactly the same. 70% means that CRS are equivalent (equivalent base CRS, conversion and coordinate system), but the names do not match at all. 50% means that CRS have similarity (equivalent base CRS and conversion), but the coordinate system do not match (e.g. different axis ordering or axis unit). 25% means that the CRS are not equivalent, but there is some similarity in the names.

For the purpose of this function, equivalence is tested with the util::IComparable::Criterion::EQUIVALENT_EXCEPT_AXIS_ORDER_GEOGCRS, that is to say that the axis order of the base GeographicCRS is ignored.

Return a list of matching reference CRS, and the percentage (0-100) of confidence in the match.

Parameters
- authorityFactory: Authority factory (or null, but degraded functionality)

Public Static Functions

ProjectedCRSNNPtr create(const util::PropertyMap &properties, const GeodeticCRSNNPtr &baseCRSIn, const operation::ConversionNNPtr &derivingConversionIn, const cs::CartesianCSNNPtr &csIn)

Instantiate a ProjectedCRS from a base CRS, a deriving operation::Conversion and a coordinate system.

Return new ProjectedCRS.

Parameters
- properties: See general_properties. At minimum the name should be defined.
- baseCRSIn: The base CRS, a GeodeticCRS that is generally a GeographicCRS.
- derivingConversionIn: The deriving operation::Conversion (typically using a map projection method)
- csIn: The coordinate system.

class SingleCRS : public osgeo::proj::crs::CRS

#include <crs.hpp> Abstract class modelling a coordinate reference system consisting of one Coordinate System and either one datum::Datum or one datum::DatumEnsemble.

Remark Implements SingleCRS from ISO_19111_2019

Subclassed by osgeo::proj::crs::DerivedCRS, osgeo::proj::crs::EngineeringCRS, osgeo::proj::crs::GeodeticCRS, osgeo::proj::crs::ParametricCRS, osgeo::proj::crs::TemporalCRS, osgeo::proj::crs::VerticalCRS
Public Functions

const datum::DatumPtr &datum()

Return the datum::Datum associated with the CRS.

This might be null, in which case datumEnsemble() return will not be null.

Return a Datum that might be null.

const datum::DatumEnsemblePtr &datumEnsemble()

Return the datum::DatumEnsemble associated with the CRS.

This might be null, in which case datum() return will not be null.

Return a DatumEnsemble that might be null.

const cs::CoordinateSystemNNPtr &coordinateSystem()

Return the cs::CoordinateSystem associated with the CRS.

This might be null, in which case datumEnsemble() return will not be null.

Return a CoordinateSystem that might be null.

class TemporalCRS : public virtual osgeo::proj::crs::SingleCRS
#include <crs.hpp> A coordinate reference system associated with a temporal datum and a one-dimensional temporal coordinate system.

Remark Implements TemporalCRS from ISO_19111_2019

Public Functions

const datum::TemporalDatumNNPtr datum() const

Return the datum::TemporalDatum associated with the CRS.

Return a TemporalDatum

const cs::TemporalCSNNPtr coordinateSystem() const

Return the cs::TemporalCS associated with the CRS.

Return a TemporalCS

Public Static Functions

TemporalCRSNNPtr create(const util::PropertyMap &properties, const datum::TemporalDatumNNPtr &datumIn, const cs::TemporalCSNNPtr &csIn)

Instantiate a TemporalCRS from a datum and a coordinate system.

Return new TemporalCRS.

Parameters
• properties: See general_properties. At minimum the name should be defined.
• datumIn: the datum.
• csIn: the coordinate system.

class VerticalCRS : public virtual osgeo::proj::crs::SingleCRS, public osgeo::proj::io::IPROJStringExportable
#include <crs.hpp> A coordinate reference system having a vertical reference frame and a one-dimensional vertical coordinate system used for recording gravity-related heights or depths.
Vertical CRSs make use of the direction of gravity to define the concept of height or depth, but the relationship with gravity may not be straightforward. If the vertical reference frame is dynamic or if the vertical CRS has an association to a velocity model then the CRS is dynamic, else it is static.

**Note** Ellipsoidal heights cannot be captured in a vertical coordinate reference system. They exist only as an inseparable part of a 3D coordinate tuple defined in a geographic 3D coordinate reference system.

**Remark** Implements VerticalCRS from ISO_19111_2019

Subclassed by osgeo::proj::crs::DerivedVerticalCRS

**Public Functions**

```cpp
const datum::VerticalReferenceFramePtr datum() const
    Return the datum::VerticalReferenceFrame associated with the CRS.
    Return a VerticalReferenceFrame.

const cs::VerticalCSNNPtr coordinateSystem() const
    Return the cs::VerticalCS associated with the CRS.
    Return a VerticalCS.

const std::vector<operation::TransformationNNPtr> &geoidModel() const
    Return the geoid model associated with the CRS.
    Geoid height model or height correction model linked to a geoid-based vertical CRS.
    Return a geoid model. might be null

const std::vector<operation::PointMotionOperationNNPtr> &velocityModel() const
    Return the velocity model associated with the CRS.
    Return a velocity model. might be null.
```

```cpp
std::list<std::pair<VerticalCRSNNPtr, int>> identify(const io::AuthorityFactoryPtr &authorityFactory) const
    Identify the CRS with reference CRSs.
    The candidate CRSs are looked in the database when authorityFactory is not null.
    The method returns a list of matching reference CRS, and the percentage (0-100) of confidence in the match. 100% means that the name of the reference entry perfectly matches the CRS name, and both are equivalent. In which case a single result is returned. 90% means that CRS are equivalent, but the names are not exactly the same. 70% means that CRS are equivalent (equivalent datum and coordinate system), but the names do not match at all. 25% means that the CRS are not equivalent, but there is some similarity in the names.
    Return a list of matching reference CRS, and the percentage (0-100) of confidence in the match.
    Parameters
    • authorityFactory: Authority factory (if null, will return an empty list)
```
Public Static Functions

VerticalCRSNNPtr create(const util::PropertyMap &properties, const datum::VerticalReferenceFrameNNPtr &datumIn, const cs::VerticalCSNNPtr &csIn)
Instantiate a VerticalCRS from a datum::VerticalReferenceFrame and a cs::VerticalCS.
Return new VerticalCRS.
Parameters
  • properties: See general_properties. At minimum the name should be defined.
  • datumIn: The datum of the CRS.
  • csIn: a VerticalCS.

VerticalCRSNNPtr create(const util::PropertyMap &properties, const datum::VerticalReferenceFramePtr &datumIn, const datum::DatumEnsemblePtr &datumEnsembleIn, const cs::VerticalCSNNPtr &csIn)
Instantiate a VerticalCRS from a datum::VerticalReferenceFrame or datum::DatumEnsemble and a cs::VerticalCS.
One and only one of datum or datumEnsemble should be set to a non-null value.
Return new VerticalCRS.
Parameters
  • properties: See general_properties. At minimum the name should be defined.
  • datumIn: The datum of the CRS, or nullptr
  • datumEnsembleIn: The datum ensemble of the CRS, or nullptr.
  • csIn: a VerticalCS.

10.5.3.8 operation namespace

namespace operation
Coordinate operations (relationship between any two coordinate reference systems).
osgeo.proj.operation namespace
This covers Conversion, Transformation, PointMotionOperation or ConcatenatedOperation.

Typedefs

typedef std::shared_ptr<CoordinateOperation> CoordinateOperationPtr
Shared pointer of CoordinateOperation

typedef util::nn<CoordinateOperationPtr> CoordinateOperationNNPtr
Non-null shared pointer of CoordinateOperation

using GeneralOperationParameterPtr = std::shared_ptr<GeneralOperationParameter>
Shared pointer of GeneralOperationParameter

using GeneralOperationParameterNNPtr = util::nn<GeneralOperationParameterPtr>
Non-null shared pointer of GeneralOperationParameter

using OperationParameterPtr = std::shared_ptr<OperationParameter>
Shared pointer of OperationParameter

using OperationParameterNNPtr = util::nn<OperationParameterPtr>
Non-null shared pointer of OperationParameter
using GeneralParameterValuePtr = std::shared_ptr<GeneralParameterValue>
    Shared pointer of GeneralParameterValue

using GeneralParameterValueNNPtr = util::nn<GeneralParameterValuePtr>
    Non-null shared pointer of GeneralParameterValue

using ParameterValuePtr = std::shared_ptr<ParameterValue>
    Shared pointer of ParameterValue

using ParameterValueNNPtr = util::nn<ParameterValuePtr>
    Non-null shared pointer of ParameterValue

using OperationParameterValuePtr = std::shared_ptr<OperationParameterValue>
    Shared pointer of OperationParameterValue

using OperationParameterValueNNPtr = util::nn<OperationParameterValuePtr>
    Non-null shared pointer of OperationParameterValue

using OperationMethodPtr = std::shared_ptr<OperationMethod>
    Shared pointer of OperationMethod

using OperationMethodNNPtr = util::nn<OperationMethodPtr>
    Non-null shared pointer of OperationMethod

using SingleOperationPtr = std::shared_ptr<SingleOperation>
    Shared pointer of SingleOperation

using SingleOperationNNPtr = util::nn<SingleOperationPtr>
    Non-null shared pointer of SingleOperation

typedef std::shared_ptr<Conversion> ConversionPtr
    Shared pointer of Conversion

typedef util::nn<ConversionPtr> ConversionNNPtr
    Non-null shared pointer of Conversion

using TransformationPtr = std::shared_ptr<Transformation>
    Shared pointer of Transformation

using TransformationNNPtr = util::nn<TransformationPtr>
    Non-null shared pointer of Transformation

using PointMotionOperationPtr = std::shared_ptr<PointMotionOperation>
    Shared pointer of PointMotionOperation

using PointMotionOperationNNPtr = util::nn<PointMotionOperationPtr>
    Non-null shared pointer of PointMotionOperation

using ConcatenatedOperationPtr = std::shared_ptr<ConcatenatedOperation>
    Shared pointer of ConcatenatedOperation

using ConcatenatedOperationNNPtr = util::nn<ConcatenatedOperationPtr>
    Non-null shared pointer of ConcatenatedOperation

using CoordinateOperationContextPtr = std::unique_ptr<CoordinateOperationContext>
    Unique pointer of CoordinateOperationContext

using CoordinateOperationContextNNPtr = util::nn<CoordinateOperationContextPtr>
    Non-null unique pointer of CoordinateOperationContext

using CoordinateOperationFactoryPtr = std::unique_ptr<CoordinateOperationFactory>
    Unique pointer of CoordinateOperationFactory
using CoordinateOperationFactoryNNPtr = util::nn<CoordinateOperationFactoryPtr>
Non-null unique pointer of CoordinateOperationFactory

Functions

static const char *getCRSQualifierStr (const crs::CRSPtr &crs)
static std::string buildOpName (const char *opType, const crs::CRSPtr &source, const crs::CRSPtr &target)
static util::PropertyMap createPropertiesForInverse (const CoordinateOperation *op, bool derivedFrom, bool approximateInversion)
static bool isTimeDependent (const std::string &methodName)
static double negate (double val)
static CoordinateOperationPtr createApproximateInverseIfPossible (const Transformation *op)
static void exportSourceCRSAndTargetCRSToWKT (const CoordinateOperation *co, io::WKTFormatter *formatter)
static crs::CRSNNPtr getResolvedCRS (const crs::CRSNNPtr &crs, const CoordinateOperationContextNNPtr &context)

class ConcatenatedOperation : public osgeo::proj::operation::CoordinateOperation
#include <coordinateoperation.hpp> An ordered sequence of two or more single coordinate operations (SingleOperation).

The sequence of coordinate operations is constrained by the requirement that the source coordinate reference system of step n+1 shall be the same as the target coordinate reference system of step n.

Remark Implements ConcatenatedOperation from ISO_19111_2019

Public Functions

const std::vector<CoordinateOperationNNPtr> &operations () const
Return the operation steps of the concatenated operation.

CoordinateOperationNNPtr inverse () const
Return the inverse of the coordinate operation.

Exceptions
• util::UnsupportedOperationException:

std::set<GridDescription> gridsNeeded (const io::DatabaseContextPtr &databaseContext)
Return grids needed by an operation.
### Public Static Functions

*ConcatenatedOperationNNPtr create(const util::PropertyMap &properties, const std::vector<CoordinateOperationNNPtr> &operationsIn, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)*

Instantiate a *ConcatenatedOperation*.

**Return** new *Transformation*.

**Parameters**

- *properties*: See *general_properties*. At minimum the name should be defined.
- *operationsIn*: Vector of the *CoordinateOperation* steps.
- *accuracies*: Vector of positional accuracy (might be empty).

**Exceptions**

- *InvalidOperation*:

*CoordinateOperationNNPtr createComputeMetadata(const std::vector<CoordinateOperationNNPtr> &operationsIn, bool checkExtent)*

Instantiate a *ConcatenatedOperation*, or return a single coordinate operation.

This computes its accuracy from the sum of its member operations, its extent

**Parameters**

- *operationsIn*: Vector of the *CoordinateOperation* steps.
- *checkExtent*: Whether we should check the non-emptyness of the intersection of the extents of the operations

**Exceptions**

- *InvalidOperation*:

### class Conversion : public osgeo::proj::operation::SingleOperation

`#include <coordinateoperation.hpp>` A mathematical operation on coordinates in which the parameter values are defined rather than empirically derived.

Application of the coordinate conversion introduces no error into output coordinates. The best-known example of a coordinate conversion is a map projection. For coordinate conversions the output coordinates are referenced to the same datum as are the input coordinates.

Coordinate conversions forming a component of a derived CRS have a source *crs::CRS* and a target *crs::CRS* that are NOT specified through the source and target associations, but through associations from *crs::DerivedCRS* to *crs::SingleCRS*.

**Remark** Implements *Conversion* from *ISO_19111_2019*

### Public Functions

*CoordinateOperationNNPtr inverse() const*

Return the inverse of the coordinate operation.

**Exceptions**

- *util::UnsupportedOperationException*:

bool *isUTM* (int &zone, bool &north) const

Return whether a conversion is a Universal Transverse Mercator conversion.

**Return** true if it is a UTM conversion.

**Parameters**
• [out] zone: UTM zone number between 1 and 60.
• [out] north: true for UTM northern hemisphere, false for UTM southern hemisphere.

ConversionNNPtr identify() const
Return a Conversion object where some parameters are better identified.

Return a new Conversion.

ConversionPtr convertToOtherMethod (int targetEPSGCode) const
Return an equivalent projection.
Currently implemented:
• EPSG_CODE_METHOD_MERCATOR_VARIANT_A (1SP) to
  EPSG_CODE_METHOD_MERCATOR_VARIANT_B (2SP)
• EPSG_CODE_METHOD_MERCATOR_VARIANT_B (2SP) to
  EPSG_CODE_METHOD_MERCATOR_VARIANT_A (1SP)
• EPSG_CODE_METHOD_LAMBERT_CONIC_CONFORMAL_1SP
  to
  EPSG_CODE_METHOD_LAMBERT_CONIC_CONFORMAL_2SP
• EPSG_CODE_METHOD_LAMBERT_CONIC_CONFORMAL_2SP
  to
  EPSG_CODE_METHOD_LAMBERT_CONIC_CONFORMAL_1SP

Return new conversion, or nullptr
Parameters
• targetEPSGCode: EPSG code of the target method.

Public Static Functions

ConversionNNPtr create (const util::PropertyMap &properties,
  const OperationMethodNNPtr &methodIn,
  const std::vector<GeneralParameterValueNNPtr> &values)
Instantiate a Conversion from a vector of GeneralParameterValue.

Return a new Conversion.
Parameters
• properties: See general_properties. At minimum the name should be defined.
• methodIn: the operation method.
• values: the values.
Exceptions
• InvalidOperation:

ConversionNNPtr create (const util::PropertyMap &propertiesConversion,
  const util::PropertyMap &propertiesOperationMethod,
  const std::vector<OperationParameterNNPtr> &parameters,
  const std::vector<ParameterValueNNPtr> &values)
Instantiate a Conversion and its OperationMethod.

Return a new Conversion.
Parameters
• propertiesConversion: See general_properties of the conversion. At minimum the name should be defined.
• propertiesOperationMethod: See general_properties of the operation method. At minimum the name should be defined.
• parameters: the operation parameters.
• values: the operation values. Constraint: values.size() == parameters.size()
Exceptions
• InvalidOperation:
\textit{ConversionNNPtr createUTM} (const \textit{util::PropertyMap} &\textit{properties}, int \textit{zone}, bool \textit{north})

Instantiate a Universal Transverse Mercator conversion.

UTM is a family of conversions, of EPSG codes from 16001 to 16060 for the northern hemisphere, and 17001 to 17060 for the southern hemisphere, based on the Transverse Mercator projection method.

Return a new Conversion.

Parameters

• \textit{properties}: See \textit{general_properties} of the conversion. If the name is not provided, it is automatically set.
• \textit{zone}: UTM zone number between 1 and 60.
• \textit{north}: true for UTM northern hemisphere, false for UTM southern hemisphere.

\textit{ConversionNNPtr createTransverseMercator} (const \textit{util::PropertyMap} &\textit{properties},
\textit{const common::Angle} &\textit{centerLat}, \textit{const common::Angle} &\textit{centerLong}, \textit{const common::Scale} &\textit{scale}, \textit{const common::Length} \textit{falseEasting}, \textit{const common::Length} \textit{falseNorthing})

Instantiate a conversion based on the Transverse Mercator projection method.

This method is defined as EPSG:9807

Return a new Conversion.

Parameters

• \textit{properties}: See \textit{general_properties} of the conversion. If the name is not provided, it is automatically set.
• \textit{centerLat}: See Latitude of natural origin/Center Latitude
• \textit{centerLong}: See Longitude of natural origin/Central Meridian
• \textit{scale}: See Scale Factor
• \textit{falseEasting}: See False Easting
• \textit{falseNorthing}: See False Northing

\textit{ConversionNNPtr createGaussSchreiberTransverseMercator} (const \textit{util::PropertyMap} &\textit{properties}, \textit{const common::Angle} &\textit{centerLat}, \textit{const common::Angle} &\textit{centerLong}, \textit{const common::Scale} &\textit{scale}, \textit{const common::Length} \textit{falseEasting}, \textit{const common::Length} \textit{falseNorthing})

Instantiate a conversion based on the Gauss Schreiber Transverse Mercator projection method.

This method is also known as Gauss-Laborde Reunion.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters

• \textit{properties}: See \textit{general_properties} of the conversion. If the name is not provided, it is automatically set.
• \textit{centerLat}: See Latitude of natural origin/Center Latitude
• \textit{centerLong}: See Longitude of natural origin/Central Meridian
- `scale`: See Scale Factor
- `falseEastling`: See False Easting
- `falseNorthing`: See False Northing

`ConversionNNPtr createTransverseMercatorSouthOriented(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Scale &scale, const common::Length &falseEasting, const common::Length &falseNorthing)`

Instantiate a conversion based on the Transverse Mercator South Orientated projection method.

This method is defined as EPSG:9808

**Return** a new `Conversion`.

**Parameters**
- `properties`: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
- `centerLat`: See Latitude of natural origin/Center Latitude
- `centerLong`: See Longitude of natural origin/Central Meridian
- `scale`: See Scale Factor
- `falseEastling`: See False Easting
- `falseNorthing`: See False Northing

`ConversionNNPtr createTwoPointEquidistant(const util::PropertyMap &properties, const common::Angle &latitudeFirstPoint, const common::Angle &longitudeFirstPoint, const common::Angle &latitudeSecondPoint, const common::Angle &longitudeSecondPoint, const common::Length &falseEasting, const common::Length &falseNorthing)`

Instantiate a conversion based on the Two Point Equidistant projection method.

There is no equivalent in EPSG.

**Return** a new `Conversion`.

**Parameters**
- `properties`: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
- `latitudeFirstPoint`: Latitude of first point.
- `longitudeFirstPoint`: Longitude of first point.
- `latitudeSecondPoint`: Latitude of second point.
- `longitudeSecondPoint`: Longitude of second point.
- `falseEastling`: See False Easting
- `falseNorthing`: See False Northing
ConversionNNPtr createTunisiaMappingGrid(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Tunisia Mapping Grid projection method.

This method is defined as EPSG:9816

Note There is currently no implementation of the method formulas in PROJ.

Return a new Conversion.

Parameters
• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLat: See Latitude of natural origin/Center Latitude
• centerLong: See Longitude of natural origin/Central Meridian
• falseEasting: See False Easting
• falseNorthing: See False Northing

ConversionNNPtr createAlbersEqualArea(const util::PropertyMap &properties, const common::Angle &latitudeFalseOrigin, const common::Angle &longitudeFalseOrigin, const common::Angle &latitudeFirstParallel, const common::Angle &latitudeSecondParallel, const common::Length &eastingFalseOrigin, const common::Length &northingFalseOrigin)

Instantiate a conversion based on the Albers Conic Equal Area projection method.

This method is defined as EPSG:9822

Note the order of arguments is conformant with the corresponding EPSG mode and different than OGRSpatialReference::setACEA() of GDAL <= 2.3

Return a new Conversion.

Parameters
• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• latitudeFalseOrigin: See Latitude of false origin
• longitudeFalseOrigin: See Longitude of false origin
• latitudeFirstParallel: See Latitude of 1st standard parallel
• latitudeSecondParallel: See Latitude of 2nd standard parallel
• eastingFalseOrigin: See Easting of false origin
• northingFalseOrigin: See Northing of false origin

ConversionNNPtr createLambertConicConformal_1SP(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Scale &scale, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Lambert Conic Conformal 1SP projection method.

This method is defined as EPSG:9801

Return a new Conversion.

Parameters
• properties: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
• centerLat: See Latitude of natural origin/Center Latitude
• centerLong: See Longitude of natural origin/Central Meridian
• scale: See Scale Factor
• falseEasting: See False Easting
• falseNorthing: See False Northing

```cpp
ConversionNNPtr createLambertConicConformal_2SP (const util::PropertyMap &properties, const common::Angle &latitudeFalseOrigin, const common::Angle &longitudeFalseOrigin, const common::Angle &latitudeFirstParallel, const common::Angle &latitudeSecondParallel, const common::Length &eastingFalseOrigin, const common::Length &northingFalseOrigin)
```

Instantiate a conversion based on the Lambert Conic Conformal (2SP) projection method.

This method is defined as EPSG:9802

**Note** the order of arguments is conformant with the corresponding EPSG mode and different than `OGRSpatialReference::setLCC()` of GDAL <= 2.3

Return a new `Conversion`.

**Parameters**

- properties: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
- latitudeFalseOrigin: See Latitude of false origin
- longitudeFalseOrigin: See Longitude of false origin
- latitudeFirstParallel: See Latitude of 1st standard parallel
- latitudeSecondParallel: See Latitude of 2nd standard parallel
- eastingFalseOrigin: See Easting of false origin
- northingFalseOrigin: See Northing of false origin
**Conversion** \( \text{createLambertConicConformal}_2 \text{SP}_ \text{Michigan} \) \{const

\begin{verbatim}
util::PropertyMap &properties, const
common::Angle &latitudeFalse-Origin, const
common::Angle &longitudeFalse-Origin, const
common::Angle &latitudeFirst-Parallel, const
common::Angle &latitudeSecond-Parallel, const
common::Length &eastingFalse-Origin, const
common::Length &northingFalse-Origin, const
common::Scale &ellipsoidScaling-Factor
\end{verbatim}

Instantiate a conversion based on the Lambert Conic Conformal (2SP Michigan) projection method. This method is defined as EPSG:1051

**Return** a new **Conversion**.

**Parameters**

- `properties`: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
- `latitudeFalseOrigin`: See Latitude of false origin
- `longitudeFalseOrigin`: See Longitude of false origin
- `latitudeFirstParallel`: See Latitude of 1st standard parallel
- `latitudeSecondParallel`: See Latitude of 2nd standard parallel
- `eastingFalseOrigin`: See Easting of false origin
- `northingFalseOrigin`: See Northing of false origin
- `ellipsoidScalingFactor`: Ellipsoid scaling factor.
**ConversionNNPtr createLambertConicConformal_2SP_Belgium** (const 
util::PropertyMap &properties, const 
common::Angle &latitudeFalse-Origin, const 
common::Angle &longitudeFalse-Origin, const 
common::Angle &latitudeFirst-Parallel, const 
common::Angle &latitudeSecond-Parallel, const 
common::Length &eastingFalse-Origin, const 
common::Length &northingFalseOrigin)

Instantiate a conversion based on the **Lambert Conic Conformal (2SP Belgium)** projection method.

This method is defined as **EPSG:9803**

**Warning** The formulas used currently in PROJ are, incorrectly, the ones of the regular LCC_2SP method.

**Note** the order of arguments is conformant with the corresponding EPSG mode and different than **OGRSpatialReference::setLCCB**() of GDAL <= 2.3

**Return** a new **Conversion**.

**Parameters**
- properties: See **general_properties** of the conversion. If the name is not provided, it is automatically set.
- latitudeFalseOrigin: See Latitude of false origin
- longitudeFalseOrigin: See Longitude of false origin
- latitudeFirstParallel: See Latitude of 1st standard parallel
- latitudeSecondParallel: See Latitude of 2nd standard parallel
- eastingFalseOrigin: See Easting of false origin
- northingFalseOrigin: See Northing of false origin

**ConversionNNPtr createAzimuthalEquidistant** (const 
util::PropertyMap &properties, 
const common::Angle &latitudeNatOrigin, const common::Angle &longitudeNatOrigin, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the **Modified Azimuthal Equidistant** projection method.

This method is defined as **EPSG:9832**

**Return** a new **Conversion**.

**Parameters**
- properties: See **general_properties** of the conversion. If the name is not provided, it is automatically set.
- latitudeNatOrigin: See Latitude of natural origin/Center Latitude
- longitudeNatOrigin: See Longitude of natural origin/Central Meridian
- falseEasting: See False Easting
- `falseNorthing`: See False Northing

\[
\text{ConversionNNPtr createGuamProjection}(\text{const util::PropertyMap &properties, const common::Angle &latitudeNatOrigin, const common::Angle &longitudeNatOrigin, const common::Length &falseEasting, const common::Length &falseNorthing})
\]

Instantiate a conversion based on the Guam Projection projection method.

This method is defined as EPSG:9831

Return a new `Conversion`.

Parameters

- `properties`: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
- `latitudeNatOrigin`: See Latitude of natural origin/Center Latitude
- `longitudeNatOrigin`: See Longitude of natural origin/Central Meridian
- `falseEasting`: See False Easting
- `falseNorthing`: See False Northing

\[
\text{ConversionNNPtr createBonne}(\text{const util::PropertyMap &properties, const common::Angle &latitudeNatOrigin, const common::Angle &longitudeNatOrigin, const common::Length &falseEasting, const common::Length &falseNorthing})
\]

Instantiate a conversion based on the Bonne projection method.

This method is defined as EPSG:9827

Return a new `Conversion`.

Parameters

- `properties`: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
- `latitudeNatOrigin`: See Latitude of natural origin/Center Latitude. PROJ calls its the standard parallel 1.
- `longitudeNatOrigin`: See Longitude of natural origin/Central Meridian
- `falseEasting`: See False Easting
- `falseNorthing`: See False Northing

\[
\text{ConversionNNPtr createLambertCylindricalEqualAreaSpherical}(\text{const util::PropertyMap &properties, const common::Angle &latitudeFirstParallel, const common::Angle &longitudeNatOrigin, const common::Length &falseEasting, const common::Length &falseNorthing})
\]

Instantiate a conversion based on the Lambert Cylindrical Equal Area (Spherical) projection method.

This method is defined as EPSG:9834
**Warning** The PROJ cea computation code would select the ellipsoidal form if a non-spherical ellipsoid is used for the base GeographicalCRS.

**Return** a new Conversion.

**Parameters**
- properties: See *general_properties* of the conversion. If the name is not provided, it is automatically set.
- latitudeFirstParallel: See Latitude of 1st standard parallel.
- longitudeNatOrigin: See Longitude of natural origin/Central Meridian
- falseEasting: See False Easting
- falseNorthing: See False Northing

```cpp
ConversionNNPtr createLambertCylindricalEqualArea(const util::PropertyMap &properties, const common::Angle &latitudeFirstParallel, const common::Angle &longitudeNatOrigin, const common::Length &falseEasting, const common::Length &falseNorthing)
```

Instantiate a conversion based on the Lambert Cylindrical Equal Area (ellipsoidal form) projection method.

This method is defined as EPSG:9835

**Return** a new Conversion.

**Parameters**
- properties: See *general_properties* of the conversion. If the name is not provided, it is automatically set.
- centerLat: See Latitude of natural origin/Center Latitude
- centerLong: See Longitude of natural origin/Central Meridian
- falseEasting: See False Easting
- falseNorthing: See False Northing

```cpp
ConversionNNPtr createCassiniSoldner(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)
```

Instantiate a conversion based on the Cassini-Soldner projection method.

This method is defined as EPSG:9806

**Return** a new Conversion.

**Parameters**
- properties: See *general_properties* of the conversion. If the name is not provided, it is automatically set.
- centerLat: See Latitude of natural origin/Center Latitude
- centerLong: See Longitude of natural origin/Central Meridian
- falseEasting: See False Easting
- falseNorthing: See False Northing
ConversionNNPtr createEquidistantConic(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Angle &latitudeFirstParallel, const common::Angle &latitudeSecondParallel, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Equidistant Conic projection method.

There is no equivalent in EPSG.

Note Although not found in EPSG, the order of arguments is conformant with the “spirit” of EPSG and different than OGRSpatialReference::setEC() of GDAL <= 2.3 *

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLat: See Latitude of natural origin/Center Latitude
• centerLong: See Longitude of natural origin/Central Meridian
• latitudeFirstParallel: See Latitude of 1st standard parallel
• latitudeSecondParallel: See Latitude of 2nd standard parallel
• falseEasting: See False Easting
• falseNorthing: See False Northing

ConversionNNPtr createEckertI(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Eckert I projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEasting: See False Easting
• falseNorthing: See False Northing

ConversionNNPtr createEckertII(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Eckert II projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEasting: See False Easting
• falseNorthing: See False Northing

ConversionNNPtr createEckertIII(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Eckert III projection method.
There is no equivalent in EPSG.

**Return** a new *Conversion*.

**Parameters**

- **properties**: See *general_properties* of the conversion. If the name is not provided, it is automatically set.
- **centerLong**: See Longitude of natural origin/Central Meridian
- **falseEasting**: See False Easting
- **falseNorthing**: See False Northing

`ConversionNPtr createEckertIV(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)`

Instantiate a conversion based on the Eckert IV projection method.

There is no equivalent in EPSG.

**Return** a new *Conversion*.

**Parameters**

- **properties**: See *general_properties* of the conversion. If the name is not provided, it is automatically set.
- **centerLong**: See Longitude of natural origin/Central Meridian
- **falseEasting**: See False Easting
- **falseNorthing**: See False Northing

`ConversionNPtr createEckertV(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)`

Instantiate a conversion based on the Eckert V projection method.

There is no equivalent in EPSG.

**Return** a new *Conversion*.

**Parameters**

- **properties**: See *general_properties* of the conversion. If the name is not provided, it is automatically set.
- **centerLong**: See Longitude of natural origin/Central Meridian
- **falseEasting**: See False Easting
- **falseNorthing**: See False Northing

`ConversionNPtr createEckertVI(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)`

Instantiate a conversion based on the Eckert VI projection method.

There is no equivalent in EPSG.

**Return** a new *Conversion*.

**Parameters**

- **properties**: See *general_properties* of the conversion. If the name is not provided, it is automatically set.
- **centerLong**: See Longitude of natural origin/Central Meridian
- **falseEasting**: See False Easting
- **falseNorthing**: See False Northing
ConversionNNPtr createEquidistantCylindrical(const util::PropertyMap &properties, const common::Angle &latitudeFirstParallel, const common::Angle &longitudeNatOrigin, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Equidistant Cylindrical projection method.

This is also known as the Equirectangular method, and in the particular case where the latitude of first parallel is 0.

This method is defined as EPSG:1028

Note This is the equivalent OGRSpatialReference::SetEquirectangular2( 0.0, latitudeFirstParallel, falseEasting, falseNorthing ) of GDAL <= 2.3, where the lat_0 / center_latitude parameter is forced to 0.

Return a new Conversion.

Parameters

- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- latitudeFirstParallel: See Latitude of 1st standard parallel.
- longitudeNatOrigin: See Longitude of natural origin/Central Meridian
- falseEasting: See False Easting
- falseNorthing: See False Northing

ConversionNNPtr createEquidistantCylindricalSpherical(const util::PropertyMap &properties, const common::Angle &latitudeFirstParallel, const common::Angle &longitudeNatOrigin, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Equidistant Cylindrical (Spherical) projection method.

This is also known as the Equirectangular method, and in the particular case where the latitude of first parallel is 0.

This method is defined as EPSG:1029

Note This is the equivalent OGRSpatialReference::SetEquirectangular2( 0.0, latitudeFirstParallel, falseEasting, falseNorthing ) of GDAL <= 2.3, where the lat_0 / center_latitude parameter is forced to 0.

Return a new Conversion.

Parameters

- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- latitudeFirstParallel: See Latitude of 1st standard parallel.
- longitudeNatOrigin: See Longitude of natural origin/Central Meridian
- falseEasting: See False Easting
- falseNorthing: See False Northing
ConversionNNPtr createGall(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Gall (Stereographic) projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEasting: See False Easting
• falseNorthing: See False Northing

ConversionNNPtr createGoodeHomolosine(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Goode Homolosine projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEasting: See False Easting
• falseNorthing: See False Northing

ConversionNNPtr createInterruptedGoodeHomolosine(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Interrupted Goode Homolosine projection method.

There is no equivalent in EPSG.

Note OGRSpatialReference::SetIGH() of GDAL <= 2.3 assumes the 3 projection parameters to be zero and this is the nominal case.

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEasting: See False Easting
• falseNorthing: See False Northing

ConversionNNPtr createGeostationarySatelliteSweepX(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &height, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Geostationary Satellite View projection method, with the sweep angle axis of the viewing instrument being $x$.

There is no equivalent in EPSG.

**Return** a new *Conversion*.

**Parameters**

- *properties*: See *general_properties* of the conversion. If the name is not provided, it is automatically set.
- *centerLong*: See Longitude of natural origin/Central Meridian
- *height*: Height of the view point above the Earth.
- *falseEastIng*: See False Easting
- *falseNorthing*: See False Northing

```cpp
ConversionNNPtr createGeostationarySatelliteSweepX(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &height, const common::Length &falseEastIng, const common::Length &falseNorthing)
```

Instantiate a conversion based on the Geostationary Satellite View projection method, with the sweep angle axis of the viewing instrument being $y$.

There is no equivalent in EPSG.

**Return** a new *Conversion*.

**Parameters**

- *properties*: See *general_properties* of the conversion. If the name is not provided, it is automatically set.
- *centerLat*: See Latitude of natural origin/Center Latitude
- *centerLong*: See Longitude of natural origin/Central Meridian
- *falseEastIng*: See False Easting
- *falseNorthing*: See False Northing

```cpp
ConversionNNPtr createGnomonic(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Length &falseEastIng, const common::Length &falseNorthing)
```

Instantiate a conversion based on the Gnomonic projection method.

There is no equivalent in EPSG.

**Return** a new *Conversion*.

**Parameters**

- *properties*: See *general_properties* of the conversion. If the name is not provided, it is automatically set.
- *centerLat*: See Latitude of natural origin/Center Latitude
- *centerLong*: See Longitude of natural origin/Central Meridian
- *falseEastIng*: See False Easting
- *falseNorthing*: See False Northing
ConversionNNPtr createHotineObliqueMercatorVariantA(
    const util::PropertyMap &properties,
    const common::Angle &latitudeProjectionCentre,
    const common::Angle &longitudeProjectionCentre,
    const common::Angle &azimuthInitialLine,
    const common::Angle &angleFromRectifiedToSkewGrid,
    const common::Scale &scale,
    const common::Length &falseEasting,
    const common::Length &falseNorthing)

Instantiate a conversion based on the Hotine Oblique Mercator (Variant A) projection method.

This is the variant with the no_uoff parameter, which corresponds to GDAL >=2.3 Hotine_Oblique_Mercator projection. In this variant, the false grid coordinates are defined at the intersection of the initial line and the aposphere (the equator on one of the intermediate surfaces inherent in the method), that is at the natural origin of the coordinate system.

This method is defined as EPSG:9812

**Note** In the case where azimuthInitialLine = angleFromRectifiedToSkewGrid = 90deg, this maps to the Swiss Oblique Mercator formulas.

**Return** a new Conversion.

**Parameters**

- **properties**: See general_properties of the conversion. If the name is not provided, it is automatically set.
- **latitudeProjectionCentre**: See Latitude of projection centre
- **longitudeProjectionCentre**: See Longitude of projection centre
- **azimuthInitialLine**: See Azimuth of initial line
- **angleFromRectifiedToSkewGrid**: See Angle from Rectified to Skew Grid
- **scale**: See Scale factor on initial line
- **falseEasting**: See False Easting
- **falseNorthing**: See False Northing

ConversionNNPtr createHotineObliqueMercatorVariantB(
    const util::PropertyMap &properties,
    const common::Angle &latitudeProjectionCentre,
    const common::Angle &longitudeProjectionCentre,
    const common::Angle &azimuthInitialLine,
    const common::Angle &angleFromRectifiedToSkewGrid,
    const common::Scale &scale,
    const common::Length &eastingProjectionCentre,
    const common::Length &northingProjectionCentre)

Instantiate a conversion based on the Hotine Oblique Mercator (Variant B) projection method.
This is the variant without the no_uoff parameter, which corresponds to GDAL $\geq 2.3$ Hotine_Oblique_Mercator_Azimuth_Center projection. In this variant, the false grid coordinates are defined at the projection centre.

This method is defined as **EPSG:9815**

**Note** In the case where azimuthInitialLine = angleFromRectifiedToSkrewGrid = 90deg, this maps to the Swiss Oblique Mercator formulas.

**Return** a new Conversion.

**Parameters**
- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- latitudeProjectionCentre: See Latitude of projection centre
- longitudeProjectionCentre: See Longitude of projection centre
- azimuthInitialLine: See Azimuth of initial line
- angleFromRectifiedToSkrewGrid: See Angle from Rectified to Skew Grid
- scale: See Scale factor on initial line
- eastingProjectionCentre: See Easting at projection centre
- northingProjectionCentre: See Northing at projection centre
ConversionNNPtr createHotineObliqueMercatorTwoPointNaturalOrigin(const util::PropertyMap &properties,
const common::Angle &latitudeProjectionCentre,
const common::Angle &latitudePoint1,
const common::Angle &longitudePoint1,
const common::Angle &latitudePoint2,
const common::Scale &scale,
const common::Length &eastProjeetionCentre,
const common::Length &northingProjectionCentre)
Instantiate a conversion based on the Hotine Oblique Mercator Two Point Natural Origin projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters

- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- latitudeProjectionCentre: See Latitude of projection centre
- latitudePoint1: Latitude of point 1.
- longitudePoint1: Longitude of point 1.
- latitudePoint2: Latitude of point 2.
- longitudePoint2: Longitude of point 2.
- scale: See Scale factor on initial line
- eastingProjectionCentre: See Easting at projection centre
- northingProjectionCentre: See Northing at projection centre

ConversionNNPtr createLabordeObliqueMercator(const util::PropertyMap &properties, const common::Angle &latitudeProjectionCentre, const common::Angle &latitudePoint1, const common::Angle &longitudeProjectionCentre, const common::Angle &azimuthInitialLine, const common::Scale &scale, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Laborde Oblique Mercator projection method.

This method is defined as EPSG:9813

Return a new Conversion.

Parameters

- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- latitudeProjectionCentre: See Latitude of projection centre
- longitudeProjectionCentre: See Longitude of projection centre
- azimuthInitialLine: See Azimuth of initial line
- scale: See Scale factor on initial line
- falseEasting: See False Easting
- falseNorthing: See False Northing

ConversionNNPtr createInternationalMapWorldPolyconic(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Angle &latitudeFirstParallel, const common::Angle &latitudeSecondParallel, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the International Map of the World Polyconic projection method.

There is no equivalent in EPSG.
Note the order of arguments is conformant with the corresponding EPSG mode and different than OGRSpatialReference::SetWMPolyconic() of GDAL <= 2.3

Return a new Conversion.

Parameters

- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- centerLong: See Longitude of natural origin/Central Meridian
- latitudeFirstParallel: See Latitude of 1st standard parallel
- latitudeSecondParallel: See Latitude of 2nd standard parallel
- falseEasting: See False Easting
- falseNorthing: See False Northing

ConversionNNPtr createKrovakNorthOriented(const util::PropertyMap &properties, const common::Angle &latitudeProjectionCentre, const common::Angle &longitudeOfOrigin, const common::Angle &colatitudeConeAxis, const common::Angle &latitudePseudoStandardParallel, const common::Scale &scaleFactorPseudoStandardParallel, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Krovak (north oriented) projection method.

This method is defined as EPSG:1041

The coordinates are returned in the “GIS friendly” order: easting, northing. This method is similar to createKrovak(), except that the later returns projected values as southing, westing, where southing(Krovak) = -northing(Krovak_North) and westing(Krovak) = -easting(Krovak_North).

Note The current PROJ implementation of Krovak hard-codes colatitudeConeAxis = 30deg17’17.30311" and latitudePseudoStandardParallel = 78deg30’N, which are the values used for the ProjectedCRS S-JTSK (Ferro) / Krovak East North (EPSG:5221). It also hard-codes the parameters of the Bessel ellipsoid typically used for Krovak.

Return a new Conversion.

Parameters

- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- latitudeProjectionCentre: See Latitude of projection centre
- longitudeOfOrigin: See Longitude of origin
- colatitudeConeAxis: See Co-latitude of cone axis
- latitudePseudoStandardParallel: See Latitude of pseudo standard
- scaleFactorPseudoStandardParallel: See Scale factor on pseudo
- falseEasting: See False Easting
- falseNorthing: See False Northing

ConversionNNPtr createKrovak(const util::PropertyMap &properties, const common::Angle &latitudeProjectionCentre, const common::Angle &longitudeOfOrigin, const common::Angle &colatitudeConeAxis, const common::Angle &latitudePseudoStandardParallel, const common::Scale &scaleFactorPseudoStandardParallel, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Krovak projection method.

This method is defined as EPSG:9819
The coordinates are returned in the historical order: southing, westing. This method is similar to `createKrovakNorthOriented()`, except that the later returns projected values as easting, northing, where easting(Krovak_North) = -westing(Krovak) and northing(Krovak_North) = -southing(Krovak).

**Note** The current PROJ implementation of Krovak hard-codes colatitudeConeAxis = 30deg17’17.30311” and latitudePseudoStandardParallel = 78deg30’N, which are the values used for the ProjectedCRS S-JTSK (Ferro) / Krovak East North (EPSG:5221). It also hard-codes the parameters of the Bessel ellipsoid typically used for Krovak.

Return a new `Conversion`.

**Parameters**
- `properties`: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
  - `latitudeProjectionCentre`: See Latitude of projection centre
  - `longitudeOfOrigin`: See Longitude of origin
  - `colatitudeConeAxis`: See Co-latitude of cone axis
  - `latitudePseudoStandardParallel`: See Latitude of pseudo standard
  - `scaleFactorPseudoStandardParallel`: See Scale factor on pseudo
  - `falseEasting`: See False Easting
  - `falseNorthing`: See False Northing

`ConversionNNPtr createLambertAzimuthalEqualArea(const util::PropertyMap &properties, const common::Angle &latitudeNatOrigin, const common::Angle &longitudeNatOrigin, const common::Length &falseEasting, const common::Length &falseNorthing)`

Instantiate a conversion based on the Lambert Azimuthal Equal Area projection method.

This method is defined as EPSG:9820

Return a new `Conversion`.

**Parameters**
- `properties`: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
  - `latitudeNatOrigin`: See Latitude of natural origin/Center Latitude
  - `longitudeNatOrigin`: See Longitude of natural origin/Central Meridian
  - `falseEasting`: See False Easting
  - `falseNorthing`: See False Northing

`ConversionNNPtr createMillerCylindrical(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)`

Instantiate a conversion based on the Miller Cylindrical projection method.

There is no equivalent in EPSG.

Return a new `Conversion`.

**Parameters**
- `properties`: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
  - `centerLong`: See Longitude of natural origin/Central Meridian
  - `falseEasting`: See False Easting
  - `falseNorthing`: See False Northing
ConversionNNPtr createMercatorVariantA(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Scale &scale, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Mercator projection method.

This is the variant, also known as Mercator (1SP), defined with the scale factor. Note that latitude of natural origin (centerLat) is a parameter, but unused in the transformation formulas.

This method is defined as EPSG:9804

Return a new Conversion.

Parameters
• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLat: See Latitude of natural origin/Center Latitude. Should be 0.
• centerLong: See Longitude of natural origin/Central Meridian
• scale: See Scale Factor
• falseEasting: See False Easting
• falseNorthing: See False Northing

ConversionNNPtr createMercatorVariantB(const util::PropertyMap &properties, const common::Angle &latitudeFirstParallel, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Mercator projection method.

This is the variant, also known as Mercator (2SP), defined with the latitude of the first standard parallel (the second standard parallel is implicitly the opposite value). The latitude of natural origin is fixed to zero.

This method is defined as EPSG:9805

Return a new Conversion.

Parameters
• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• latitudeFirstParallel: See Latitude of 1st standard parallel
• centerLong: See Longitude of natural origin/Central Meridian
• falseEasting: See False Easting
• falseNorthing: See False Northing

ConversionNNPtr createPopularVisualisationPseudoMercator(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

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Instantiate a conversion based on the Popular Visualisation Pseudo Mercator projection method.

Also known as WebMercator. Mostly/only used for Projected CRS EPSG:3857 (WGS 84 / Pseudo-Mercator)

This method is defined as EPSG:1024

**Return** a new Conversion.

**Parameters**

- **properties**: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
- **centerLat**: See Latitude of natural origin/Center Latitude. Usually 0
- **centerLong**: See Longitude of natural origin/Central Meridian. Usually 0
- **falseEasting**: See False Easting. Usually 0
- **falseNorthing**: See False Northing. Usually 0

`ConversionNNPtr createMollweide(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEast, const common::Length &falseNorthing)`

(1/2)

Instantiate a conversion based on the Mollweide projection method.

There is no equivalent in EPSG.

**Return** a new Conversion.

**Parameters**

- **properties**: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
- **centerLong**: See Longitude of natural origin/Central Meridian
- **falseEast**: See False Easting
- **falseNorthing**: See False Northing

`ConversionNNPtr createNewZealandMappingGrid(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Length &falseEast, const common::Length &falseNorthing)`

(2/2)

Instantiate a conversion based on the New Zealand Map Grid projection method.

This method is defined as EPSG:9811

**Return** a new Conversion.

**Parameters**

- **properties**: See `general_properties` of the conversion. If the name is not provided, it is automatically set.
- **centerLat**: See Latitude of natural origin/Center Latitude
- **centerLong**: See Longitude of natural origin/Central Meridian
- **falseEast**: See False Easting
- **falseNorthing**: See False Northing

`ConversionNNPtr createObliqueStereographic(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Scale &scale, const common::Length &falseEast, const common::Length &falseNorthing)`

(3/3)

Instantiate a conversion based on the Oblique Stereographic (Alternative) projection method.

This method is defined as EPSG:9809
Return a new Conversion.

Parameters

- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- centerLat: See Latitude of natural origin/Center Latitude
- centerLong: See Longitude of natural origin/Central Meridian
- scale: See Scale Factor
- falseEasting: See False Easting
- falseNorthing: See False Northing

ConversionNNPtr createOrthographic(const(util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Orthographic projection method.

This method is defined as EPSG:9840

Note At the time of writing, PROJ only implements the spherical formulation

Return a new Conversion.

Parameters

- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- centerLat: See Latitude of natural origin/Center Latitude
- centerLong: See Longitude of natural origin/Central Meridian
- falseEasting: See False Easting
- falseNorthing: See False Northing

ConversionNNPtr createAmericanPolyconic(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the American Polyconic projection method.

This method is defined as EPSG:9818

Return a new Conversion.

Parameters

- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- centerLat: See Latitude of natural origin/Center Latitude
- centerLong: See Longitude of natural origin/Central Meridian
- falseEasting: See False Easting
- falseNorthing: See False Northing

ConversionNNPtr createPolarStereographicVariantA(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Scale &scale, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Polar Stereographic (Variant A) projection method.

This method is defined as EPSG:9810
This is the variant of polar stereographic defined with a scale factor.

Return a new Conversion.

Parameters
- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- centerLat: See Latitude of natural origin/Center Latitude. Should be 90 deg ou -90 deg.
- centerLong: See Longitude of natural origin/Central Meridian
- scale: See Scale Factor
- falseEastIng: See False Easting
- falseNorthing: See False Northing

ConversionNNPtr createPolarStereographicVariantB(const util::PropertyMap &properties, const common::Angle &latitudeStandardParallel, const common::Angle &longitudeOfOrigin, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Polar Stereographic (Variant B) projection method.

This method is defined as EPSG:9829

This is the variant of polar stereographic defined with a latitude of standard parallel.

Return a new Conversion.

Parameters
- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- latitudeStandardParallel: See Latitude of standard parallel
- longitudeOfOrigin: See Longitude of origin
- falseEastIng: See False Easting
- falseNorthing: See False Northing

ConversionNNPtr createRobinson(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Robinson projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters
- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- centerLong: See Longitude of natural origin/Central Meridian
- falseEastIng: See False Easting
- falseNorthing: See False Northing

ConversionNNPtr createSinusoidal(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Sinusoidal projection method.

There is no equivalent in EPSG.

Return a new Conversion.
Parameters
• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEastings: See False Easting
• falseNorthings: See False Northing

ConversionNNPtr createStereographic(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Scale &scale, const common::Length &falseEastings, const common::Length &falseNorthings)

Instantiate a conversion based on the Stereographic projection method.

There is no equivalent in EPSG. This method implements the original “Oblique Stereographic” method described in “Snyder’s Map Projections - A Working manual”, which is different from the “Oblique Stereographic (alternative)” method implemented in createObliqueStereographic().

Return a new Conversion.

Parameters
• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEastings: See False Easting
• falseNorthings: See False Northing

ConversionNNPtr createVanDerGrinten(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEastings, const common::Length &falseNorthings)

Instantiate a conversion based on the Van der Grinten projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters
• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEastings: See False Easting
• falseNorthings: See False Northing

ConversionNNPtr createWagnerI(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEastings, const common::Length &falseNorthings)

Instantiate a conversion based on the Wagner I projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters
• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
Conversion NNPtr `createWagnerII` (const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Wagner II projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters
- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- centerLong: See Longitude of natural origin/Central Meridian
- falseEasting: See False Easting
- falseNorthing: See False Northing

Conversion NNPtr `createWagnerIII` (const util::PropertyMap &properties, const common::Angle &latitudeTrueScale, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Wagner III projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters
- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- latitudeTrueScale: Latitude of true scale.
- centerLong: See Longitude of natural origin/Central Meridian
- falseEasting: See False Easting
- falseNorthing: See False Northing

Conversion NNPtr `createWagnerIV` (const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Wagner IV projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters
- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- centerLong: See Longitude of natural origin/Central Meridian
- falseEasting: See False Easting
- falseNorthing: See False Northing

Conversion NNPtr `createWagnerV` (const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Wagner V projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters
• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEastings: See False Easting
• falseNortings: See False Northing

ConversionNNPtr createWagnerVI(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEastings, const common::Length &falseNortings)

Instantiate a conversion based on the Wagner VI projection method.

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEastings: See False Easting
• falseNortings: See False Northing

ConversionNNPtr createWagnerVII(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEastings, const common::Length &falseNortings)

Instantiate a conversion based on the Wagner VII projection method.

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEastings: See False Easting
• falseNortings: See False Northing

ConversionNNPtr createQuadrilateralizedSphericalCube(const util::PropertyMap &properties, const common::Angle &centerLat, const common::Angle &centerLong, const common::Length &falseEastings, const common::Length &falseNortings)

Instantiate a conversion based on the Quadrilateralized Spherical Cube projection method.

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLat: See Latitude of natural origin/Center Latitude
• centerLong: See Longitude of natural origin/Central Meridian
• falseEastings: See False Easting
• falseNortings: See False Northing
ConversionNNPtr createSphericalCrossTrackHeight(const util::PropertyMap &properties, const common::Angle &pegPointLat, const common::Angle &pegPointLong, const common::Angle &pegPointHeading, const common::Length &pegPointHeight)

Instantiate a conversion based on the Spherical Cross-Track Height projection method.

There is no equivalent in EPSG.

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• pegPointLat: Peg point latitude.
• pegPointLong: Peg point longitude.
• pegPointHeading: Peg point heading.
• pegPointHeight: Peg point height.

ConversionNNPtr createEqualEarth(const util::PropertyMap &properties, const common::Angle &centerLong, const common::Length &falseEasting, const common::Length &falseNorthing)

Instantiate a conversion based on the Equal Earth projection method.

This method is defined as EPSG:1078

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• centerLong: See Longitude of natural origin/Central Meridian
• falseEasting: See False Easting
• falseNorthing: See False Northing

ConversionNNPtr createChangeVerticalUnit(const util::PropertyMap &properties, const common::Scale &factor)

Instantiate a conversion based on the Change of Vertical Unit method.

This method is defined as EPSG:1069

Return a new Conversion.

Parameters

• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
• factor: Conversion factor

ConversionNNPtr createAxisOrderReversal (bool is3D)

Instantiate a conversion based on the Axis order reversal method.

This swaps the longitude, latitude axis.

This method is defined as EPSG:9843, or for 3D as EPSG:9844

Return a new Conversion.

Parameters

• is3D: Whether this should apply on 3D geographicCRS
ConversionNNPtr createGeographicGeocentric(const util::PropertyMap &properties)
Instantiates a conversion based on the Geographic/Geocentric method.

Return a new Conversion.

Parameters
• properties: See general_properties of the conversion. If the name is not provided, it is automatically set.

class CoordinateOperation : public osgeo::proj::common::ObjectUsage, public osgeo::proj::io::IPROJStringExportable
#include <coordinateoperation.hpp> Abstract class for a mathematical operation on coordinates.

A mathematical operation:
• on coordinates that transforms or converts them from one coordinate reference system to another coordinate reference system
• or that describes the change of coordinate values within one coordinate reference system due to the motion of the point between one coordinate epoch and another coordinate epoch.

Many but not all coordinate operations (from CRS A to CRS B) also uniquely define the inverse coordinate operation (from CRS B to CRS A). In some cases, the coordinate operation method algorithm for the inverse coordinate operation is the same as for the forward algorithm, but the signs of some coordinate operation parameter values have to be reversed. In other cases, different algorithms are required for the forward and inverse coordinate operations, but the same coordinate operation parameter values are used. If (some) entirely different parameter values are needed, a different coordinate operation shall be defined.

Remark Implements CoordinateOperation from ISO_19111_2019

Subclassed by osgeo::proj::operation::ConcatenatedOperation, osgeo::proj::operation::SingleOperation

Public Functions

const util::optional<std::string> &operationVersion() const
Return the version of the coordinate transformation (i.e. instantiation due to the stochastic nature of the parameters).
Mandatory when describing a coordinate transformation or point motion operation, and should not be supplied for a coordinate conversion.

Return version or empty.

const std::vector<metadata::PositionalAccuracyNNPtr> &coordinateOperationAccuracies() const
Return estimate(s) of the impact of this coordinate operation on point accuracy.
Gives position error estimates for target coordinates of this coordinate operation, assuming no errors in source coordinates.

Return estimate(s) or empty vector.

const crs::CRSPtr sourceCRS() const
Return the source CRS of this coordinate operation.
This should not be null, expect for of a derivingConversion of a DerivedCRS when the owning DerivedCRS has been destroyed.

Return source CRS, or null.
const crs::CRSPtr targetCRS() const
    Return the target CRS of this coordinate operation.

    This should not be null, except for of a derivingConversion of a DerivedCRS when the owning De-
    rivedCRS has been destroyed.
    
    Return target CRS, or null.

const crs::CRSPtr &interpolationCRS() const
    Return the interpolation CRS of this coordinate operation.
    
    Return interpolation CRS, or null.

const util::optional<common::DataEpoch> &sourceCoordinateEpoch() const
    Return the source epoch of coordinates.
    
    Return source epoch of coordinates, or empty.

const util::optional<common::DataEpoch> &targetCoordinateEpoch() const
    Return the target epoch of coordinates.
    
    Return target epoch of coordinates, or empty.

virtual CoordinateOperationNNPtr inverse() const = 0
    Return the inverse of the coordinate operation.

Exceptions
    • util::UnsupportedOperationException:

virtual std::set<GridDescription> gridsNeeded(const io::DatabaseContextPtr &databaseContext) const = 0
    Return grids needed by an operation.

bool isPROJInstantiable(const io::DatabaseContextPtr &databaseContext) const
    Return whether a coordinate operation can be instantiated as a PROJ pipeline, checking in particular
    that referenced grids are available.

bool hasBallparkTransformation() const
    Return whether a coordinate operation has a “ballpark” transformation, that is a very approximate
    one, due to lack of more accurate transformations.

    Typically a null geographic offset between two horizontal datum, or a null vertical offset (or limited
    to unit changes) between two vertical datum. Errors of several tens to one hundred meters might be
    expected, compared to more accurate transformations.

    CoordinateOperationNNPtr normalizeForVisualization() const
    Return a variation of the current coordinate operation whose axis order is the one expected for visual-
    ization purposes.

Public Static Attributes

const std::string OPERATION_VERSION_KEY
    Key to set the operation version of a operation::CoordinateOperation.

    The value is to be provided as a string.

class CoordinateOperationContext
    #include <coordinateoperation.hpp> Context in which a coordinate operation is to be used.
Remark  Implements  [CoordinateOperationFactory](https://sis.apache.org/apidocs/org/apache/sis/referencing/operation/CoordinateOperationContext.html) from Apache SIS

**Public Types**

```java
enum SourceTargetCRSExtentUse
Specify how source and target CRS extent should be used to restrict candidate operations (only taken into account if no explicit area of interest is specified.  
Values:

NONE
  Ignore CRS extent

BOTH
  Test coordinate operation extent against both CRS extent.

INTERSECTION
  Test coordinate operation extent against the intersection of both CRS extent.

SMALLEST
  Test coordinate operation against the smallest of both CRS extent.
```

```java
enum SpatialCriterion
Spatial criterion to restrict candidate operations.  
Values:

STRICT_CONTAINMENT
  The area of validity of transforms should strictly contain the area of interest.

PARTIAL_INTERSECTION
  The area of validity of transforms should at least intersect the area of interest.
```

```java
enum GridAvailabilityUse
Describe how grid availability is used.  
Values:

USE_FOR_SORTING
  Grid availability is only used for sorting results. Operations where some grids are missing will be sorted last.

DISCARD_OPERATION_IF_MISSING_GRID
  Completely discard an operation if a required grid is missing.

IGNORE_GRID_AVAILABILITY
  Ignore grid availability at all. Results will be presented as if all grids were available.
```

```java
enum IntermediateCRSUse
Describe if and how intermediate CRS should be used  
Values:

ALWAYS
  Always search for intermediate CRS.

IF_NO_DIRECT_TRANSFORMATION
  Only attempt looking for intermediate CRS if there is no direct transformation available.

NEVER
```
**Public Functions**

```cpp
const io::AuthorityFactoryPtr &getAuthorityFactory() const
    Return the authority factory, or null.

const metadata::ExtentPtr &getAreaOfInterest() const
    Return the desired area of interest, or null.

void setAreaOfInterest(const metadata::ExtentPtr &extent)
    Set the desired area of interest, or null.

double getDesiredAccuracy() const
    Return the desired accuracy (in metre), or 0.

void setDesiredAccuracy(double accuracy)
    Set the desired accuracy (in metre), or 0.

void setSourceAndTargetCRSExtentUse(SourceTargetCRSExtentUse use)
    Set how source and target CRS extent should be used when considering if a transformation can be
    used (only takes effect if no area of interest is explicitly defined).
    The default is CoordinateOperationContext::SourceTargetCRSExtentUse::SMALLEST.

CoordinateOperationContext::SourceTargetCRSExtentUse getSourceAndTargetCRSExtentUse() const
    Return how source and target CRS extent should be used when considering if a transformation can be
    used (only takes effect if no area of interest is explicitly defined).
    The default is CoordinateOperationContext::SourceTargetCRSExtentUse::SMALLEST.

void setSpatialCriterion(SpatialCriterion criterion)
    Set the spatial criterion to use when comparing the area of validity of coordinate operations with the
    area of interest / area of validity of source and target CRS.
    The default is STRICT_CONTAINMENT.

CoordinateOperationContext::SpatialCriterion getSpatialCriterion() const
    Return the spatial criterion to use when comparing the area of validity of coordinate operations with
    the area of interest / area of validity of source and target CRS.
    The default is STRICT_CONTAINMENT.

void setUsePROJAlternativeGridNames(bool usePROJNames)
    Set whether PROJ alternative grid names should be substituted to the official authority names.
    This only has effect is an authority factory with a non-null database context has been attached to this
    context.
    If set to false, it is still possible to obtain later the substitution by using
    io::PROJStringFormatter::create() with a non-null database context.
    The default is true.

bool getUsePROJAlternativeGridNames() const
    Return whether PROJ alternative grid names should be substituted to the official authority names.
    The default is true.

void setDiscardSuperseded(bool discard)
    Set whether transformations that are superseded (but not deprecated) should be discarded.
    The default is true.
```
bool getDiscardSuperseded() const
   Return whether transformations that are superseded (but not deprecated) should be discarded.
   The default is true.

void setGridAvailabilityUse(GridAvailabilityUse use)
   Set how grid availability is used.
   The default is USE_FOR_SORTING.

CoordinateOperationContext::GridAvailabilityUse getGridAvailabilityUse() const
   Return how grid availability is used.
   The default is USE_FOR_SORTING.

void setAllowUseIntermediateCRS(IntermediateCRSUse use)
   Set whether an intermediate pivot CRS can be used for researching coordinate operations between a
   source and target CRS.

Concretely if in the database there is an operation from A to C (or C to A), and another one
from C to B (or B to C), but no direct operation between A and B, setting this parameter to AL-
WAYS/IF_NO_DIRECT_TRANSFORMATION, allow chaining both operations.

The current implementation is limited to researching one intermediate step.

By default, with the IF_NO_DIRECT_TRANSFORMATION strategy, all potential C candidates will
be used if there is no direct transformation.

CoordinateOperationContext::IntermediateCRSUse getAllowUseIntermediateCRS() const
   Return whether an intermediate pivot CRS can be used for researching coordinate operations between
   a source and target CRS.

Concretely if in the database there is an operation from A to C (or C to A), and another one
from C to B (or B to C), but no direct operation between A and B, setting this parameter to AL-
WAYS/IF_NO_DIRECT_TRANSFORMATION, allow chaining both operations.

The default is IF_NO_DIRECT_TRANSFORMATION.

void setIntermediateCRS(const std::vector<std::pair<std::string, std::string>> &intermedi-
ateCRSAuthCodes)
   Restrict the potential pivot CRSs that can be used when trying to build a coordinate operation between
two CRS that have no direct operation.

Parameters
   • intermediateCRSAuthCodes: a vector of (auth_name, code) that can be used as potential pivot RS

const std::vector<std::pair<std::string, std::string>> &getIntermediateCRS() const
   Return the potential pivot CRSs that can be used when trying to build a coordinate operation between
two CRS that have no direct operation.
Public Static Functions

CoordinateOperationContextNNPtr create(const io::AuthorityFactoryPtr &authorityFactory, const metadata::ExtentPtr &extent, double accuracy)

Creates a context for a coordinate operation.

If a non null authorityFactory is provided, the resulting context should not be used simultaneously by more than one thread.

If authorityFactory->getAuthority() is the empty string, then coordinate operations from any authority will be searched, with the restrictions set in the authority_to_authority_preference database table. If authorityFactory->getAuthority() is set to “any”, then coordinate operations from any authority will be searched If authorityFactory->getAuthority() is a non-empty string different of “any”, then coordinate operations will be searched only in that authority namespace.

Return a new context.

Parameters
- authorityFactory: Authority factory, or null if no database lookup is allowed. Use io::authorityFactory::create(context, std::string()) to allow all authorities to be used.
- extent: Area of interest, or null if none is known.
- accuracy: Maximum allowed accuracy in metre, as specified in or 0 to get best accuracy.

class CoordinateOperationFactory

#include <coordinateoperation.hpp> Creates coordinate operations. This factory is capable to find coordinate transformations or conversions between two coordinate reference systems.

Remark Implements (partially) CoordinateOperationFactory from GeoAPI

Public Functions

CoordinateOperationPtr createOperation(const crs::CRSNNPtr &sourceCRS, const crs::CRSNNPtr &targetCRS) const

Find a CoordinateOperation from sourceCRS to targetCRS. This is a helper of createOperations(), using a coordinate operation context with no authority factory (so no catalog searching is done), no desired accuracy and no area of interest. This returns the first operation of the result set of createOperations(), or null if none found.

Return a CoordinateOperation or nullptr.

Parameters
- sourceCRS: source CRS.
- targetCRS: source CRS.

std::vector<CoordinateOperationNNPtr> createOperations(const crs::CRSNNPtr &sourceCRS, const crs::CRSNNPtr &targetCRS, const CoordinateOperationContextNNPtr &context) const

Find a list of CoordinateOperation from sourceCRS to targetCRS.

The operations are sorted with the most relevant ones first: by descending area (intersection of the transformation area with the area of interest, or intersection of the transformation with the area of use of the CRS), and by increasing accuracy. Operations with unknown accuracy are sorted last, whatever their area.

Return a list
Parameters

• sourceCRS: source CRS.
• targetCRS: source CRS.
• context: Search context.

Public Static Functions

CoordinateOperationFactoryNNPtr create()
Instantiates a CoordinateOperationFactory.

class GeneralOperationParameter : public osgeo::proj::common::IdentifiedObject
#include <coordinateoperation.hpp> Abstract class modelling a parameter value (OperationParameter) or group of parameters.

Remark Implements GeneralOperationParameter from ISO_19111_2019

Subclassed by osgeo::proj::operation::OperationParameter

class GeneralParameterValue : public osgeo::proj::util::BaseObject, public osgeo::proj::io::IWKTExportable, public osgeo::proj::util::IComparable
#include <coordinateoperation.hpp> Abstract class modelling a parameter value (OperationParameterValue) or group of parameter values.

Remark Implements GeneralParameterValue from ISO_19111_2019

Subclassed by osgeo::proj::operation::OperationParameterValue

struct GridDescription
#include <coordinateoperation.hpp> Grid description.

Public Members

std::string shortName
Grid short filename

std::string fullName
Grid full path name (if found)

std::string packageName
Package name (or empty)

std::string url
Grid URL (if packageName is empty), or package URL (or empty)

bool directDownload
Whether url can be fetched directly.

bool openLicense
Whether the grid is released with an open license.

bool available
Whether GRID is available.

class InvalidOperation : public osgeo::proj::util::Exception
#include <coordinateoperation.hpp> Exception that can be thrown when an invalid operation is attempted to be constructed.
class OperationMethod : public osgeo::proj::common::IdentifiedObject
#include <coordinateoperation.hpp> The method (algorithm or procedure) used to perform the coordinate operation.

For a projection method, this contains the name of the projection method and the name of the projection parameters.

Remark Implements OperationMethod from ISO_19111_2019

Public Functions

const util::optional<std::string> &formula ()
Return the formula(s) or procedure used by this coordinate operation method.

This may be a reference to a publication (in which case use formulaCitation()).

Note that the operation method may not be analytic, in which case this attribute references or contains
the procedure, not an analytic formula.

Return the formula, or empty.

const util::optional<metadata::Citation> &formulaCitation ()
Return a reference to a publication giving the formula(s) or procedure used by the coordinate operation method.

Return the formula citation, or empty.

const std::vector<GeneralOperationParameterNNPtr> &parameters ()
Return the parameters of this operation method.

Return the parameters.

int getEPSGCode ()
Return the EPSG code, either directly, or through the name.

Return code, or 0 if not found

Public Static Functions

OperationMethodNNPtr create (const util::PropertyMap &properties, const std::vector<GeneralOperationParameterNNPtr> &parameters)
Instantiate a operation method from a vector of GeneralOperationParameter.

Return a new OperationMethod.

Parameters

• properties: See general_properties. At minimum the name should be defined.

• parameters: Vector of GeneralOperationParameterNNPtr.

OperationMethodNNPtr create (const util::PropertyMap &properties, const std::vector<OperationParameterNNPtr> &parameters)
Instantiate a operation method from a vector of OperationParameter.

Return a new OperationMethod.

Parameters

• properties: See general_properties. At minimum the name should be defined.

• parameters: Vector of OperationParameterNNPtr.
The definition of a parameter used by a coordinate operation method.

Most parameter values are numeric, but other types of parameter values are possible.

Remark Implements OperationParameter from ISO_19111_2019

Public Functions

int getEPSGCode ()
Return the EPSG code, either directly, or through the name.
Return code, or 0 if not found

Public Static Functions

OperationParameterNNPtr create (const util::PropertyMap &properties)
Instantiate a OperationParameter.
Return a new OperationParameter.
Parameters
• properties: See general_properties. At minimum the name should be defined.

const char *getNameForEPSGCode (int epsg_code)
Return the name of a parameter designed by its EPSG code.
Return name, or nullptr if not found

class OperationParameterValue : public osgeo::proj::operation::GeneralParameterValue
#include <coordinateoperation.hpp> A parameter value, ordered sequence of values, or reference to a file of parameter values.
This combines a OperationParameter with the corresponding ParameterValue.

Remark Implements OperationParameterValue from ISO_19111_2019

Public Functions

const OperationParameterNNPtr &parameter ()
Return the parameter (definition)
Return the parameter (definition).

const ParameterValueNNPtr &parameterValue ()
Return the parameter value.
Return the parameter value.
Public Static Functions

(OperationParameterValueNNPtr create(const OperationParameterNNPtr &parameterIn,
const ParameterValueNNPtr &valueIn)

Instantiate a OperationParameterValue.

Return a new OperationParameterValue.

Parameters

• parameterIn: Parameter (definition).
• valueIn: Parameter value.

class ParameterValue : public osgeo::proj::util::BaseObject, public osgeo::proj::io::IWKTExportable, public osgeo::proj::util::IComparable

#include <coordinateoperation.hpp>

The value of the coordinate operation parameter.

Most parameter values are numeric, but other types of parameter values are possible.

Remark Implements ParameterValue from ISO_19111_2019

Public Types

enum Type

Type of the value.

Values:

MEASURE

Measure (i.e. value with a unit)

STRING

String

INTEGER

Integer

BOOLEAN

Boolean

FILENAME

Filename

Public Functions

const ParameterValue::Type &type ()

Returns the type of a parameter value.

Return the type.

const common::Measure &value ()

Returns the value as a Measure (assumes type() == Type::MEASURE)

Return the value as a Measure.

const std::string &stringValue ()

Returns the value as a string (assumes type() == Type::STRING)

Return the value as a string.

const std::string &valueFile ()

Returns the value as a filename (assumes type() == Type::FILENAME)
Return the value as a filename.

```cpp
int integerValue() {
  // Returns the value as an integer (assumes type() == Type::INTEGER)
  return the value as an integer.
}
```

bool booleanValue() {
  // Returns the value as a boolean (assumes type() == Type::BOOLEAN)
  return the value as a boolean.
}

Public Static Functions

### ParameterValueNNPtr create(const common::Measure &measureIn)
Instantiates a ParameterValue from a Measure (i.e. a value associated with a unit).

```cpp
ParameterValueNNPtr create(const char *stringValueIn)
/* Instantiate a ParameterValue from a string value. */
```

```cpp
ParameterValueNNPtr create(const std::string &stringValueIn)
/* Instantiate a ParameterValue from a string value. */
```

```cpp
ParameterValueNNPtr create(int integerValueIn)
/* Instantiate a ParameterValue from an integer value. */
```

```cpp
ParameterValueNNPtr create(bool booleanValueIn)
/* Instantiate a ParameterValue from a boolean value. */
```

```cpp
ParameterValueNNPtr createFilename(const std::string &stringValueIn)
/* Instantiate a ParameterValue from a filename. */
```

### class PointMotionOperation: public osgeo::proj::operation::SingleOperation
A mathematical operation that describes the change of coordinate values within one coordinate reference system due to the motion of the point between one coordinate epoch and another coordinate epoch.

The motion is due to tectonic plate movement or deformation.

**Remark** Implements PointMotionOperation from ISO_19111_2019

### class SingleOperation: public virtual osgeo::proj::operation::CoordinateOperation
A single (not concatenated) coordinate operation (CoordinateOperation)

**Remark** Implements SingleOperation from ISO_19111_2019
Subclassed by `osgeo::proj::operation::Conversion`, `osgeo::proj::operation::PointMotionOperation`, `osgeo::proj::operation::Transformation`

**Public Functions**

```cpp
const std::vector<GeneralParameterValueNNPtr> &parameterValues() const
    Return the parameter values.

const OperationMethodNNPtr &method() const
    Return the operation method associated to the operation.

const ParameterValuePtr &parameterValue(const std::string &paramName, int epsg_code = 0) const
    Return the parameter value corresponding to a parameter name or EPSG code.
    Parameters
    • paramName: the parameter name (or empty, in which case epsg_code should be non zero)
    • epsg_code: the parameter EPSG code (possibly zero)

const ParameterValuePtr &parameterValue(int epsg_code) const
    Return the parameter value corresponding to a EPSG code.
    Parameters
    • epsg_code: the parameter EPSG code

const common::Measure &parameterValueMeasure(const std::string &paramName, int epsg_code = 0) const
    Return the parameter value, as a measure, corresponding to a parameter name or EPSG code.
    Parameters
    • paramName: the parameter name (or empty, in which case epsg_code should be non zero)
    • epsg_code: the parameter EPSG code (possibly zero)

const common::Measure &parameterValueMeasure(int epsg_code) const
    Return the parameter value, as a measure, corresponding to a EPSG code.
    Parameters
    • epsg_code: the parameter EPSG code

std::set<GridDescription> gridsNeeded(const io::DatabaseContextPtr &databaseContext) const
    Return grids needed by an operation.

std::list<std::string> validateParameters() const
    Validate the parameters used by a coordinate operation.
    Return whether the method is known or not, or a list of missing or extra parameters for the operations recognized by this implementation.
**Public Static Functions**

```
SingleOperationNNPtr createPROJBased(const util::PropertyMap &properties, const std::string &PROJString,
const crs::CRSPtr &sourceCRS, const crs::CRSPtr &targetCRS,
std::vector<metadata::PositionalAccuracyNNPtr> &accuracies = std::vector<metadata::PositionalAccuracyNNPtr>())
```

Instantiate a PROJ-based single operation.

**Note** The operation might internally be a pipeline chaining several operations. The use of the Single-Operation modeling here is mostly to be able to get the PROJ string as a parameter.

**Return** the new instance

**Parameters**

- `properties`: Properties
- `PROJString`: the PROJ string.
- `sourceCRS`: source CRS (might be null).
- `targetCRS`: target CRS (might be null).
- `accuracies`: Vector of positional accuracy (might be empty).

**class Transformation : public** osgeo::proj::operation::SingleOperation

A mathematical operation on coordinates in which parameters are empirically derived from data containing the coordinates of a series of points in both coordinate reference systems.

This computational process is usually “over-determined”, allowing derivation of error (or accuracy) estimates for the coordinate transformation. Also, the stochastic nature of the parameters may result in multiple (different) versions of the same coordinate transformations between the same source and target CRSs. Any single coordinate operation in which the input and output coordinates are referenced to different datums (reference frames) will be a coordinate transformation.

**Remark** Implements Transformation from ISO_19111_2019

**Public Functions**

```
const crs::CRSNPtr &sourceCRS()
```

Return the source `crs::CRS` of the transformation.

**Return** the source CRS.

```
const crs::CRSNPtr &targetCRS()
```

Return the target `crs::CRS` of the transformation.

**Return** the target CRS.

```
CoordinateOperationNNPtr inverse() const
```

Return the inverse of the coordinate operation.

**Exceptions**

- `util::UnsupportedOperationException`

```
TransformationNNPtr substitutePROJAlternativeGridNames (io::DatabaseContextNNPtr databaseContext)
```

Return an equivalent transformation to the current one, but using PROJ alternative grid names.
Public Static Functions

TransformationNNPtr create(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, const crs::CRSPtr &interpolationCRSIn, const OperationMethodNNPtr &methodIn, const std::vector<GeneralParameterValueNNPtr> &values, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation from a vector of GeneralParameterValue.

Return new Transformation.

Parameters

- properties: See general_properties. At minimum the name should be defined.
- sourceCRSIn: Source CRS.
- targetCRSIn: Target CRS.
- interpolationCRSIn: Interpolation CRS (might be null)
- methodIn: Operation method.
- values: Vector of GeneralOperationParameterNNPtr.
- accuracies: Vector of positional accuracy (might be empty).

Exceptions

- InvalidOperation:

TransformationNNPtr create(const util::PropertyMap &propertiesTransformation, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, const crs::CRSPtr &interpolationCRSIn, const util::PropertyMap &propertiesOperationMethod, const std::vector<OperationParameterNNPtr> &parameters, const std::vectorParameterValueNNPtr &values, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation ands its OperationMethod.

Return new Transformation.

Parameters

- propertiesTransformation: The general_properties of the Transformation. At minimum the name should be defined.
- sourceCRSIn: Source CRS.
- targetCRSIn: Target CRS.
- interpolationCRSIn: Interpolation CRS (might be null)
- propertiesOperationMethod: The general_properties of the OperationMethod. At minimum the name should be defined.
- parameters: Vector of parameters of the operation method.
- values: Vector of ParameterValueNNPtr. Constraint: values.size() == parameters.size()
- accuracies: Vector of positional accuracy (might be empty).

Exceptions

- InvalidOperation:

TransformationNNPtr createGeocentricTranslations(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, double translationXMetre, double translationYMetre, double translationZMetre, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation with Geocentric Translations method.
Return new Transformation.

Parameters
- properties: See general_properties of the Transformation. At minimum the name should be defined.
- sourceCRSIn: Source CRS.
- targetCRSIn: Target CRS.
- translationXMetre: Value of the Translation_X parameter (in metre).
- translationYMetre: Value of the Translation_Y parameter (in metre).
- translationZMetre: Value of the Translation_Z parameter (in metre).
- accuracies: Vector of positional accuracy (might be empty).

TransformationNNPtr createPositionVector(const util::PropertyMap &properties,
const crs::CRSNNPtr &sourceCRSIn,
const crs::CRSNNPtr &targetCRSIn,
double translationXMetre, double translationYMetre, double translationZMetre,
double rotationXArcSecond, double rotationYArcSecond, double rotationZArcSecond,
double scaleDifferencePPM, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation with Position vector transformation method.

This is similar to createCoordinateFrameRotation(), except that the sign of the rotation terms is inverted.

Return new Transformation.

Parameters
- properties: See general_properties of the Transformation. At minimum the name should be defined.
- sourceCRSIn: Source CRS.
- targetCRSIn: Target CRS.
- translationXMetre: Value of the Translation_X parameter (in metre).
- translationYMetre: Value of the Translation_Y parameter (in metre).
- translationZMetre: Value of the Translation_Z parameter (in metre).
- scaleDifferencePPM: Value of the Scale_Difference parameter (in parts-per-million).
- accuracies: Vector of positional accuracy (might be empty).

TransformationNNPtr createCoordinateFrameRotation(const util::PropertyMap &properties,
const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn,
double translationXMetre, double translationYMetre, double translationZMetre,
double rotationXArcSecond, double rotationYArcSecond, double rotationZArcSecond,
double scaleDifferencePPM, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation with Coordinate Frame Rotation method.
This is similar to `createPositionVector()`, except that the sign of the rotation terms is inverted.

**Return** new `Transformation`.

**Parameters**

- **properties**: See `general_properties` of the `Transformation`. At minimum the name should be defined.
- **sourceCRSIn**: Source CRS.
- **targetCRSIn**: Target CRS.
- **translationXMetre**: Value of the Translation_X parameter (in metre).
- **translationYMetre**: Value of the Translation_Y parameter (in metre).
- **translationZMetre**: Value of the Translation_Z parameter (in metre).
- **rotationXArcSecond**: Value of the Rotation_X parameter (in arc-second).
- **rotationYArcSecond**: Value of the Rotation_Y parameter (in arc-second).
- **rotationZArcSecond**: Value of the Rotation_Z parameter (in arc-second).
- **scaleDifferencePPM**: Value of the Scale_Difference parameter (in parts-per-million).
- **accuracies**: Vector of positional accuracy (might be empty).

```cpp
TransformationNNPtr createTimeDependentPositionVector(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, double translationXMetre, double translationYMetre, double translationZMetre, double rotationXArcSecond, double rotationYArcSecond, double rotationZArcSecond, double scaleDifferencePPM, double rateTranslationX, double rateTranslationY, double rateTranslationZ, double rateRotationX, double rateRotationY, double rateRotationZ, double rateScaleDifference, double referenceEpochYear, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)
```

Instantiate a transformation with Time Dependent position vector transformation method.

This is similar to `createTimeDependentCoordinateFrameRotation()`, except that the sign of the rotation terms is inverted.

This method is defined as EPSG:1053

**Return** new `Transformation`.

**Parameters**

- **properties**: See `general_properties` of the `Transformation`. At minimum the name should be defined.
- **sourceCRSIn**: Source CRS.
- **targetCRSIn**: Target CRS.
- **translationXMetre**: Value of the Translation_X parameter (in metre).
• translationYMetre: Value of the Translation_Y parameter (in metre).
• translationZMetre: Value of the Translation_Z parameter (in metre).
• rotationXArcSecond: Value of the Rotation_X parameter (in arc-second).
• rotationYArcSecond: Value of the Rotation_Y parameter (in arc-second).
• rotationZArcSecond: Value of the Rotation_Z parameter (in arc-second).
• scaleDifferencePPM: Value of the Scale_Difference parameter (in parts-per-million).
• rateTranslationX: Value of the rate of change of X-axis translation (in metre/year)
• rateTranslationY: Value of the rate of change of Y-axis translation (in metre/year)
• rateTranslationZ: Value of the rate of change of Z-axis translation (in metre/year)
• rateRotationX: Value of the rate of change of X-axis rotation (in arc-second/year)
• rateRotationY: Value of the rate of change of Y-axis rotation (in arc-second/year)
• rateRotationZ: Value of the rate of change of Z-axis rotation (in arc-second/year)
• rateScaleDifference: Value of the rate of change of scale difference (in PPM/year)
• referenceEpochYear: Parameter reference epoch (in decimal year)
• accuracies: Vector of positional accuracy (might be empty).
TransformationNNPtr createTimeDependentCoordinateFrameRotation(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, double translationXMetre, double translationYMetre, double translationZMetre, double rotationXArcSecond, double rotationYArcSecond, double rotationZArcSecond, double scaleDifferencePPM, double rateTranslationX, double rateTranslationY, double rateTranslationZ, double rateRotationX, double rateRotationY, double rateRotationZ, double rateScaleDifference, double referenceEpochYear, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation with Time Dependent Position coordinate frame rotation transformation method.

This is similar to createTimeDependentPositionVector(), except that the sign of the rotation terms is inverted.
This method is defined as **EPSG:1056**

**Return** `new Transformation.`

**Parameters**

- **properties**: See `general_properties` of the `Transformation`. At minimum the name should be defined.
- **sourceCRSIn**: Source CRS.
- **targetCRSIn**: Target CRS.
- **translationXMetre**: Value of the Translation_X parameter (in metre).
- **translationYMetre**: Value of the Translation_Y parameter (in metre).
- **translationZMetre**: Value of the Translation_Z parameter (in metre).
- **rotationXArcSecond**: Value of the Rotation_X parameter (in arc-second).
- **rotationYArcSecond**: Value of the Rotation_Y parameter (in arc-second).
- **rotationZArcSecond**: Value of the Rotation_Z parameter (in arc-second).
- **scaleDifferencePPM**: Value of the Scale_Difference parameter (in parts-per-million).
- **rateTranslationX**: Value of the rate of change of X-axis translation (in metre/year)
- **rateTranslationY**: Value of the rate of change of Y-axis translation (in metre/year)
- **rateTranslationZ**: Value of the rate of change of Z-axis translation (in metre/year)
- **rateRotationX**: Value of the rate of change of X-axis rotation (in arc-second/year)
- **rateRotationY**: Value of the rate of change of Y-axis rotation (in arc-second/year)
- **rateRotationZ**: Value of the rate of change of Z-axis rotation (in arc-second/year)
- **rateScaleDifference**: Value of the rate of change of scale difference (in PPM/year)
- **referenceEpochYear**: Parameter reference epoch (in decimal year)
- **accuracies**: Vector of positional accuracy (might be empty).

**Exceptions**

- `InvalidOperation`

TransformationNNPtr `createTOWGS84` (const crs::CRSNNPtr &sourceCRSIn, const std::vector<double> &TOWGS84Parameters)

Instantiate a transformation from TOWGS84 parameters.

This is a helper of `createPositionVector()` with the source CRS being the GeographicCRS of sourceCRSIn, and the target CRS being EPSG:4326

**Return** `new Transformation.`

**Parameters**

- **sourceCRSIn**: Source CRS.
- **TOWGS84Parameters**: The vector of 3 double values (Translation_X,_Y,_Z) or 7 double values (Translation_X,_Y,_Z, Rotation_X,_Y,_Z, Scale_Difference) passed to `createPositionVector()`

**Exceptions**

- `InvalidOperation`

TransformationNNPtr `createNTv2` (const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, const std::string &filename, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation with NTv2 method.

**Return** `new Transformation`.

**Parameters**

- **properties**: See `general_properties` of the `Transformation`. At minimum the name should be defined.
- **sourceCRSIn**: Source CRS.
- **targetCRSIn**: Target CRS.
- **filename**: NTv2 filename.
TransformationNNPtr createMolodensky(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, double translationXMetre, double translationYMetre, double translationZMetre, double semiMajorAxisDifferenceMetre, double flattingDifference, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation with Molodensky method.

This method is defined as EPSG:9604

See createAbridgedMolodensky() for a related method.

Return new Transformation.

Parameters

- properties: See general_properties of the Transformation. At minimum the name should be defined.
- sourceCRSIn: Source CRS.
- targetCRSIn: Target CRS.
- translationXMetre: Value of the Translation_X parameter (in metre).
- translationYMetre: Value of the Translation_Y parameter (in metre).
- translationZMetre: Value of the Translation_Z parameter (in metre).
- semiMajorAxisDifferenceMetre: The difference between the semi-major axis values of the ellipsoids used in the target and source CRS (in metre).
- flattingDifference: The difference between the flattening values of the ellipsoids used in the target and source CRS.
- accuracies: Vector of positional accuracy (might be empty).

Exceptions

- InvalidOperation:

TransformationNNPtr createAbridgedMolodensky(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, double translationXMetre, double translationYMetre, double translationZMetre, double semiMajorAxisDifferenceMetre, double flattingDifference, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation with Abridged Molodensky method.

This method is defined as EPSG:9605

See createdMolodensky() for a related method.

Return new Transformation.

Parameters

- properties: See general_properties of the Transformation. At minimum the name should be defined.
- sourceCRSIn: Source CRS.
- targetCRSIn: Target CRS.
- translationXMetre: Value of the Translation_X parameter (in metre).
- translationYMetre: Value of the Translation_Y parameter (in metre).
- translationZMetre: Value of the Translation_Z parameter (in metre).
- semiMajorAxisDifferenceMetre: The difference between the semi-major axis values of the ellipsoids used in the target and source CRS (in metre).
- **flatteningDifference**: The difference between the flattening values of the ellipsoids used in the target and source CRS.
- **accuracies**: Vector of positional accuracy (might be empty).

**Exceptions**
- **InvalidOperation**:

```cpp
class TransformationNNPtr createGravityRelatedHeightToGeographic3D(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, const crs::CRSPtr &interpolationCRSIn, const std::string &filename, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)
```

Instantiate a transformation from GravityRelatedHeight to Geographic3D.

**Return** new `Transformation`.

**Parameters**
- **properties**: See `general_properties` of the `Transformation`. At minimum the name should be defined.
- **sourceCRSIn**: Source CRS.
- **targetCRSIn**: Target CRS.
- **interpolationCRSIn**: Interpolation CRS. (might be null)
- **filename**: GRID filename.
- **accuracies**: Vector of positional accuracy (might be empty).

```cpp
class TransformationNNPtr createVERTCON(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, const std::string &filename, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)
```

Instantiate a transformation with method VERTCON.

**Return** new `Transformation`.

**Parameters**
- **properties**: See `general_properties` of the `Transformation`. At minimum the name should be defined.
- **sourceCRSIn**: Source CRS.
- **targetCRSIn**: Target CRS.
- **filename**: GRID filename.
- **accuracies**: Vector of positional accuracy (might be empty).

```cpp
class TransformationNNPtr createLongitudeRotation(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, const common::Angle &offset)
```

Instantiate a transformation with method Longitude rotation.
This method is defined as **EPSG:9601**

- **Return** new `Transformation`.

  **Parameters**
  - `properties`: See `general_properties` of the `Transformation`. At minimum the name should be defined.
  - `sourceCRSIn`: Source CRS.
  - `targetCRSIn`: Target CRS.
  - `offset`: Longitude offset to add.

```cpp
TransformationNNPtr createGeographic2DOffsets(const util::PropertyMap &properties, const crs::CRSSPtr &sourceCRSIn, const crs::CRSSPtr &targetCRSIn, const common::Angle &offsetLat, const common::Angle &offsetLon, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)
```

Instantiate a transformation with method Geographic 2D offsets.

This method is defined as **EPSG:9619**

- **Return** new `Transformation`.

  **Parameters**
  - `properties`: See `general_properties` of the `Transformation`. At minimum the name should be defined.
  - `sourceCRSIn`: Source CRS.
  - `targetCRSIn`: Target CRS.
  - `offsetLat`: Latitude offset to add.
  - `offsetLon`: Longitude offset to add.
  - `accuracies`: Vector of positional accuracy (might be empty).

```cpp
TransformationNNPtr createGeographic3DOffsets(const util::PropertyMap &properties, const crs::CRSSPtr &sourceCRSIn, const crs::CRSSPtr &targetCRSIn, const common::Angle &offsetLat, const common::Angle &offsetLon, const common::Length &offsetHeight, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)
```

Instantiate a transformation with method Geographic 3D offsets.

This method is defined as **EPSG:9660**

- **Return** new `Transformation`.

  **Parameters**
  - `properties`: See `general_properties` of the `Transformation`. At minimum the name should be defined.
  - `sourceCRSIn`: Source CRS.
  - `targetCRSIn`: Target CRS.
  - `offsetLat`: Latitude offset to add.
  - `offsetLon`: Longitude offset to add.
  - `offsetHeight`: Height offset to add.
  - `accuracies`: Vector of positional accuracy (might be empty).
TransformationNNPtr createGeographic2DWithHeightOffsets(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, const common::Angle &offsetLat, const common::Angle &offsetLon, const common::Length &offsetHeight, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation with method Geographic 2D with height offsets. This method is defined as EPSG:9618
• Return new Transformation.

Parameters
– properties: See general_properties of the Transformation. At minimum the name should be defined.
– sourceCRSIn: Source CRS.
– targetCRSIn: Target CRS.
– offsetLat: Latitude offset to add.
– offsetLon: Longitude offset to add.
– offsetHeight: Geoid undulation to add.
– accuracies: Vector of positional accuracy (might be empty).

TransformationNNPtr createVerticalOffset(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, const common::Length &offsetHeight, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation with method Vertical Offset. This method is defined as EPSG:9616
• Return new Transformation.

Parameters
– properties: See general_properties of the Transformation. At minimum the name should be defined.
– sourceCRSIn: Source CRS.
– targetCRSIn: Target CRS.
– offsetHeight: Geoid undulation to add.
– accuracies: Vector of positional accuracy (might be empty).

TransformationNNPtr createChangeVerticalUnit(const util::PropertyMap &properties, const crs::CRSNNPtr &sourceCRSIn, const crs::CRSNNPtr &targetCRSIn, const common::Scale &factor, const std::vector<metadata::PositionalAccuracyNNPtr> &accuracies)

Instantiate a transformation based on the Change of Vertical Unit method. This method is defined as EPSG:1069
Return a new Transformation.

Parameters
- properties: See general_properties of the conversion. If the name is not provided, it is automatically set.
- sourceCRSIn: Source CRS.
- targetCRSIn: Target CRS.
- factor: Conversion factor
- accuracies: Vector of positional accuracy (might be empty).

10.5.3.9 io namespace

namespace io
I/O classes.

osgeo.proj.io namespace.

Typedefs

using DatabaseContextPtr = std::shared_ptr<DatabaseContext>
    Shared pointer of DatabaseContext.

using DatabaseContextNNPtr = util::nn<DatabaseContextPtr>
    Non-null shared pointer of DatabaseContext.

using WKTNodePtr = std::unique_ptr<WKTNode>
    Unique pointer of WKTNode.

using WKTNodeNNPtr = util::nn<WKTNodePtr>
    Non-null unique pointer of WKTNode.

using WKTFormatterPtr = std::unique_ptr<WKTFormatter>
    WKTFormatter unique pointer.

using WKTFormatterNNPtr = util::nn<WKTFormatterPtr>
    Non-null WKTFormatter unique pointer.

using PROJStringFormatterPtr = std::unique_ptr<PROJStringFormatter>
    PROJStringFormatter unique pointer.

using PROJStringFormatterNNPtr = util::nn<PROJStringFormatterPtr>
    Non-null PROJStringFormatter unique pointer.

using IPROJStringExportablePtr = std::shared_ptr<IPROJStringExportable>
    Shared pointer of IPROJStringExportable.

using IPROJStringExportableNNPtr = util::nn<IPROJStringExportablePtr>
    Non-null shared pointer of IPROJStringExportable.

using AuthorityFactoryPtr = std::shared_ptr<AuthorityFactory>
    Shared pointer of AuthorityFactory.

using AuthorityFactoryNNPtr = util::nn<AuthorityFactoryPtr>
    Non-null shared pointer of AuthorityFactory.
Functions

```cpp
static crs::GeodeticCRSNNPtr cloneWithProps(const crs::GeodeticCRSNNPtr &geodCRS, const util::PropertyMap &props)
```

```cpp
util::BaseObjectNNPtr createFromUserInput(const std::string &text, const DatabaseContext &dbContext, bool usePROJ4InitRules)
```

Instantiate a sub-class of BaseObject from a user specified text.

The text can be a:
- WKT string
- PROJ string
- database code, prefixed by its authority. e.g. “EPSG:4326”
- OGC URN combining references for compound coordinate reference systems e.g. “urn:ogc:def:crs:EPSG::2393,crs:EPSG::5717” We also accept a custom abbreviated syntax EPSG:2393+5717
- OGC URN combining references for concatenated operations e.g. “urn:ogc:def:coordinateOperation,coordinateOperation:EPSG::3895,coordinateOperation:EPSG::1618”
- an Object name. e.g “WGS 84”, “WGS 84 / UTM zone 31N”. In that case as uniqueness is not guaranteed, the function may apply heuristics to determine the appropriate best match.

Parameters

- `text`: One of the above mentioned text format
- `dbContext`: Database context, or nullptr (in which case database lookups will not work)
- `usePROJ4InitRules`: When set to true, init=epsg:XXXX syntax will be allowed and will be interpreted according to PROJ.4 and PROJ.5 rules, that is geodeticCRS will have longitude, latitude order and will expect/output coordinates in radians. ProjectedCRS will have easting, northing axis order (except the ones with Transverse Mercator South Orientated projection). In that mode, the epsg:XXXX syntax will be also interpreted the same way.

Exceptions

- `ParsingException`

```cpp
util::BaseObjectNNPtr createFromUserInput(const std::string &text, PJ_CONTEXT *ctx)
```

Instantiate a sub-class of BaseObject from a user specified text.

The text can be a:
- WKT string
- PROJ string
- database code, prefixed by its authority. e.g. “EPSG:4326”
- OGC URN combining references for compound coordinate reference systems e.g. “urn:ogc:def:crs:EPSG::2393,crs:EPSG::5717” We also accept a custom abbreviated syntax EPSG:2393+5717
- OGC URN combining references for concatenated operations e.g. "urn:ogc:def:coordinateOperation,coordinateOperation:EPSG::3895,coordinateOperation:EPSG::1618"
- an Object name. e.g “WGS 84”, “WGS 84 / UTM zone 31N”. In that case as uniqueness is not guaranteed, the function may apply heuristics to determine the appropriate best match.

Parameters

- text: One of the above mentioned text format
- ctx: PROJ context

Exceptions

- ParsingException

class AuthorityFactory

#include <io.hpp> Builds object from an authority database.

A AuthorityFactory should be used only by one thread at a time.

Remark Implements AuthorityFactory from GeoAPI

Public Types

enum ObjectType

Object type.

Values:

PRIME_MERIDIAN

Object of type datum::PrimeMeridian

ELLIPSOID

Object of type datum::Ellipsoid

DATUM

Object of type datum::Datum (and derived classes)

GEODETIC_REFERENCE_FRAME

Object of type datum::GeodeticReferenceFrame (and derived classes)

VERTICAL_REFERENCE_FRAME

Object of type datum::VerticalReferenceFrame (and derived classes)

CRS

Object of type crs::CRS (and derived classes)

GEODETIC_CRS

Object of type crs::GeodeticCRS (and derived classes)

GEOCENTRIC_CRS

GEODETIC_CRS of type geocentric

GEOGeneric_CRS

Object of type crs::GeographicCRS (and derived classes)

GEOGRAPHIC_2D_CRS

GEOGeneric_CRS of type Geographic 2D

GEOGRAPHIC_3D_CRS

GEOGeneric_CRS of type Geographic 3D
Public Functions

util::BaseObjectNNPtr createObject (const std::string &code) const
Returns an arbitrary object from a code.

The returned object will typically be an instance of Datum, CoordinateSystem, ReferenceSystem or CoordinateOperation. If the type of the object is know at compile time, it is recommended to invoke the most precise method instead of this one (for example createCoordinateReferenceSystem(code) instead of createObject(code) if the caller know he is asking for a coordinate reference system).

If there are several objects with the same code, a FactoryException is thrown.

Return object.
Parameters
  • code: Object code allocated by authority. (e.g. “4326”)

Exceptions
  • NoSuchAuthorityCodeException:
  • FactoryException:

UnitOfMeasureNNPtr createUnitOfMeasure (const std::string &code) const
Returns a common::UnitOfMeasure from the specified code.

Return object.
Parameters
  • code: Object code allocated by authority.

Exceptions
  • NoSuchAuthorityCodeException:
  • FactoryException:

metadata::ExtentNNPtr createExtent (const std::string &code) const
Returns a metadata::Extent from the specified code.

Return object.
Parameters
  • code: Object code allocated by authority.

Exceptions
  • NoSuchAuthorityCodeException:
  • FactoryException:
datum::PrimeMeridianNNPtr createPrimeMeridian(const std::string &code) const
Returns a datum::PrimeMeridian from the specified code.

Parameters
• code: Object code allocated by authority.

Exceptions
• NoSuchAuthorityCodeException:
• FactoryException:

std::string identifyBodyFromSemiMajorAxis(double a, double tolerance) const
Identify a celestial body from an approximate radius.

Return celestial body name if one single match found.

Parameters
• semi_major_axis: Approximate semi-major axis.
• tolerance: Relative error allowed.

Exceptions
• FactoryException:

datum::EllipsoidNNPtr createEllipsoid(const std::string &code) const
Returns a datum::Ellipsoid from the specified code.

Parameters
• code: Object code allocated by authority.

Exceptions
• NoSuchAuthorityCodeException:
• FactoryException:

datum::DatumNNPtr createDatum(const std::string &code) const
Returns a datum::Datum from the specified code.

Parameters
• code: Object code allocated by authority.

Exceptions
• NoSuchAuthorityCodeException:
• FactoryException:

datum::GeodeticReferenceFrameNNPtr createGeodeticDatum(const std::string &code)
Returns a datum::GeodeticReferenceFrame from the specified code.

Parameters
• code: Object code allocated by authority.

Exceptions
• NoSuchAuthorityCodeException:
• FactoryException:

datum::VerticalReferenceFrameNNPtr createVerticalDatum(const std::string &code)
Returns a datum::VerticalReferenceFrame from the specified code.

Parameters
• code: Object code allocated by authority.

Exceptions
PROJ coordinate transformation software library, Release 6.1.1

- NoSuchAuthorityCodeException
- FactoryException

```cpp
cs::CoordinateSystemNNPtr createCoordinateSystem(const std::string &code) const
Returns a cs::CoordinateSystem from the specified code.

Return object.
Parameters
  - code: Object code allocated by authority.
Exceptions
  - NoSuchAuthorityCodeException
  - FactoryException
```

```cpp
crs::GeodeticCRSNNPtr createGeodeticCRS(const std::string &code) const
Returns a crs::GeodeticCRS from the specified code.

Return object.
Parameters
  - code: Object code allocated by authority.
Exceptions
  - NoSuchAuthorityCodeException
  - FactoryException
```

```cpp
crs::GeographicCRSNNPtr createGeographicCRS(const std::string &code) const
Returns a crs::GeographicCRS from the specified code.

Return object.
Parameters
  - code: Object code allocated by authority.
Exceptions
  - NoSuchAuthorityCodeException
  - FactoryException
```

```cpp
crs::VerticalCRSNNPtr createVerticalCRS(const std::string &code) const
Returns a crs::VerticalCRS from the specified code.

Return object.
Parameters
  - code: Object code allocated by authority.
Exceptions
  - NoSuchAuthorityCodeException
  - FactoryException
```

```cpp
operation::ConversionNNPtr createConversion(const std::string &code) const
Returns a operation::Conversion from the specified code.

Return object.
Parameters
  - code: Object code allocated by authority.
Exceptions
  - NoSuchAuthorityCodeException
  - FactoryException
```

```cpp
crs::ProjectedCRSNNPtr createProjectedCRS(const std::string &code) const
Returns a crs::ProjectedCRS from the specified code.

Return object.
Parameters
  - code: Object code allocated by authority.
Exceptions

- NoSuchAuthorityCodeException:
- FactoryException:

```cpp
crs::CompoundCRSNNPtr createCompoundCRS (const std::string &code) const
```
Returns a `crs::CompoundCRS` from the specified code.

**Return** object.

**Parameters**

- `code`: Object code allocated by authority.

**Exceptions**

- NoSuchAuthorityCodeException:
- FactoryException:

```cpp
crs::CRSNNPtr createCoordinateReferenceSystem (const std::string &code) const
```
Returns a `crs::CRS` from the specified code.

**Return** object.

**Parameters**

- `code`: Object code allocated by authority.

**Exceptions**

- NoSuchAuthorityCodeException:
- FactoryException:

```cpp
operation::CoordinateOperationNNPtr createCoordinateOperation (const std::string &code, bool usePROJAlternativeGridNames) const
```
Returns a `operation::CoordinateOperation` from the specified code.

**Return** object.

**Parameters**

- `code`: Object code allocated by authority.
- `usePROJAlternativeGridNames`: Whether PROJ alternative grid names should be substituted to the official grid names.

**Exceptions**

- NoSuchAuthorityCodeException:
- FactoryException:

```cpp
std::vector<operation::CoordinateOperationNNPtr> createFromCoordinateReferenceSystemCodes (const std::string &sourceCRSCode, const std::string &targetCRSCode) const
```
Returns a list `operation::CoordinateOperation` between two CRS.

The list is ordered with preferred operations first. No attempt is made at inferring operations that are not explicitly in the database.

Deprecated operations are rejected.

**Return** list of coordinate operations

**Parameters**

- `sourceCRSCode`: Source CRS code allocated by authority.
- `targetCRSCode`: Source CRS code allocated by authority.
Exceptions

- `NoSuchAuthorityCodeException`
- `FactoryException`

```cpp
const std::string &getAuthority() {
    Returns the authority name associated to this factory.
    
    Return name.
}
```

```cpp
std::set<std::string> getAuthorityCodes(const ObjectType &type, bool allowDeprecated = true) const
    Returns the set of authority codes of the given object type.
    
    Return the set of authority codes for spatial reference objects of the given type.
    
    Parameters
    - `type`: Object type.
    - `allowDeprecated`: whether we should return deprecated objects as well.
    
    Exceptions
    - `FactoryException`
```

```cpp
std::string getDescriptionText(const std::string &code) const
    Gets a description of the object corresponding to a code.
    
    Note In case of several objects of different types with the same code, one of them will be arbitrarily selected.
    
    Return description.
    
    Parameters
    - `code`: Object code allocated by authority. (e.g. “4326”)
    
    Exceptions
    - `NoSuchAuthorityCodeException`
    - `FactoryException`
```

```cpp
std::list<AuthorityFactory::CRSInfo> getCRSInfoList() const
    Return a list of information on CRS objects.
    
    This is functionnaly equivalent of listing the codes from an authority, instantiating a CRS object for each of them and getting the information from this CRS object, but this implementation has much less overhead.
    
    Exceptions
    - `FactoryException`
```

```cpp
const DatabaseContextNNPtr &databaseContext() const
    Returns the database context.
```
std::vector<operation::CoordinateOperationNNPtr>createFromCoordinateReferenceSystemCodes(const std::string &sourceCRSAuthName, const std::string &sourceCRSCode, const std::string &targetCRSAuthName, const std::string &targetCRSCodes, bool usePROJAlternativeGridNames, bool discardIfMissingGrid, bool discardSuperseded) const

Returns a list operation::CoordinateOperation between two CRS.

The list is ordered with preferred operations first. No attempt is made at inferring operations that are not explicitly in the database (see createFromCRSCodesWithIntermediates() for that), and only source - target operations are searched (ie if target -> source is present, you need to call this method with the arguments reversed, and apply the reverse transformations).

Deprecated operations are rejected.

If getAuthority() returns empty, then coordinate operations from all authorities are considered.

Return list of coordinate operations

Parameters
  * sourceCRSAuthName: Authority name of sourceCRSCode
• **sourceCRSCode**: Source CRS code allocated by authority `sourceCRSAuthName`.
• **targetCRSAuthName**: Authority name of `targetCRSCode`.
• **targetCRSCode**: Source CRS code allocated by authority `targetCRSAuthName`.
• **usePROJAlternativeGridNames**: Whether PROJ alternative grid names should be substituted to the official grid names.
• **discardIfMissingGrid**: Whether coordinate operations that reference missing grids should be removed from the result set.
• **discardSuperseded**: Whether coordinate operations that are superseded (but not deprecated) should be removed from the result set.

**Exceptions**

- **NoSuchAuthorityCodeException**:
- **FactoryException**: 

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std::vector<operation::CoordinateOperationNNPtr> createFromCRSCodesWithIntermediates(const std::string &sourceCRSAuthName, const std::string &sourceCRSCode, const std::string &targetCRSAuthName, const std::string &targetCRSCode, bool usePROJAlternativeGridNames, bool discardIfMissingGrid, bool discardSuperseded, const std::vector<std::pair<std::string, std::string>> &intermediateCodes)

Returns a list operation::CoordinateOperation between two CRS, using intermediate codes.
The list is ordered with preferred operations first.

Deprecated operations are rejected.

The method will take care of considering all potential combinations (ie contrary to `createFromCoordinateReferenceSystemCodes()`, you do not need to call it with sourceCRS and targetCRS switched)

If `getAuthority()` returns empty, then coordinate operations from all authorities are considered.

**Return** list of coordinate operations

**Parameters**

- `sourceCRSAuthName`: Authority name of sourceCRSCode
- `sourceCRSCode`: Source CRS code allocated by authority `sourceCRSAuthName`.
- `targetCRSAuthName`: Authority name of targetCRSCode
- `targetCRSCode`: Source CRS code allocated by authority `targetCRSAuthName`.
- `usePROJAlternativeGridNames`: Whether PROJ alternative grid names should be substituted to the official grid names.
- `discardIfMissingGrid`: Whether coordinate operations that reference missing grids should be removed from the result set.
- `discardSuperseded`: Whether coordinate operations that are superseded (but not deprecated) should be removed from the result set.
- `intermediateCRSAuthCodes`: List of (auth_name, code) of CRS that can be used as potential intermediate CRS. If the list is empty, the database will be used to find common CRS in operations involving both the source and target CRS.

**Exceptions**

- `NoSuchAuthorityCodeException`
- `FactoryException`

```cpp
std::string getOfficialNameFromAlias(const std::string &aliasedName, const std::string &tableName, const std::string &source, bool tryEquivalentNameSpelling, std::string &outTableName, std::string &outAuthName, std::string &outCode) const
```

Gets the official name from a possibly alias name.

**Return** official name (or empty if not found).

**Parameters**

- `aliasedName`: Alias name.
- `tableName`: Table name/category. Can help in case of ambiguities. Or empty otherwise.
- `tryEquivalentNameSpelling`: whether the comparison of aliasedName with the alt_name column of the alis_name table should be done with using `metadata::Identifier::isEquivalentName()` rather than strict string comparison;
- `outTableName`: Table name in which the official name has been found.
- `outAuthName`: Authority name of the official name that has been found.
- `outCode`: Code of the official name that has been found.

**Exceptions**

- `FactoryException`

```cpp
std::list<common::IdentifiedObjectNNPtr> createObjectsFromName(const std::string &name, const std::vector<ObjectType> &allowedObjectTypes = std::vector<ObjectType>(), bool approximateMatch = true, size_t limitResultCount = 0) const
```
Return a list of objects by their name.

**Return** list of matched objects.

**Parameters**
- `searchedName`: Searched name. Must be at least 2 character long.
- `allowedObjectTypes`: List of object types into which to search. If empty, all object types will be searched.
- `approximateMatch`: Whether approximate name identification is allowed.
- `limitResultCount`: Maximum number of results to return. Or 0 for unlimited.

**Exceptions**
- `FactoryException`:

```cpp
std::list<std::pair<std::string, std::string>> listAreaOfUseFromName(const std::string &name, bool approximateMatch) const
```

Return a list of area of use from their name.

**Return** list of (auth_name, code) of matched objects.

**Parameters**
- `name`: Searched name.
- `approximateMatch`: Whether approximate name identification is allowed.

**Exceptions**
- `FactoryException`:

---

**Public Static Functions**

```cpp
AuthorityFactoryNNPtr create(const DatabaseContextNNPtr &context, const std::string &authorityName)
```

Instantiate a `AuthorityFactory`.

The authority name might be set to the empty string in the particular case where `createFromCoordinateReferenceSystemCodes(const std::string&, const std::string&, const std::string&, const std::string&)` const is called.

**Return** new `AuthorityFactory`.

**Parameters**
- `context`: Contexte.
- `authorityName`: Authority name.

```cpp
struct CRSInfo
#include <io.hpp> CRS information
```

**Public Members**

```cpp
std::string authName
Authority name
```

```cpp
std::string code
Code
```

```cpp
std::string name
Name
```

**ObjectType type**

Type
bool deprecated
    Whether the object is deprecated

bool bbox_valid
    Whereas the west_lon_degree, south_lat_degree, east_lon_degree and north_lat_degree fields are
    valid.

double west_lon_degree
    Western-most longitude of the area of use, in degrees.

double south_lat_degree
    Southern-most latitude of the area of use, in degrees.

double east_lon_degree
    Eastern-most longitude of the area of use, in degrees.

double north_lat_degree
    Northern-most latitude of the area of use, in degrees.

std::string areaName
    Name of the area of use.

std::string projectionMethodName
    Name of the projection method for a projected CRS. Might be empty even for projected CRS in
    some cases.

class DatabaseContext
    #include <io.hpp> Database context.

    A database context should be used only by one thread at a time.

Public Functions

    const std::string & getPath () const
        Return the path to the database.

    const char * getMetadata (const char *key) const
        Return a metadata item.

        Value remains valid while this is alive and to the next call to getMetadata

    std::set<std::string> getAuthorities () const
        Return the list of authorities used in the database.

    std::vector<std::string> getDatabaseStructure () const
        Return the list of SQL commands (CREATE TABLE, CREATE TRIGGER, CREATE VIEW) needed
        to initialize a new database.

Public Static Functions

    DatabaseContextNNPtr create (const std::string &databasePath = std::string(), const
    std::vector<std::string> &auxiliaryDatabasePaths = std::vector<std::string>(), PJ_CONTEXT *ctx = nullptr)

        Instantiate a database context.

        This database context should be used only by one thread at a time.

Parameters
• databasePath: Path and filename of the database. Might be empty string for the default rules to locate the default proj.db
• auxiliaryDatabasePaths: Path and filename of auxiliary databases. Might be empty.
• ctx: Context used for file search.

Exceptions
• FactoryException:

```cpp
class FactoryException : public osgeo::proj::util::Exception
#include <io.hpp> Exception thrown when a factory can’t create an instance of the requested object.
```

Subclassed by `osgeo::proj::io::NoSuchAuthorityCodeException`

```cpp
class FormattingException : public osgeo::proj::util::Exception
#include <io.hpp> Exception possibly thrown by IWKTExportable::exportToWKT() or IPROJStringExportable::exportToPROJString().
```

```cpp
class IPROJStringExportable
#include <io.hpp> Interface for an object that can be exported to a PROJ string.
```

Subclassed by `osgeo::proj::crs::BoundCRS`, `osgeo::proj::crs::CompoundCRS`, `osgeo::proj::crs::GeodeticCRS`, `osgeo::proj::crs::ProjectedCRS`, `osgeo::proj::crs::VerticalCRS`, `osgeo::proj::datum::Ellipsoid`, `osgeo::proj::datum::PrimeMeridian`, `osgeo::proj::operation::CoordinateOperation`

### Public Functions

```cpp
std::string exportToPROJString (PROJStringFormatter *formatter) const
Builds a PROJ string representation.
```

- For `PROJStringFormatter::Convention::PROJ_5` (the default),
  - For a `crs::CRS`, returns the same as `PROJStringFormatter::Convention::PROJ_4`. It should be noted that the export of a CRS as a PROJ string may cause loss of many important aspects of a CRS definition. Consequently it is discouraged to use it for interoperability in newer projects. The choice of a WKT representation will be a better option.
  - For `operation::CoordinateOperation`, returns a PROJ pipeline.
- For `PROJStringFormatter::Convention::PROJ_4`, format a string compatible with the OGRSpatialReference::exportToProj4() of GDAL <=2.3. It is only compatible of a few CRS objects. The PROJ string will also contain a +type=crs parameter to disambiguate the nature of the string from a CoordinateOperation.
  - For a `crs::GeographicCRS`, returns a proj=longlat string, with ellipsoid / datum / prime meridian information, ignoring axis order and unit information.
  - For a geocentric `crs::GeodeticCRS`, returns the transformation from geographic coordinates into geocentric coordinates.
  - For a `crs::ProjectedCRS`, returns the projection method, ignoring axis order.
  - For a `crs::BoundCRS`, returns the PROJ string of its source/base CRS, amended with towgs84 / nadgrids parameter when the deriving conversion can be expressed in that way.

Return a PROJ string.

### Parameters

- `formatter`: PROJ string formatter.

### Exceptions

- `FormattingException`:

```cpp
class IWKTExportable
#include <io.hpp> Interface for an object that can be exported to WKT.
```
Subclassed by osgeo::proj::common::IdentifiedObject, osgeo::proj::metadata::Identifier, osgeo::proj::operation::GeneralParameterValue, osgeo::proj::operation::ParameterValue

**Public Functions**

```cpp
std::string exportToWKT (WKTFormatter *formatter) const
    Builds a WKT representation. May throw a FormattingException
```

```cpp
class NoSuchAuthorityCodeException : public osgeo::proj::io::FactoryException
    #include <io.hpp> Exception thrown when an authority factory can’t find the requested authority code.
```

**Public Functions**

```cpp
const std::string &getAuthority () const
    Returns authority name.
```

```cpp
const std::string &getAuthorityCode () const
    Returns authority code.
```

```cpp
class ParsingException : public osgeo::proj::util::Exception
    #include <io.hpp> Exception possibly thrown by WKTNode::createFrom() or WKTParser::createFromWKT().
```

```cpp
class PROJStringFormatter
    #include <io.hpp> Formatter to PROJ strings.
```

An instance of this class can only be used by a single thread at a time.

**Public Types**

```cpp
enum Convention
    PROJ variant.
    Values:
    PROJ_5
        PROJ v5 (or later versions) string.
    PROJ_4
        PROJ v4 string as output by GDAL exportToProj4()
```

**Public Functions**

```cpp
void setUseApproxTMerc (bool flag)
    Set whether approximate Transverse Mercator or UTM should be used.
```

```cpp
const std::string &toString () const
    Returns the PROJ string.
```
Public Static Functions

\texttt{PROJStringFormatterNNPtr\ create(\ Convention\ conventionIn = \ Convention::PROJ\_5, DatabaseContextPtr\ dbContext = nullptr)}

Constructs a new formatter.
A formatter can be used only once (its internal state is mutated)
Its default behaviour can be adjusted with the different setters.

\textbf{Return} new formatter.

\textbf{Parameters}
- \texttt{conventionIn}: PROJ string flavor. Defaults to \texttt{Convention::PROJ\_5}
- \texttt{dbContext}: Database context (can help to find alternative grid names). May be nullptr

\textbf{class PROJStringParser}
\begin{verbatim}
#include <io.hpp>
\end{verbatim}

Parse a PROJ string into the appropriate subclass of \texttt{util::BaseObject}.

Public Functions

\texttt{PROJStringParser\ &attachDatabaseContext(const\ DatabaseContextPtr\ &dbContext)}

Attach a database context, to allow queries in it if needed.

\texttt{PROJStringParser\ &setUsePROJ4InitRules(bool\ enable)}

Set how init=epsg:XXXX syntax should be interpreted.

\textbf{Parameters}
- \texttt{enable}: When set to true, init=epsg:XXXX syntax will be allowed and will be interpreted
  according to PROJ.4 and PROJ.5 rules, that is geodeticCRS will have longitude, latitude order
  and will expect/output coordinates in radians. ProjectedCRS will have easting, northing axis
  order (except the ones with Transverse Mercator South Orientated projection).

\texttt{std::vector<std::string>\ warningList()}\ const

Return the list of warnings found during parsing.

\texttt{BaseObjectNNPtr\ createFromPROJString(const\ std::string\ &projString)}

Instantiate a sub-class of BaseObject from a PROJ string.

The projString must contain +type=crs for the object to be detected as a CRS instead of a CoordinateOperation.

\textbf{Exceptions}
- \texttt{ParsingException}

\textbf{class WKTFormatter}
\begin{verbatim}
#include <io.hpp>
\end{verbatim}

Formatter to WKT strings.

An instance of this class can only be used by a single thread at a time.
Public Types

enum Convention_
  WKT variant.

Values:

WKT2
  Full WKT string, conforming to ISO 19162:2015(E) / OGC 12-063r5 (_WKT2_2015) with all possible nodes and new keyword names.

_WKT2_2015 = WKT2

WKT2_SIMPLIFIED
  Same as WKT2 with the following exceptions:
  • UNIT keyword used.
  • ID node only on top element.
  • No ORDER element in AXIS element.
  • PRIMEM node omitted if it is Greenwich.
  • ELLIPSOID.UNIT node omitted if it is UnitOfMeasure::METRE.
  • PARAMETER.UNIT / PRIMEM.UNIT omitted if same as AXIS.
  • AXIS.UNIT omitted and replaced by a common GEODCRS.UNIT if they are all the same on all axis.

_WKT2_2015_SIMPLIFIED = WKT2_SIMPLIFIED

_WKT2_2018
  Full WKT string, conforming to ISO 19162:2018 / OGC 18-010, with (_WKT2_2018) all possible nodes and new keyword names. Non-normative list of differences:
  • _WKT2_2018 uses GEOGCRS / BASEGEOGCRS keywords for GeographicCRS.

_WKT2_2018_SIMPLIFIED
  _WKT2_2018 with the simplification rule of WKT2_SIMPLIFIED

_WKT1_GDAL
  WKT1 as traditionally output by GDAL, deriving from OGC 01-009. A notable departure from _WKT1_GDAL with respect to OGC 01-009 is that in _WKT1_GDAL, the unit of the PRIMEM value is always degrees.

_WKT1_ESRI
  WKT1 as traditionally output by ESRI software, deriving from OGC 99-049.

enum OutputAxisRule
  Rule for output AXIS nodes

Values:

YES
  Always include AXIS nodes

NO
  Never include AXIS nodes

_WKT1_GDAL_EPSG_STYLE
  Includes them only on PROJCS node if it uses Easting/Northing ordering. Typically used for _WKT1_GDAL
Public Functions

WKTFormatter &setMultiLine (bool multiLine)
   Whether to use multi line output or not.

WKTFormatter &setIndentationWidth (int width)
   Set number of spaces for each indentation level (defaults to 4).

WKTFormatter &setOutputAxis (OutputAxisRule outputAxis)
   Set whether AXIS nodes should be output.

WKTFormatter &setStrict (bool strict)
   Set whether the formatter should operate on strict more or not.
   The default is strict mode, in which case a FormattingException can be thrown.

bool isStrict () const
   Returns whether the formatter is in strict mode.

const std::string &toString () const
   Returns the WKT string from the formatter.

Public Static Functions

WKTFormatterNNPtr create (Convention_ convention = Convention_::WKT2, DatabaseContextPtr dbContext = nullptr)
   Constructs a new formatter.
   A formatter can be used only once (its internal state is mutated)
   Its default behaviour can be adjusted with the different setters.
   Return new formatter.
   Parameters
      • convention: WKT flavor. Defaults to Convention_::WKT2
      • dbContext: Database context, to allow queries in it if needed. This is used for example for _WKT1_ESRI output to do name substitutions.

WKTFormatterNNPtr create (const WKTFormatterNNPtr &other)
   Constructs a new formatter from another one.
   A formatter can be used only once (its internal state is mutated)
   Its default behaviour can be adjusted with the different setters.
   Return new formatter.
   Parameters
      • other: source formatter.

class WKTNode
   #include <io.hpp> Node in the tree-splitted WKT representation.
Public Functions

`WKTNode (const std::string &valueIn)`
Instantiate a `WKTNode`.

Parameters
- `valueIn`: the name of the node.

`const std::string &value () const`
Return the value of a node.

`const std::vector<WKTNodeNNPtr> &children () const`
Return the children of a node.

`void addChild (WKTNodeNNPtr &&child)`
Adds a child to the current node.

Parameters
- `child`: child to add. This should not be a parent of this node.

`const WKTNodePtr &lookForChild (const std::string &childName, int occurrence = 0)`
Return the (occurrence-1)th sub-node of name `childName`.

Return the child, or `nullptr`.

Parameters
- `childName`: name of the child.
- `occurrence`: occurrence index (starting at 0)

`int countChildrenOfName (const std::string &childName) const`
Return the count of children of given name.

Return count

Parameters
- `childName`: name of the children to look for.

`std::string toString () const`
Return a WKT representation of the tree structure.

Public Static Functions

`WKTNodeNNPtr createFrom (const std::string &wkt, size_t indexStart = 0)`
Instantiate a `WKTNode` hierarchy from a WKT string.

Parameters
- `wkt`: the WKT string to parse.
- `indexStart`: the start index in the wkt string.

Exceptions
- `ParsingException`:

class `WKTParser`

`#include <io.hpp>` Parse a WKT string into the appropriate subclass of `util::BaseObject`.

10.5. Reference
Public Types

```cpp
enum WKTGuessedDialect
{
    WKT2_2018,
    WKT2_2015,
    WKT1_GDAL,
    WKT1_ESRI,
    NOT_WKT
};
```

Values:
- `WKT2_2018`
- `WKT2_2015`
- `WKT1_GDAL`
- `WKT1_ESRI`
- `NOT_WKT`

Public Functions

```cpp
WKTParser &attachDatabaseContext (const DatabaseContextPtr &dbContext)
{
    Attach a database context, to allow queries in it if needed.
}

WKTParser &setStrict (bool strict)
{
    Set whether parsing should be done in strict mode.
}

std::list<std::string> warningList () const
{
    Return the list of warnings found during parsing.
    
    Note: The list might be non-empty only if setStrict(false) has been called.
}

BaseObjectNNPtr createFromWKT (const std::string &wkt)
{
    Instantiate a sub-class of BaseObject from a WKT string.
    
    By default, validation is strict (to the extent of the checks that are actually implemented. Currently only WKT1 strict grammar is checked), and any issue detected will cause an exception to be thrown, unless setStrict(false) is called priorly.
    
    In non-strict mode, non-fatal issues will be recovered and simply listed in warningList(). This does not prevent more severe errors to cause an exception to be thrown.
}

Exceptions

- `ParsingException`

```cpp
WKTParser::WKTGuessedDialect guessDialect (const std::string &wkt)
{
    Guess the “dialect” of the WKT string.
}
10.5.4 Deprecated API

## Contents

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### 10.5.4.1 Introduction

Procedure `pj_init()` selects and initializes a cartographic projection with its argument control parameters. `argc` is the number of elements in the array of control strings `argv` that each contain individual cartographic control keyword assignments (+ proj arguments). The list must contain at least the `proj=projection` and Earth’s radius or elliptical parameters. If the initialization of the projection is successful a valid address is returned otherwise a NULL value.

The `pj_init_plus()` function operates similarly to `pj_init()` but takes a single string containing the definition, with each parameter prefixed with a plus sign. For example `+proj=utm +zone=11 +ellps=WGS84`.

Once initialization is performed either forward or inverse projections can be performed with the returned value of `pj_init()` used as the argument `proj`. The argument structure `projUV` values `u` and `v` contain respective longitude and latitude or `x` and `y`. Latitude and longitude are in radians. If a projection operation fails, both elements of `projUV` are set to `HUGE_VAL` (defined in `math.h`).

Note: all projections have a forward mode, but some do not have an inverse projection. If the projection does not have an inverse the `projPJ` structure element `inv` will be NULL.

The `pj_transform` function may be used to transform points between the two provided coordinate systems. In addition to converting between cartographic projection coordinates and geographic coordinates, this function also takes care of datum shifts if possible between the source and destination coordinate system. Unlike `pj_fwd()` and `pj_inv()` it is also allowable for the coordinate system definitions (`projPJ` *) to be geographic coordinate.
PROJ coordinate transformation software library, Release 6.1.1

systems (defined as +proj=latlong). The x, y and z arrays contain the input values of the points, and are replaced with the output values. The function returns zero on success, or the error number (also in pj_errno) on failure. Memory associated with the projection may be freed with pj_free().

10.5.4.2 Example

The following program reads latitude and longitude values in decimal degrees, performs Mercator projection with a Clarke 1866 ellipsoid and a 33° latitude of true scale and prints the projected cartesian values in meters:

```c
#include <proj_api.h>

main(int argc, char **argv) {
  projPJ pj_merc, pj_latlong;
  double x, y;
  if (!(pj_merc = pj_init_plus("+proj=merc +ellps=clrk66 +lat_ts=33")))
    exit(1);
  if (!(pj_latlong = pj_init_plus("+proj=latlong +ellps=clrk66")))
    exit(1);
  while (scanf("%lf %lf", &x, &y) == 2) {
    x *= DEG_TO_RAD;
    y *= DEG_TO_RAD;
    p = pj_transform(pj_latlong, pj_merc, 1, 1, &x, &y, NULL);
    printf("%.2f\t%.2f\n", x, y);
  }
  exit(0);
}
```

For this program, an input of -16 20.25 would give a result of -1495284.21 1920596.79.

10.5.4.3 API Functions

pj_transform

```c
int pj_transform( projPJ srcdefn,
                 projPJ dstdefn,
                 long point_count,
                 int point_offset,
                 double *x,
                 double *y,
                 double *z );
```

Transform the x/y/z points from the source coordinate system to the destination coordinate system.

srcdefn: source (input) coordinate system.
dstdefn: destination (output) coordinate system.
point_count: the number of points to be processed (the size of the x/y/z arrays).
point_offset: the step size from value to value (measured in doubles) within the x/y/z arrays - normally 1 for a packed array. May be used to operate on xyz interleaved point arrays.
x/y/z: The array of X, Y and Z coordinate values passed as input, and modified in place for output. The Z may optionally be NULL.
return: The return is zero on success, or a PROJ.4 error code.
The `pj_transform()` function transforms the passed in list of points from the source coordinate system to the destination coordinate system. Note that geographic locations need to be passed in radians, not decimal degrees, and will be returned similarly. The z array may be passed as NULL if Z values are not available.

If there is an overall failure, an error code will be returned from the function. If individual points fail to transform - for instance due to being over the horizon - then those x/y/z values will be set to `HUGE_VAL` on return. Input values that are `HUGE_VAL` will not be transformed.

**pj_init_plus**

```c
projPJ pj_init_plus(const char *definition);
```

This function converts a string representation of a coordinate system definition into a projPJ object suitable for use with other API functions. On failure the function will return NULL and set pj_errno. The definition should be of the general form `+proj=tmerc +lon_0 +datum=WGS84`. Refer to PROJ.4 documentation and the Geodetic transformation notes for additional detail.

Coordinate system objects allocated with `pj_init_plus()` should be deallocated with `pj_free()`.

**pj_free**

```c
void pj_free( projPJ pj );
```

Frees all resources associated with pj.

**pj_is_latlong**

```c
int pj_is_latlong( projPJ pj );
```

Returns TRUE if the passed coordinate system is geographic (`proj=latlong`).

**pj_is_geocent**

```c
int pj_is_geocent( projPJ pj );
```

Returns TRUE if the coordinate system is geocentric (`proj=geocent`).

**pj_get_def**

```c
char *pj_get_def( projPJ pj, int options);
```

Returns the PROJ.4 initialization string suitable for use with `pj_init_plus()` that would produce this coordinate system, but with the definition expanded as much as possible (for instance `+init=` and `+datum=` definitions).
**PROJ coordinate transformation software library, Release 6.1.1**

**pj_latlong_from_proj**

```c
projPJ pj_latlong_from_proj( projPJ pj_in );
```

Returns a new coordinate system definition which is the geographic coordinate (lat/long) system underlying `pj_in`.

**pj_set_finder**

```c
void pj_set_finder( const char *(*new_finder)(const char *) );
```

Install a custom function for finding init and grid shift files.

**pj_set_searchpath**

```c
void pj_set_searchpath ( int count, const char **path );
```

Set a list of directories to search for init and grid shift files.

**pj_deallocate_grids**

```c
void pj_deallocate_grids( void );
```

Frees all resources associated with loaded and cached datum shift grids.

**pj_strerrno**

```c
char *pj_strerrno( int );
```

Returns the error text associated with the passed in error code.

**pj_get_errno_ref**

```c
int *pj_get_errno_ref( void );
```

Returns a pointer to the global `pj_errno` error variable.

**pj_get_release**

```c
const char *pj_get_release( void );
```

Returns an internal string describing the release version.
### Obsolete Functions

```c
XY pj_fwd( LP lp, PJ *P );
LP pj_inv( XY xy, PJ *P );
projPJ pj_init(int argc, char **argv);
```

### 10.6 Using PROJ in CMake projects

The recommended way to use the PROJ library in a CMake project is to link to the imported library target `${PROJ4_LIBRARIES}` provided by the CMake configuration which comes with the library. Typical usage is:

```cmake
find_package(PROJ4)

target_link_libraries(MyApp ${PROJ4_LIBRARIES})
```

By adding the imported library target `${PROJ4_LIBRARIES}` to the target link libraries, CMake will also pass the include directories to the compiler. This requires that you use CMake version 2.8.11 or later. If you are using an older version of CMake, then add

```cmake
include_directories(${PROJ4_INCLUDE_DIRS})
```

The CMake command `find_package` will look for the configuration in a number of places. The lookup can be adjusted for all packages by setting the cache variable or environment variable `CMAKE_PREFIX_PATH`. In particular, CMake will consult (and set) the cache variable `PROJ4_DIR`.

### 10.7 Language bindings

PROJ bindings are available for a number of different development platforms.

#### 10.7.1 Python

`pyproj`: Python interface (wrapper for PROJ)

#### 10.7.2 Ruby

`proj4rb`: Bindings for PROJ in ruby

#### 10.7.3 TCL

`proj4tcl`: Bindings for PROJ in tcl (critcl source)
10.7.4 MySQL

fProj4: Bindings for PROJ in MySQL

10.7.5 Excel

proj.xll: Excel add-in for PROJ map projections

10.7.6 Visual Basic

PROJ VB Wrappers: By Eric G. Miller.

10.7.7 Fortran

Fortran-Proj: Bindings for PROJ in Fortran (By João Macedo @likeno)

10.8 Version 4 to 6 API Migration

This is a transition guide for developers wanting to migrate their code to use PROJ version 6.

10.8.1 Code example

The difference between the old and new API is shown here with a few examples. Below we implement the same program with the two different API's. The program reads input longitude and latitude from the command line and convert them to projected coordinates with the Mercator projection.

We start by writing the program for PROJ 4:

```c
#include <proj_api.h>

int main(int argc, char **argv) {
    projPJ pj_merc, pj_latlong;
    double x, y;

    if (!pj_longlat = pj_init_plus("+proj=longlat +ellps=clrk66"))
        return 1;
    if (!pj_merc = pj_init_plus("+proj=merc +datum=clrk66 +lat_ts=33"))
        return 1;

    while (scanf("%lf %lf", &x, &y) == 2) {
        x *= DEG_TO_RAD; /* longitude */
        y *= DEG_TO_RAD; /* latitude */
        p = pj_transform(pj_longlat, pj_merc, 1, 1, &x, &y, NULL);
        printf("%.2f %.2f
", x, y);
    }

    pj_free(pj_longlat);
    pj_free(pj_merc);
    return 0;
}
```
The same program implemented using PROJ 6:

```c
#include <proj.h>

main(int argc, char **argv) {
    PJ *P;
    PJ_COORD c;

    /* NOTE: the use of PROJ strings to describe CRS is strongly discouraged */
    /* in PROJ 6, as PROJ strings are a poor way of describing a CRS, and */
    /* more precise its geodetic datum. */
    /* Use of codes provided by authorities (such as "EPSG:4326", etc...) */
    /* or WKT strings will bring the full power of the "transformation */
    /* engine" used by PROJ to determine the best transformation(s) between */
    /* two CRS. */
    P = proj_create_crs_to_crs(PJ_DEFAULT_CTX,
            "+proj=longlat +ellps=clrs66",
            "+proj=merc +ellps=clrk66 +lat_ts=33",
            NULL);

    if (P==0)
        return 1;

    { /* For that particular use case, this is not needed. */
        /* proj_normalize_for_visualization() ensures that the coordinate */
        /* order expected and returned by proj_trans() will be longitude, */
        /* latitude for geographic CRS, and easting, northing for projected */
        /* CRS. If instead of using PROJ strings as above, "EPSG:XXXX" codes */
        /* had been used, this might had been necessary. */
        PJ* P_for_GIS = proj_normalize_for_visualization(C, P);
        if ( 0 == P_for_GIS ) {
            proj_destroy(P);
            return 1;
        }
        proj_destroy(P);
        P = P_for_GIS;
    }

    while (scanf("%lf %lf", &c.lp.lam, &c.lp.phi) == 2) {
        /* No need to convert to radian */
        c = proj_trans(P, PJ_FWD, c);
        printf("%.2f \t %.2f \n", c.xy.x, c.xy.y);
    }

    proj_destroy(P);
}
```

10.8. Version 4 to 6 API Migration
10.8.2 Function mapping from old to new API

<table>
<thead>
<tr>
<th>Old API functions</th>
<th>New API functions</th>
</tr>
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<tbody>
<tr>
<td>pj_fwd</td>
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</tr>
<tr>
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<td>proj_trans()</td>
</tr>
<tr>
<td>pj_fwd3</td>
<td>proj_trans()</td>
</tr>
<tr>
<td>pj_inv3</td>
<td>proj_trans()</td>
</tr>
<tr>
<td>pj_transform</td>
<td>proj_create_crs_to_crs() + (proj_normalize_for_visualization() + proj_trans(), proj_trans_array() or proj_trans_generic())</td>
</tr>
<tr>
<td>pj_init</td>
<td>proj_create() + proj_create_crs_to_crs()</td>
</tr>
<tr>
<td>pj_free</td>
<td>proj_destroy()</td>
</tr>
<tr>
<td>pj_is_latlong</td>
<td>proj_get_type()</td>
</tr>
<tr>
<td>pj_is_geocent</td>
<td>proj_get_type()</td>
</tr>
<tr>
<td>pj_get_def</td>
<td>proj_pj_info()</td>
</tr>
<tr>
<td>pj_latlong_from</td>
<td>project direct equivalent, but can be accomplished by chaining proj_create(), proj_crs_get_horizontal_datum() and proj_create_geographic_crs_from_datum()</td>
</tr>
<tr>
<td>pj_set_finder</td>
<td>proj_context_set_file_finder()</td>
</tr>
<tr>
<td>pj_set_search_path</td>
<td>proj_context_set_search_paths()</td>
</tr>
<tr>
<td>pj_deallocate</td>
<td>No equivalent</td>
</tr>
<tr>
<td>pj_strerror</td>
<td>proj_errno()</td>
</tr>
<tr>
<td>pj_get_errno_ref</td>
<td>proj_errno()</td>
</tr>
<tr>
<td>pj_get_release</td>
<td>proj_info()</td>
</tr>
</tbody>
</table>

10.9 Version 4 to 5 API Migration

This is a transition guide for developers wanting to migrate their code to use PROJ version 5.

10.9.1 Background

Before we go on, a bit of background is needed. The new API takes a different view of the world than the old because it is needed in order to obtain high accuracy transformations. The old API is constructed in such a way that any transformation between two coordinate reference systems must pass through the ill-defined WGS84 reference frame, using it as a hub. The new API does away with this limitation to transformations in PROJ. It is still possible to do that type of transformations but in many cases there will be a better alternative.

The world view represented by the old API is always sufficient if all you care about is meter level accuracy - and in many cases it will provide much higher accuracy than that. But the view that “WGS84 is the true foundation of the world, and everything else can be transformed natively to and from WGS84” is inherently flawed.

First and foremost because any time WGS84 is mentioned, you should ask yourself “Which of the six WGS84 realizations are we talking about here?”.

Second, because for many (especially legacy) systems, it may not be straightforward to transform to WGS84 (or actually ITRF-something, ETRS-something or NAD-something which appear to be the practical meaning of the term WGS84 in everyday PROJ related work), while centimeter-level accurate transformations may exist between pairs of older systems.

The concept of a hub reference frame (“datum”) is not inherently bad, but in many cases you need to handle and select that datum with more care than the old API allows. The primary aim of the new API is to allow just that. And to
do that, you must realize that the world is inherently 4 dimensional. You may in many cases assume one or more of the coordinates to be constant, but basically, to obtain geodetic accuracy transformations, you need to work in 4 dimensions.

Now, having described the background for introducing the new API, let’s try to show how to use it. First note that in order to go from system A to system B, the old API starts by doing an inverse transformation from system A to WGS84, then does a forward transformation from WGS84 to system B.

With cs2cs being the command line interface to the old API, and cct being the same for the new, this example of doing the same thing in both world views will should give an idea of the differences:

```bash
$ echo 300000 6100000 | cs2cs +proj=utm +zone=33 +ellps=GRS80 +to +proj=utm +zone=32 +ellps=GRS80
683687.87 6099299.66 0.00

$ echo 300000 6100000 0 0 | cct +proj=pipeline +step +inv +proj=utm +zone=33 +ellps=GRS80 +step +proj=utm +zone=32 +ellps=GRS80
683687.8667 6099299.6624 0.0000 0.0000
```

Lookout for the +inv in the first +step, indicating an inverse transform.

### 10.9.2 Code example

The difference between the old and new API is shown here with a few examples. Below we implement the same program with the two different API’s. The program reads input longitude and latitude from the command line and convert them to projected coordinates with the Mercator projection.

We start by writing the program for PROJ v. 4:

```c
#include <proj_api.h>

main(int argc, char **argv) {
    projPJ pj_merc, pj_longlat;
    double x, y;

    if (!(pj_longlat = pj_init_plus("+proj=longlat +ellps=clrk66")))
        return 1;
    if (!(pj_merc = pj_init_plus("+proj=merc +ellps=clrk66 +lat_ts=33")))
        return 1;

    while (scanf("%lf %lf", &x, &y) == 2) {
        x *= DEG_TO_RAD; /* longitude */
        y *= DEG_TO_RAD; /* latitude */
        p = pj_transform(pj_longlat, pj_merc, 1, 1, &x, &y, NULL);
        printf("%.2f\t%.2f\n", x, y);
    }

    pj_free(pj_longlat);
    pj_free(pj_merc);

    return 0;
}
```

The same program implemented using PROJ v. 5:
#include <proj.h>

main(int argc, char **argv) {
    PJ *P;
    PJ_COORD c;

    P = proj_create(PJ_DEFAULT_CTX, "+proj=merc +ellps=clrk66 +lat_ts=33");
    if (P==0)
        return 1;

    while (scanf("%lf %lf", &c.lp.lam, &c.lp.phi) == 2) {
        c.lp.lam = proj_torad(c.lp.lam);
        c.lp.phi = proj_torad(c.lp.phi);
        c = proj_trans(P, PJ_FWD, c);
        printf("%.2f	%.2f\n", c.xy.x, c.xy.y);
    }

    proj_destroy(P);
}

Looking at the two different programs, there’s a few immediate differences that catches the eye. First off, the included header file describing the API has changed from \texttt{proj\_api.h} to simply \texttt{proj.h}. All functions in \texttt{proj.h} belongs to the \texttt{proj} namespace.

With the new API also comes new datatypes. E.g. the transformation object \texttt{projPJ} which has been changed to a pointer of type \texttt{PJ}. This is done to highlight the actual nature of the object, instead of hiding it away behind a typedef.

New data types for handling coordinates have also been introduced. In the above example we use the \texttt{PJ\_COORD}, which is a union of various types. The benefit of this is that it is possible to use the various structs in the union to communicate what state the data is in at different points in the program. For instance as in the above example where the coordinate is read from STDIN as a geodetic coordinate, communicated to the reader of the code by using the \texttt{c.lp} struct. After it has been projected we print it to STDOUT by accessing the individual elements in \texttt{c.xy} to illustrate that the coordinate is now in projected space. Data types are prefixed with \texttt{PJ\_}.

The final, and perhaps biggest, change is that the fundamental concept of transformations in PROJ are now handled in a single transformation object (\texttt{PJ}) and not by stating the source and destination systems as previously. It is of course still possible to do just that, but the transformation object now captures the whole transformation from source to destination in one. In the example with the old API the source system is described as \texttt{+proj=latlon +ellps=clrk66} and the destination system is described as \texttt{+proj=merc +ellps=clrk66 +lat_ts=33}. Since the Mercator projection accepts geodetic coordinates as its input, the description of the source in this case is superfluous. We use that to our advantage in the new API and simply state the destination. This is simple at a glance, but is actually a big conceptual change. We are now focused on the path between two systems instead of what the source and destination systems are.
### 10.9.3 Function mapping from old to new API

<table>
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</tr>
<tr>
<td>pj_inv3</td>
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</tr>
<tr>
<td>pj_transform</td>
<td>proj_trans_array or proj_trans_generic</td>
</tr>
<tr>
<td>pj_init</td>
<td>proj_create()</td>
</tr>
<tr>
<td>pj_init_plus</td>
<td>proj_create()</td>
</tr>
<tr>
<td>pj_free</td>
<td>proj_destroy()</td>
</tr>
<tr>
<td>pj_is_latlong</td>
<td>proj_angular_output()</td>
</tr>
<tr>
<td>pj_is_geocent</td>
<td>proj_angular_output()</td>
</tr>
<tr>
<td>pj_get_def</td>
<td>proj_pj_info()</td>
</tr>
<tr>
<td>pj_latlong_from_proj</td>
<td>No equivalent</td>
</tr>
<tr>
<td>pj_set_finder</td>
<td>No equivalent</td>
</tr>
<tr>
<td>pj_set_searchpath</td>
<td>No equivalent</td>
</tr>
<tr>
<td>pj_deallocate_grids</td>
<td>No equivalent</td>
</tr>
<tr>
<td>pj_strerror</td>
<td>No equivalent</td>
</tr>
<tr>
<td>pj_get_errno_ref</td>
<td>proj_errno()</td>
</tr>
<tr>
<td>pj_get_release</td>
<td>proj_info()</td>
</tr>
</tbody>
</table>

**Attention:** The `projects.h` header and the functions related to it is considered deprecated from version 5.0.0 and onwards. The header will be removed from PROJ in version 6.0.0 scheduled for release February 1st 2019.

**Attention:** The nmake build system on Windows will not be supported from version 6.0.0 on onwards. Use CMake instead.

**Attention:** The `proj_api.h` header and the functions related to it is considered deprecated from version 5.0.0 and onwards. The header will be removed from PROJ in version 7.0.0 scheduled for release February 1st 2020.

**Attention:** With the introduction of PROJ 5, behavioural changes has been made to existing functionality. Consult *Known differences between versions* for the details.
The PROJ community is what makes the software stand out from its competitors. PROJ is used and developed by group of very enthusiastic, knowledgeable and friendly people. Whether you are a first time user of PROJ or a long-time contributor the community is always very welcoming.

11.1 Communication channels

11.1.1 Mailing list

Users and developers of the library are using the mailing list to discuss all things related to PROJ. The mailing list is the primary forum for asking for help with use of PROJ. The mailing list is also used for announcements, discussions about the development of the library and from time to time interesting discussions on geodesy appear as well. You are more than welcome to join in on the discussions!

The PROJ mailing list can be found at https://lists.osgeo.org/mailman/listinfo/proj

11.1.2 GitHub

GitHub is the development platform we use for collaborating on the PROJ code. We use GitHub to keep track of the changes in the code and to index bug reports and feature requests. We are happy to take contributions in any form, either as code, bug reports, documentation or feature requests. See Contributing for more info on how you can help improve PROJ.

The PROJ GitHub page can be found at https://github.com/OSGeo/PROJ

Note: The issue tracker on GitHub is only meant to keep track of bugs, feature request and other things related to the development of PROJ. Please ask your questions about the use of PROJ on the mailing list instead.

11.1.3 Gitter

Gitter is the instant messaging alternative to the mailing list. PROJ has a room under the OSGeo organization. Most of the core developers stop by from time to time for an informal chat. You are more than welcome to join the discussion.

The Gitter room can be found at https://gitter.im/OSGeo/proj
11.2 Contributing

PROJ has a wide and varied user base. Some are highly skilled geodesists with a deep knowledge of map projections and reference systems, some are GIS software developers and others are GIS users. All users, regardless of the profession or skill level, has the ability to contribute to PROJ. Here’s a few suggestion on how:

- Help PROJ-users that is less experienced than yourself.
- Write a bug report
- Request a new feature
- Write documentation for your favorite map projection
- Fix a bug
- Implement a new feature

In the following sections you can find some guidelines on how to contribute. As PROJ is managed on GitHub most contributions require that you have a GitHub account. Familiarity with issues and the GitHub Flow is an advantage.

11.2.1 Help a fellow PROJ user

The main forum for support for PROJ is the mailing list. You can subscribe to the mailing list here and read the archive here.

If you have questions about the usage of PROJ the mailing list is also the place to go. Please do not use the GitHub issue tracker as a support forum. Your question is much more likely to be answered on the mailing list, as many more people follow that than the issue tracker.

11.2.2 Adding bug reports

Bug reports are handled in the issue tracker on PROJ’s home on GitHub. Writing a good bug report is not easy. But fixing a poorly documented bug is not easy either, so please put in the effort it takes to create a thorough bug report.

A good bug report includes at least:

- A title that quickly explains the problem
- A description of the problem and how it can be reproduced
- Version of PROJ being used
- Version numbers of any other relevant software being used, e.g. operating system
- A description of what already has been done to solve the problem

The more information that is given up front, the more likely it is that a developer will find interest in solving the problem. You will probably get follow-up questions after submitting a bug report. Please answer them in a timely manner if you have an interest in getting the issue solved.

Finally, please only submit bug reports that are actually related to PROJ. If the issue materializes in software that uses PROJ it is likely a problem with that particular software. Make sure that it actually is a PROJ problem before you submit an issue. If you can reproduce the problem only by using tools from PROJ it is definitely a problem with PROJ.
11.2.3 Feature requests

Got an idea for a new feature in PROJ? Submit a thorough description of the new feature in the issue tracker. Please include any technical documents that can help the developer make the new feature a reality. An example of this could be a publicly available academic paper that describes a new projection. Also, including a numerical test case will make it much easier to verify that an implementation of your requested feature actually works as you expect.

Note that not all feature requests are accepted.

11.2.4 Write documentation

PROJ is in dire need of better documentation. Any contributions of documentation are greatly appreciated. The PROJ documentation is available on proj.org. The website is generated with Sphinx. Contributions to the documentation should be made as Pull Requests on GitHub.

If you intend to document one of PROJ’s supported projections please use the Mercator projection as a template.

11.2.5 Code contributions

See Code contributions

11.2.5.1 Legalese

Committers are the front line gatekeepers to keep the code base clear of improperly contributed code. It is important to the PROJ users, developers and the OSGeo foundation to avoid contributing any code to the project without it being clearly licensed under the project license.

Generally speaking the key issues are that those providing code to be included in the repository understand that the code will be released under the MIT/X license, and that the person providing the code has the right to contribute the code. For the committer themselves understanding about the license is hopefully clear. For other contributors, the committer should verify the understanding unless the committer is very comfortable that the contributor understands the license (for instance frequent contributors).

If the contribution was developed on behalf of an employer (on work time, as part of a work project, etc) then it is important that an appropriate representative of the employer understand that the code will be contributed under the MIT/X license. The arrangement should be cleared with an authorized supervisor/manager, etc.

The code should be developed by the contributor, or the code should be from a source which can be rightfully contributed such as from the public domain, or from an open source project under a compatible license.

All unusual situations need to be discussed and/or documented.

Committers should adhere to the following guidelines, and may be personally legally liable for improperly contributing code to the source repository:

- Make sure the contributor (and possibly employer) is aware of the contribution terms.
- Code coming from a source other than the contributor (such as adapted from another project) should be clearly marked as to the original source, copyright holders, license terms and so forth. This information can be in the file headers, but should also be added to the project licensing file if not exactly matching normal project licensing (COPYING).
- Existing copyright headers and license text should never be stripped from a file. If a copyright holder wishes to give up copyright they must do so in writing to the foundation before copyright messages are removed. If license terms are changed it has to be by agreement (written in email is ok) of the copyright holders.
- Code with licenses requiring credit, or disclosure to users should be added to COPYING.
• When substantial contributions are added to a file (such as substantial patches) the author/contributor should be added to the list of copyright holders for the file.
• If there is uncertainty about whether a change is proper to contribute to the code base, please seek more information from the project steering committee, or the foundation legal counsel.

11.2.6 Additional Resources

• General GitHub documentation
• GitHub pull request documentation

11.2.7 Acknowledgements

The code contribution section of this CONTRIBUTING file is inspired by PDAL’s and the legalese section is modified from GDAL committer guidelines

11.3 Guidelines for PROJ code contributors

This is a guide for PROJ, casual or regular, code contributors.

11.3.1 Code contributions.

Code contributions can be either bug fixes or new features. The process is the same for both, so they will be discussed together in this section.

11.3.1.1 Making Changes

• Create a topic branch from where you want to base your work.
• You usually should base your topic branch off of the master branch.
• To quickly create a topic branch: git checkout -b my-topic-branch
• Make commits of logical units.
• Check for unnecessary whitespace with git diff --check before committing.
• Make sure your commit messages are in the proper format.
• Make sure you have added the necessary tests for your changes.
• Make sure that all tests pass
11.3.1.2 Submitting Changes

- Push your changes to a topic branch in your fork of the repository.
- Submit a pull request to the PROJ repository in the OSGeo organization.
- If your pull request fixes/references an issue, include that issue number in the pull request. For example:

```
Wiz the bang
Fixes #123.
```

- PROJ developers will look at your patch and take an appropriate action.

11.3.1.3 Coding conventions

Programming language

PROJ is developed strictly in ANSI C 89.

Coding style

We don’t enforce any particular coding style, but please try to keep it as simple as possible. If improving existing code, please try to conform with the style of the locally surrounding code.

Whitespace

Throughout the PROJ code base you will see differing whitespace use. The general rule is to keep whitespace in whatever form it is in the file you are currently editing. If the file has a mix of tabs and space please convert the tabs to space in a separate commit before making any other changes. This makes it a lot easier to see the changes in diffs when evaluating the changed code. New files should use spaces as whitespace.

File names

Files in which projections are implemented are prefixed with an upper-case PJ_ and most other files are prefixed with lower-case pj_. Some file deviate from this pattern, most of them dates back to the very early releases of PROJ. New contributions should follow the pj-prefix pattern. Unless there are obvious reasons not to.

11.3.2 Tools

11.3.2.1 cppcheck static analyzer

You can run locally scripts/cppcheck.sh that is a wrapper script around the cppcheck utility. It is known to work with cppcheck 1.61 of Ubuntu Trusty 14.0, since this is what is currently used on Travis-CI (travis/linux_gcc/before_install.sh). At the time of writing, this also works with cppcheck 1.72 of Ubuntu Xenial 16.04, and latest cppcheck master.

cppcheck can have false positives. In general, it is preferable to rework the code a bit to make it more ‘obvious’ and avoid those false positives. When not possible, you can add a comment in the code like
in the preceding line. Replace duplicateBreak with the actual name of the violated rule emitted by cppcheck.

### 11.3.2.2 CLang Static Analyzer (CSA)

CSA is run by the Travis/csa build configuration. You may also run it locally.

Preliminary step: install clang. For example:

```
wget http://releases.llvm.org/6.0.0/clang+llvm-6.0.0-x86_64-linux-gnu-ubuntu-14.04.tar.xz
```

```
tar xJf clang+llvm-6.0.0-x86_64-linux-gnu-ubuntu-14.04.tar.xz
```

Run configure under the scan-build utility of clang:

```
./clang+llvm-6.0.0-x86_64-linux-gnu-ubuntu-14.04/bin/scan-build ./configure
```

Build under scan-build:

```
./clang+llvm-6.0.0-x86_64-linux-gnu-ubuntu-14.04/bin/scan-build make [-j8]
```

If CSA finds errors, they will be emitted during the build. And in which case, at the end of the build process, scan-build will emit a warning message indicating errors have been found and how to display the error report. This is with something like

```
./clang+llvm-6.0.0-x86_64-linux-gnu-ubuntu-14.04/bin/scan-view /tmp/scan-build-2018-03-15-121416-17476-1
```

This will open a web browser with the interactive report.

CSA may also have false positives. In general, this happens when the code is non-trivial / makes assumptions that hard to check at first sight. You will need to add extra checks or rework it a bit to make it more “obvious” for CSA. This will also help humans reading your code!

### 11.3.2.3 Typo detection and fixes

Run `scripts/fix_typos.sh`

### 11.3.2.4 Include What You Use (IWYU)

Managing C includes is a pain. IWYU makes updating headers a bit easier. IWYU scans the code for functions that are called and makes sure that the headers for all those functions are present and in sorted order. However, you cannot blindly apply IWYU to PROJ. It does not understand ifdefs, other platforms, or the order requirements of PROJ internal headers. So the way to use it is to run it on a copy of the source and merge in only the changes that make sense. Additions of standard headers should always be safe to merge. The rest require careful evaluation. See the IWYU documentation for motivation and details.

IWYU docs
11.4 Request for Comments

A PROJ RFC describes a major change in the technological underpinnings of PROJ, major additions to functionality, or changes in the direction of the project.

11.4.1 PROJ RFC 1: Project Committee Guidelines

**Author** Frank Warmerdam, Howard Butler  
**Contact** howard@hobu.co  
**Status** Passed  
**Last Updated** 2018-06-08

### 11.4.1.1 Summary

This document describes how the PROJ Project Steering Committee (PSC) determines membership, and makes decisions on all aspects of the PROJ project - both technical and non-technical.

Examples of PSC management responsibilities:

- setting the overall development road map
- developing technical standards and policies (e.g. coding standards, file naming conventions, etc.)
- ensuring regular releases (major and maintenance) of PROJ software
- reviewing RFC for technical enhancements to the software
- project infrastructure (e.g. GitHub, continuous integration hosting options, etc.)
- formalization of affiliation with external entities such as OSGeo
- setting project priorities, especially with respect to project sponsorship
- creation and oversight of specialized sub-committees (e.g. project infrastructure, training)

In brief the project team votes on proposals on the proj mailing list. Proposals are available for review for at least two days, and a single veto is sufficient delay progress though ultimately a majority of members can pass a proposal.

### 11.4.1.2 List of PSC Members

(up-to-date as of 2018-06)  
- Kristian Evers @kbevers (DK) Chair  
- Howard Butler @hobu (USA)  
- Charles Karney @cffk (USA)  
- Thomas Knudsen @busstoptaktik (DK)  
- Even Rouault @rouault (FR)  
- Kurt Schwehr @schwehr (USA)  
- Frank Warmerdam @warmerdam (USA) Emeritus
11.4.1.3 Detailed Process

- Proposals are written up and submitted on the proj mailing list for discussion and voting, by any interested party, not just committee members.
- Proposals need to be available for review for at least two business days before a final decision can be made.
- Respondents may vote “+1” to indicate support for the proposal and a willingness to support implementation.
- Respondents may vote “-1” to veto a proposal, but must provide clear reasoning and alternate approaches to resolving the problem within the two days.
- A vote of -0 indicates mild disagreement, but has no effect. A 0 indicates no opinion. A +0 indicate mild support, but has no effect.
- Anyone may comment on proposals on the list, but only members of the Project Steering Committee’s votes will be counted.
- A proposal will be accepted if it receives +2 (including the author) and no vetoes (-1).
- If a proposal is vetoed, and it cannot be revised to satisfy all parties, then it can be resubmitted for an override vote in which a majority of all eligible voters indicating +1 is sufficient to pass it. Note that this is a majority of all committee members, not just those who actively vote.
- Upon completion of discussion and voting the author should announce whether they are proceeding (proposal accepted) or are withdrawing their proposal (vetoed).
- The Chair gets a vote.
- The Chair is responsible for keeping track of who is a member of the Project Steering Committee (perhaps as part of a PSC file in CVS).
- Addition and removal of members from the committee, as well as selection of a Chair should be handled as a proposal to the committee.
- The Chair adjudicates in cases of disputes about voting.

RFC Origin

PROJ RFC and Project Steering Committee is derived from similar governance bodies in both the GDAL and MapServer software projects.

11.4.1.4 When is Vote Required?

- Any change to committee membership (new members, removing inactive members)
- Changes to project infrastructure (e.g. tool, location or substantive configuration)
- Anything that could cause backward compatibility issues.
- Adding substantial amounts of new code.
- Changing inter-subsystem APIs, or objects.
- Issues of procedure.
- When releases should take place.
- Anything dealing with relationships with external entities such as OSGeo
- Anything that might be controversial.
11.4.1.5 Observations

- The Chair is the ultimate adjudicator if things break down.
- The absolute majority rule can be used to override an obstructionist veto, but it is intended that in normal circumstances vetoers need to be convinced to withdraw their veto. We are trying to reach consensus.

11.4.1.6 Committee Membership

The PSC is made up of individuals consisting of technical contributors (e.g. developers) and prominent members of the PROJ user community. There is no set number of members for the PSC although the initial desire is to set the membership at 6.

Adding Members

Any member of the proj mailing list may nominate someone for committee membership at any time. Only existing PSC committee members may vote on new members. Nominees must receive a majority vote from existing members to be added to the PSC.

Stepping Down

If for any reason a PSC member is not able to fully participate then they certainly are free to step down. If a member is not active (e.g. no voting, no IRC or email participation) for a period of two months then the committee reserves the right to seek nominations to fill that position. Should that person become active again (hey, it happens) then they would certainly be welcome, but would require a nomination.

11.4.1.7 Membership Responsibilities

Guiding Development

Members should take an active role guiding the development of new features they feel passionate about. Once a change request has been accepted and given a green light to proceed does not mean the members are free of their obligation. PSC members voting “+1” for a change request are expected to stay engaged and ensure the change is implemented and documented in a way that is most beneficial to users. Note that this applies not only to change requests that affect code, but also those that affect the web site, technical infrastructure, policies and standards.

Mailing List Participation

PSC members are expected to be active on the proj mailing list, subject to Open Source mailing list etiquette. Non-developer members of the PSC are not expected to respond to coding level questions on the developer mailing list, however they are expected to provide their thoughts and opinions on user level requirements and compatibility issues when RFC discussions take place.
11.4.1.8 Updates

June 2018

RFC 1 was ratified by the following members

11.4.2 PROJ RFC 2: Initial integration of “GDAL SRS barn” work

**Author** Even Rouault

**Contact** even.rouault at spatialys.com

**Status** Adopted (not yet merged into master)

**Initial version** 2018-10-09

**Last Updated** 2018-10-31

11.4.2.1 Summary

This RFC is the result of a first phase of the GDAL Coordinate System Barn Raising efforts. In its current state, this work mostly consists of:

- a C++ implementation of the ISO-19111:2018 / OGC Topic 2 “Referencing by coordinates” classes to represent Datums, Coordinate systems, CRSs (Coordinate Reference Systems) and Coordinate Operations.
- methods to convert between this C++ modeling and WKT1, WKT2 and PROJ string representations of those objects
- management and query of a SQLite3 database of CRS and Coordinate Operation definition
- a C API binding part of those capabilities

11.4.2.2 Related standards

Consult Applicable standards

(They will be linked from the PROJ documentation)

11.4.2.3 Details

Structure in packages / namespaces

The C++ implementation of the (upcoming) ISO-19111:2018 / OGC Topic 2 “Referencing by coordinates” classes follows this abstract modeling as much as possible, using package names as C++ namespaces, abstract classes and method names. A new BoundCRS class has been added to cover the modeling of the WKT2 BoundCRS construct, that is a generalization of the WKT1 TOWGS84 concept. It is strongly recommended to have the ISO-19111 standard open to have an introduction for the concepts when looking at the code. A few classes have also been inspired by the GeoAPI

The classes are organized into several namespaces:

- **osgeo::proj::util** A set of base types from ISO 19103, GeoAPI and other PROJ “technical” specific classes
  
  Template optional&lt;T&gt;, classes BaseObject, IComparable, BoxedValue, ArrayOfBaseObject, PropertyMap, LocalName, NameSpace, GenericName, NameFactory, CodeList, Exception, InvalidValueType- Exception, UnsupportedOperationException
• **osgeo::proj::metadata:** Common classes from ISO 19115 (Metadata) standard
  Classes: Citation, GeographicExtent, GeographicBoundingBox, TemporalExtent, VerticalExtent, Extent, Identifier, PositionalAccuracy,

• **osgeo::proj::common:** Common classes: UnitOfMeasure, Measure, Scale, Angle, Length, DateTime, DateEpoch, IdentifiedObject, ObjectDomain, ObjectUsage

• **osgeo::proj::cs:** Coordinate systems and their axis

• **osgeo::proj::datum:** Datum (the relationship of a coordinate system to the body)

• **osgeo::proj::crs:** CRS = coordinate reference system = coordinate system with a datum
  Classes: CRS, GeodeticCRS, GeographicCRS, DerivedCRS, ProjectedCRS, VerticalCRS, CompoundCRS, BoundaryCRS, TemporalCRS, EngineeringCRS, ParametricCRS, DerivedGeodeticCRS, DerivedGeographicCRS, DerivedProjectedCRS, DerivedVerticalCRS

• **osgeo::proj::operation:** Coordinate operations (relationship between any two coordinate reference systems)

• **osgeo::proj::io:** I/O classes: WKTFormatter, PROJStringFormatter, FormattingException, ParsingException, IWKTExportable, IPROJStringExportable, WKTNode, WKTParser, PROJStringParser, DatabaseContext, AuthorityFactory, FactoryException, NoSuchAuthorityCodeException

**What does what?**

The code to parse WKT and PROJ strings and build ISO-19111 objects is contained in `io.cpp`
The code to format WKT and PROJ strings from ISO-19111 objects is mostly contained in the related `exportToWKT()` and `exportToPROJString()` methods overridden in the applicable classes. `io.cpp` contains the general mechanics to build such strings.

Regarding WKT strings, three variants are handled in import and export:
- **WKT2_2018:** variant corresponding to the upcoming ISO-19162:2018 standard
- **WKT2_2015:** variant corresponding to the current ISO-19162:2015 standard
- **WKT1_GDAL:** variant corresponding to the way GDAL understands the OGC 01-099 and OGC 99-049 standards

Regarding PROJ strings, two variants are handled in import and export:
- **PROJ5:** variant used by PROJ >= 5, possibly using pipeline constructs, and avoiding `+towgs84` / `+nadgrids` legacy constructs. This variant honours axis order and input/output units. That is the pipeline for the conversion of EPSG:4326 to EPSG:32631 will assume that the input coordinates are in latitude, longitude order, with degrees.
- **PROJ4:** variant used by PROJ 4.x

11.4. Request for Comments
The raw query of the proj.db database and the upper level construction of ISO-19111 objects from the database contents is done in factory.cpp

A few design principles

Methods generally take and return xxxNNPtr objects, that is non-null shared pointers (pointers with internal reference counting). The advantage of this approach is that the user has not to care about the life-cycle of the instances (and this makes the code leak-free by design). The only point of attention is to make sure no reference cycles are made. This is the case for all classes, except the CoordinateOperation class that point to CRS for sourceCRS and targetCRS members, whereas DerivedCRS point to a Conversion instance (which derives from CoordinateOperation). This issue was detected in the ISO-19111 standard. The solution adopted here is to use std::weak_ptr in the CoordinateOperation class to avoid the cycle. This design artifact is transparent to users.

Another important design point is that all ISO19111 objects are immutable after creation, that is they only have get- ters that do not modify their states. Consequently they could possibly use in a thread-safe way. There are however classes like PROJStringFormatter, WKTFormatter, DatabaseContext, AuthorityFactory and CoordinateOperationContext whose instances are mutable and thus can not be used by multiple threads at once.

Example how to build the EPSG:4326 / WGS84 Geographic2D definition from scratch:

```cpp
auto greenwich = PrimeMeridian::create(
    util::PropertyMap()
    .set(metadata::Identifier::CODESPACE_KEY, metadata::Identifier::EPSG)
    .set(metadata::Identifier::CODE_KEY, 8901)
    .set(common::IdentifiedObject::NAME_KEY, "Greenwich"),
    common::Angle(0));
// actually predefined as PrimeMeridian::GREENWICH constant

auto ellipsoid = Ellipsoid::createFlattenedSphere(
    util::PropertyMap()
    .set(metadata::Identifier::CODESPACE_KEY, metadata::Identifier::EPSG)
    .set(metadata::Identifier::CODE_KEY, 7030)
    .set(common::IdentifiedObject::NAME_KEY, "WGS 84"),
    common::Length(6378137),
    common::Scale(298.257223563));
// actually predefined as Ellipsoid::WGS84 constant

auto datum = GeodeticReferenceFrame::create(
    util::PropertyMap()
    .set(metadata::Identifier::CODESPACE_KEY, metadata::Identifier::EPSG)
    .set(metadata::Identifier::CODE_KEY, 6326)
    .set(common::IdentifiedObject::NAME_KEY, "World Geodetic System 1984"),
    ellipsoid,
    util::optional<std::string>(), // anchor
    greenwich);
// actually predefined as GeodeticReferenceFrame::EPSG_6326 constant

auto geogCRS = GeographicCRS::create(
    util::PropertyMap()
    .set(metadata::Identifier::CODESPACE_KEY, metadata::Identifier::EPSG)
    .set(metadata::Identifier::CODE_KEY, 4326)
    .set(common::IdentifiedObject::NAME_KEY, "WGS 84"),
    datum,
    cs::EllipsoidalCS::createLatitudeLongitude(common::UnitOfMeasure::DEGREE));
// actually predefined as GeographicCRS::EPSG_4326 constant
```
Algorithmic focus

On the algorithmic side, a somewhat involved logic is the CoordinateOperationFactory::createOperations() in coordinateoperation.cpp that takes a pair of source and target CRS and returns a set of possible coordinate operations (either single operations like a Conversion or a Transformation, or concatenated operations). It uses the intrinsic structure of those objects to create the coordinate operation pipeline. That is, if going from a ProjectedCRS to another one, by doing first the inverse conversion from the source ProjectedCRS to its base GeographicCRS, then finding the appropriate transformation(s) from this base GeographicCRS to the base GeographicCRS of the target CRS, and then applying the conversion from this base GeographicCRS to the target ProjectedCRS. At each step, it queries the database to find if one or several transformations are available. The resulting coordinate operations are filtered, and sorted, with user provided hints:

- desired accuracy
- area of use, defined as a bounding box in longitude, latitude space (its actual CRS does not matter for the intended use)
- if no area of use is defined, if and how the area of use of the source and target CRS should be used. By default, the smallest area of use is used. The rationale is for example when transforming between a national ProjectedCRS and a world-scope GeographicCRS to use the area of use of this ProjectedCRS to select the appropriate datum shifts.
- how the area of use of the candidate transformations and the desired area of use (either explicitly or implicitly defined, as explained above) are compared. By default, only transformations whose area of use is fully contained in the desired area of use are selected. It is also possible to relax this test by specifying that only an intersection test must be used.
- whether PROJ transformation grid names should be substituted to the official names, when a match is found in the grid_alternatives table of the database. Defaults to true
- whether the availability of those grids should be used to filter and sort the results. By default, the transformations using grids available in the system will be presented first.

The results are sorted, with the most relevant ones appearing first in the result vector. The criteria used are in that order

- grid actual availability: operations referencing grids not available will be listed after ones with available grids
- grid potential availability: operation referencing grids not known at all in the proj.db will be listed after operations with grids known, but not available.
- known accuracy: operations with unknown accuracies will be listed after operations with known accuracy
- area of use: operations with smaller area of use (the intersection of the operation area of used with the desired area of use) will be listed after the ones with larger area of use
- accuracy: operations with lower accuracy will be listed after operations with higher accuracy (caution: lower accuracy actually means a higher numeric value of the accuracy property, since it is a precision in metre)

All those settings can be specified in the CoordinateOperationContext instance passed to createOperations().

An interesting example to understand how those parameters play together is to use projinfo -s EPSG:4267 -t EPSG:4326 (NAD27 to WGS84 conversions), and see how specifying desired area of use, spatial criterion, grid availability, etc. affects the results.

The following command currently returns 78 results:

```
projinfo -s EPSG:4267 -t EPSG:4326 --summary --spatial-test intersects
```

The createOperations() algorithm also does a kind of “CRS routing”. A typical example is if wanting to transform between CRS A and CRS B, but no direct transformation is referenced in proj.db between those. But if there are transformations between A <-> C and B <-> C, then it is possible to build a concatenated operation A -> C -> B.
The typical example is when C is WGS84, but the implementation is generic and just finds a common pivot from the database. An example of finding a non-WGS84 pivot is when searching a transformation between EPSG:4326 and EPSG:6668 (JGD2011 - Japanese Geodetic Datum 2011), which has no direct transformation registered in the EPSG database. However, there are transformations between those two CRS and JGD2000 (and also Tokyo datum, but that one involves less accurate transformations).

```
projinfo -s EPSG:4326 -t EPSG:6668 --grid-check none --bbox 135.42,34.84,142.14,41.58 --summary
```

Candidate operations found: 7

unknown id, Inverse of JGD2000 to WGS 84 (1) + JGD2000 to JGD2011 (1), 1.2 m, Japan — northern Honshu

unknown id, Inverse of JGD2000 to WGS 84 (1) + JGD2000 to JGD2011 (2), 2 m, Japan — excluding northern main province

unknown id, Inverse of Tokyo to WGS 84 (108) + Tokyo to JGD2011 (2), 9.2 m, Japan — onshore excluding northern main province

unknown id, Inverse of Tokyo to WGS 84 (108) + Tokyo to JGD2000 (2) + JGD2000 to JGD2011 (1), 9.4 m, Japan — northern Honshu

unknown id, Inverse of Tokyo to WGS 84 (2) + Tokyo to JGD2011 (2), 13.2 m, Japan — onshore mainland and adjacent islands

unknown id, Inverse of Tokyo to WGS 84 (2) + Tokyo to JGD2000 (2) + JGD2000 to JGD2011 (1), 13.4 m, Japan — northern Honshu

unknown id, Inverse of Tokyo to WGS 84 (1) + Tokyo to JGD2011 (2), 29.2 m, Asia — Japan and South Korea

11.4.2.4 Code repository

The current state of the work can be found in the iso19111 branch of rouault/proj.4 repository, and is also available as a GitHub pull request at https://github.com/OSGeo/proj.4/pull/1040

Here is a not-so-usable comparison with a fixed snapshot of master branch

11.4.2.5 Database

Content

The database contains CRS and coordinate operation definitions from the EPSG database (IOGP's EPSG Geodetic Parameter Dataset) v9.5.3, IGNF registry (French National Geographic Institute), ESRI database, as well as a few customizations.

Building (for PROJ developers creating the database)

The building of the database is a several stage process:
Construct SQL scripts for EPSG

The first stage consists in constructing .sql scripts mostly with CREATE TABLE and INSERT statements to create the database structure and populate it. There is one .sql file for each database table, populated with the content of the EPSG database, automatically generated with the build_db.py script, which processes the PostgreSQL dumps issued by IOGP. A number of other scripts are dedicated to manual editing, for example grid_alternatives.sql file that binds official grid names to PROJ grid names.

Concert UTF8 SQL to sqlite3 db

The second stage is done automatically by the make process. It pipes the .sql script, in the right order, to the sqlite3 binary to generate a first version of the proj.db SQLite3 database.

Add extra registries

The third stage consists in creating additional .sql files from the content of other registries. For that process, we need to bind some definitions of those registries to those of the EPSG database, to be able to link to existing objects and detect some boring duplicates. The ignf.sql file has been generated using the build_db_create_ignf.py script from the current data/IGNF file that contains CRS definitions (and implicit transformations to WGS84) as PROJ.4 strings. The esri.sql file has been generated using the build_db_from_esri.py script, from the .csv files in https://github.com/Esri/projection-engine-db-doc/tree/master/csv.

Finalize proj.db

The last stage runs make again to incorporate the new .sql files generated in the previous stage (so the process of building the database involves a kind of bootstrapping…)

Building (for PROJ users)

The make process just runs the second stage mentioned above from the .sql files. The resulting proj.db is currently 5.3 MB large.

Structure

The database is structured into the following tables and views. They generally match an ISO-19111 concept, and is generally close to the general structure of the EPSG database. Regarding identification of objects, where the EPSG database only contains a ‘code’ numeric column, the PROJ database identifies objects with a (auth_name, code) tuple of string values, allowing several registries to be combined together.

- **Technical:**
  - **authority_list**: view enumerating the authorities present in the database. Currently: EPSG, IGNF, PROJ
  - **metadata**: a few key/value pairs, for example to indicate the version of the registries imported in the database
  - **object_view**: synthetic view listing objects (ellipsoids, datums, CRS, coordinate operations…) code and name, and the table name where they are further described
  - **alias_names**: list possible alias for the name field of object table
– **link_from_deprecated_to_non_deprecated**: to handle the link between old ESRI to new ESRI/EPSG codes

**Common:**

– **unit_of_measure**: table with UnitOfMeasure definitions.
– **area**: table with area-of-use (bounding boxes) applicable to CRS and coordinate operations.

**Coordinate systems:**

– **axis**: table with CoordinateSystemAxis definitions.
– **coordinate_system**: table with CoordinateSystem definitions.

**Ellipsoid and datums:**

– **ellipsoid**: table with ellipsoid definitions.
– **prime_meridian**: table with PrimeMeridian definitions.
– **geodetic_datum**: table with GeodeticReferenceFrame definitions.
– **vertical_datum**: table with VerticalReferenceFrame definitions.

**CRS:**

– **geodetic_crs**: table with GeodeticCRS and GeographicCRS definitions.
– **projected_crs**: table with ProjectedCRS definitions.
– **vertical_crs**: table with VerticalCRS definitions.
– **compound_crs**: table with CompoundCRS definitions.

**Coordinate operations:**

– **coordinate_operation_view**: view giving a number of common attributes shared by the concrete tables implementing CoordinateOperation.
– **conversion**: table with definitions of Conversion (mostly parameter and values of Projection).
– **concatenated_operation**: table with definitions of ConcatenatedOperation.
– **grid_transformation**: table with all grid-based transformations.
– **grid_packages**: table listing packages in which grids can be found. e.g. “proj-datumgrid”, “proj-datumgrid-europe”, ...
– **grid_alternatives**: table binding official grid names to PROJ grid names. e.g. “Und_min2.5x2.5 egm2008_isw=82_WGS84_TideFree.gz” -> “egm08_25.gtx”
– **helmert_transformation**: table with all Helmert-based transformations.
– **other_transformation**: table with other type of transformations.

The main departure with the structure of the EPSG database is the split of the various coordinate operations over several tables. This was done mostly for human-readability as the EPSG organization of coordoperation, coordoperationmethod, coordoperationparam, coordoperationparamusage, coordoperationparamvalue tables makes it hard to grasp at once all the parameters and values for a given operation.
11.4.2.6 Utilities

A new projinfo utility has been added. It enables the user to enter a CRS or coordinate operation by an AUTHORITY:CODE, PROJ string or WKT string, and see it translated in the different flavors of PROJ and WKT strings. It also enables to build coordinate operations between two CRSs.

Usage

usage: projinfo [-o formats] [-k crs|operation] [--summary] [-q]
[-bbox min_long,min_lat,max_long,max_lat]
[-spatial-test contains|intersects]
[-crs-extent-use none|both|intersection|smallest]
[-grid-check none|discard_missing|sort]
[-boundcrs-to-wgs84]
{object_definition} | (-s {srs_def} -t {srs_def})
-o: formats is a comma separated combination of: all,default,PROJ4,PROJ,WKT_ALL,WKT2_→2015,WKT2_2018,WKT1_GDAL

Examples

Specify CRS by AUTHORITY:CODE

$ projinfo EPSG:4326

PROJ string:
+proj=pipeline +step +proj=longlat +ellps=WGS84 +step +proj=unitconvert +xy_in=rad
->+xy_out=deg +step +proj=axisswap +order=2,1

WKT2_2015 string:
GEODCRS "WGS 84",
  DATUM [ "World Geodetic System 1984" ],
  ELLIPSOID [ "WGS 84", 6378137,298.257223563,
    LENGTHUNIT [ "metre",1 ] ],
  PRIMEM [ "Greenwich", 0 ],
  ANGLEUNIT [ "degree", 0.0174532925199433 ],
  CS [ ellipsoidal, 2 ],
  AXIS [ "geodetic latitude (Lat)" , north, ORDER [ 1 ],
    ANGLEUNIT [ "degree", 0.0174532925199433 ] ],
  AXIS [ "geodetic longitude (Lon)" , east, ORDER [ 2 ],
    ANGLEUNIT [ "degree", 0.0174532925199433 ] ],
  AREA [ "World" ],
  BBOX [ −90,−180,90,180 ],
  ID [ "EPSG", 4326 ]
Specify CRS by PROJ string and specify output formats

```
$ projinfo -o PROJ4,PROJ,WKT1_GDAL,WKT2_2018 "+title=IGN 1972 Nuku Hiva - UTM fuseau 7 Sud +proj=tmerc +towgs84=165.7320,216.7200,180.5050,-0.6434,-0.4512,-0.0791,7.420400 +a=6378388.0000 +rf=297.0000000000000000 +lat_0=0.0000000000000000 +lon_0=-141.0000000000000000 +k_0=0.9996000000000000000 +x_0=500000.0000000000000000 +y_0=10000000.00000000000000000 +units=m +no_defs"

PROJ string:
Error when exporting to PROJ string: BoundCRS cannot be exported as a PROJ.5 string, but its baseCRS might

PROJ.4 string:
+proj=utm +zone=7 +south +ellps=intl +towgs84=165.732,216.72,180.505,-0.6434,-0.4512,-0.0791,7.4204

WKT2_2018 string:
BOUNDCRS[
  SOURCECRS[
    PROJCRS["IGN 1972 Nuku Hiva - UTM fuseau 7 Sud",
      BASEGEOGCRS["unknown",
        DATUM["unknown",
          ELLIPSOID["International 1909 (Hayford)",6378388,297,
            LENGTHUNIT["metre",1],
            ID["EPSG",9001]]],
          PRIMEM["Greenwich",0,
            ANGLEUNIT["degree",0.0174532925199433],
            ID["EPSG",8901]]],
        CONVERSION["unknown",
          METHOD["Transverse Mercator",
            ID["EPSG",9807]],
          PARAMETER["Latitude of natural origin",0,
            ANGLEUNIT["degree",0.0174532925199433],
            ID["EPSG",8801]],
          PARAMETER["Longitude of natural origin",-141,
            ANGLEUNIT["degree",0.0174532925199433],
            ID["EPSG",8802]],
          PARAMETER["Scale factor at natural origin",0.9996,
            SCALEUNIT["unity",1],
            ID["EPSG",8805]],
          PARAMETER["False easting",500000,
            LENGTHUNIT["metre",1],
            ID["EPSG",8806]],
          PARAMETER["False northing",10000000,
            LENGTHUNIT["metre",1],
            ID["EPSG",8807]]],
        CS[Cartesian,2],
        AXIS[(E)],east,
          ORDER[1],
          LENGTHUNIT["metre",1],
          ID["EPSG",9001]],
      AXIS[(N)],north,
        ORDER[2],
        LENGTHUNIT["metre",1],
        ID["EPSG",9001]]],
  TARGETCRS[
    GEOGCRS["WGS 84",
      DATUM["World Geodetic System 1984",]]
]"}
```
ELLIPSOID["WGS 84", 6378137, 298.257223563, LENGTHUNIT["metre", 1]],
PRIMEM["Greenwich", 0],
ANGLEUNIT["degree", 0.0174532925199433],
CS[ellipsoidal, 2],
AXIS["latitude", north,
ORDER[1],
ANGLEUNIT["degree", 0.0174532925199433],
AXIS["longitude", east,
ORDER[2],
ANGLEUNIT["degree", 0.0174532925199433]],
ID["EPSG", 4326]],
ABRIDGEDTRANSFORMATION["Transformation from unknown to WGS84",
METHOD["Position Vector transformation (geog2D domain)"],
ID["EPSG", 9606],
PARAMETER["X-axis translation", 165.732, ID["EPSG", 8605]],
PARAMETER["Y-axis translation", 216.72, ID["EPSG", 8606]],
PARAMETER["Z-axis translation", 180.505, ID["EPSG", 8607]],
PARAMETER["X-axis rotation", -0.6434, ID["EPSG", 8608]],
PARAMETER["Y-axis rotation", -0.4512, ID["EPSG", 8609]],
PARAMETER["Z-axis rotation", -0.0791, ID["EPSG", 8610]],
PARAMETER["Scale difference", 1.0000074204, ID["EPSG", 8611]]]

WKT1_GDAL:
PROJCS["IGN 1972 Nuku Hiva - UTM fuseau 7 Sud",
GEOGCS["unknown",
DATUM["unknown",
SPHEROID["International 1909 (Hayford)", 6378388, 297],
TOWGS84[165.732, 216.72, 180.505, -0.6434, -0.4512, -0.0791, 7.4204]],
PRIMEM["Greenwich", 0],
AUTHORITY["EPSG", "8901"],
UNIT["degree", 0.0174532925199433],
AUTHORITY["EPSG", "9122"],
AXIS["Longitude", EAST],
AXIS["Latitude", NORTH]],
PROJECTION["Transverse_Mercator"],
PARAMETER["latitude_of_origin", 0],
PARAMETER["central_meridian", -141],
PARAMETER["scale_factor", 0.9996],
PARAMETER["false_easting", 500000],
PARAMETER["false_northing", 10000000],
UNIT["metre", 1],
AUTHORITY["EPSG", "9001"],
AXIS["Easting", EAST],
AXIS["Northing", NORTH]]
**Find transformations between 2 CRS**

Between “Poland zone I” (based on Pulkovo 42 datum) and “UTM WGS84 zone 34N”

Summary view:

```
$ projinfo -s EPSG:2171 -t EPSG:32634 --summary
```

Candidate operations found: 1
unknown id, Inverse of Poland zone I + Pulkovo 1942(58) to WGS 84 (1) + UTM zone 34N,
-1 m, Poland - onshore

Display of pipelines:

```
$ PROJ_LIB=data src/projinfo -s EPSG:2171 -t EPSG:32634 -o PROJ

PROJ string:
+proj=pipeline +step +proj=axisswap +order=2,1 +step +inv +proj=sterea +lat_0=50.625
+lon_0=21.0833333333333 +k=0.9998 +x_0=4637000 +y_0=5647000 +ellps=krass +step
+proj=cart +ellps=krass +step +proj=helmert +x=33.4 +y=-146.6 +z=-76.3 +rx=-0.359
+ry=-0.053 +rz=0.844 +s=-0.84 +convention=position_vector +step +inv +proj=cart
+ellps=WGS84 +step +proj=utm +zone=34 +ellps=WGS84
```

**11.4.2.7 Impacted files**

New files (excluding makefile.am, CMakeLists.txt and other build infrastructure artifacts):

- **include/proj/: Public installed C++ headers**
  - `common.hpp`: declarations of osgeo::proj::common namespace.
  - `coordinateoperation.hpp`: declarations of osgeo::proj::operation namespace.
  - `coordinatesystem.hpp`: declarations of osgeo::proj::cs namespace.
  - `crs.hpp`: declarations of osgeo::proj::crs namespace.
  - `datum.hpp`: declarations of osgeo::proj::datum namespace.
  - `io.hpp`: declarations of osgeo::proj::io namespace.
  - `metadata.hpp`: declarations of osgeo::proj::metadata namespace.
  - `util.hpp`: declarations of osgeo::proj::util namespace.
  - `nn.hpp`: Code from https://github.com/dropbox/nn to manage Non-nullable pointers for C++

- **include/proj/internal: Private non-installed C++ headers**
  - `coordinateoperation_internal.hpp`: classes InverseCoordinateOperation, InverseConversion, InverseTransformation, PROJBasedOperation, and functions to get conversion mappings between WKT and PROJ syntax
  - `coordinateoperation_constants.hpp`: Select subset of conversion/transformation EPSG names and codes for the purpose of translating them to PROJ strings
  - `coordinatesystem_internal.hpp`: classes AxisDirectionWKT1, AxisName and AxisAbbreviation
  - `internal.hpp`: a few helper functions, mostly to do string-based operations
PROJ coordinate transformation software library, Release 6.1.1

- **io_internal.hpp**: class WKTConstants
- **helmert_constants.hpp**: Helmert-based transformation & parameters names and codes.
- **lru_cache.hpp**: code from https://github.com/mohaps/lrucache11 to have a generic Least-Recently-Used cache of objects

• **src/**:
  - **c_api.cpp**: C++ API mapped to C functions
  - **common.cpp**: implementation of common.hpp
  - **coordinateoperation.cpp**: implementation of coordinateoperation.hpp
  - **coordinatesystem.cpp**: implementation of coordinatesystem.hpp
  - **crs.cpp**: implementation of crs.hpp
  - **datum.cpp**: implementation of datum.hpp
  - **factory.cpp**: implementation of AuthorityFactory class (from io.hpp)
  - **internal.cpp**: implementation of internal.hpp
  - **io.cpp**: implementation of io.hpp
  - **metadata.cpp**: implementation of metadata.hpp
  - **static.cpp**: a number of static constants (like pre-defined well-known ellipsoid, datum and CRS), put in the right order for correct static initializations
  - **util.cpp**: implementation of util.hpp
  - **projinfo.cpp**: new ‘projinfo’ binary
  - **general.dox**: generic introduction documentation.

• **data/sql/**:
  - **area.sql**: generated by build_db.py
  - **axis.sql**: generated by build_db.py
  - **begin.sql**: hand generated (trivial)
  - **commit.sql**: hand generated (trivial)
  - **compound_crs.sql**: generated by build_db.py
  - **concatenated_operation.sql**: generated by build_db.py
  - **conversion.sql**: generated by build_db.py
  - **coordinate_operation.sql**: generated by build_db.py
  - **coordinate_system.sql**: generated by build_db.py
  - **crs.sql**: generated by build_db.py
  - **customizations.sql**: hand generated (empty)
  - **ellipsoid.sql**: generated by build_db.py
  - **geodetic_crs.sql**: generated by build_db.py
  - **geodetic_datum.sql**: generated by build_db.py
  - **grid_alternatives.sql**: hand-generated. Contains links between official registry grid names and PROJ ones
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– proj_db_table_defs.sql: hand-generated. Database structure: CREATE TABLE / CREATE VIEW / CREATE TRIGGER
– projected_crs.sql: generated by build_db.py
– unit_of_measure.sql: generated by build_db.py
– vertical_crs.sql: generated by build_db.py
– vertical_datum.sql: generated by build_db.py

• scripts/:
  – build_db.py: generate .sql files from EPSG database dumps
  – build_db_create_ignf.py: generates data/sql/ignf.sql
  – build_db_from_esri.py: generates data/sql/esri.sql
  – doxygen.sh: generates Doxygen documentation
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  – test_operation.cpp: test of src/operation.cpp
11.4.2.8 C API

proj.h has been extended to bind a number of C++ classes/methods to a C API.

The main structure is an opaque PJ_OBJ* roughly encapsulating a osgeo::proj::BaseObject, that can represent a CRS or a CoordinateOperation object. A number of the C functions will work only if the right type of underlying C++ object is used with them. Misuse will be properly handled at runtime. If a user passes a PJ_OBJ* representing a coordinate operation to a pj_obj_crs_xxxx() function, it will properly error out. This design has been chosen over creating a dedicate PJ_xxx object for each C++ class, because such an approach would require adding many conversion and free functions for little benefit.

This C API is incomplete. In particular, it does not allow to build ISO19111 objects at hand. However it currently permits a number of actions:

- building CRS and coordinate operations from WKT and PROJ strings, or from the proj.db database
- exporting CRS and coordinate operations as WKT and PROJ strings
- querying main attributes of those objects
- finding coordinate operations between two CRS.

test_c_api.cpp should demonstrates simple usage of the API (note: for the conveniency of writing the tests in C++, test_c_api.cpp wraps the C PJ_OBJ* instances in C++ ‘keeper’ objects that automatically call the pj_obj_unref() function at function end. In a pure C use, the caller must use pj_obj_unref() to prevent leaks.)

11.4.2.9 Documentation

All public C++ classes and methods and C functions are documented with Doxygen.

Current snapshot of Class list

Spaghetti inheritance diagram

A basic integration of the Doxygen XML output into the general PROJ documentation (using reStructuredText format) has been done with the the Sphinx extension Breathe, producing:

- One section with the C++ API
- One section with the C API

11.4.2.10 Testing

Nearly all exported methods are tested by a unit test. Global line coverage of the new files is 92%. Those tests represent 16k lines of codes.

11.4.2.11 Build requirements

The new code leverages on a number of C++11 features (auto keyword, constexpr, initializer list, std::shared_ptr, lambda functions, etc.), which means that a C++11-compliant compiler must be used to generate PROJ:

- gcc >= 4.8
- clang >= 3.3
- Visual Studio >= 2015.

Compilers tested by the Travis-CI and AppVeyor continuous integration environments:

- GCC 4.8
• mingw-w64-x86-64 4.8
• clang 5.0
• Apple LLVM version 9.1.0 (clang-902.0.39.2)
• MSVC 2015 32 and 64 bit
• MSVC 2017 32 and 64 bit

The librsqlite3 >= 3.7 development package must also be available. And the sqlite3 binary must be available to build the proj.db files from the .sql files.

11.4.2.12 Runtime requirements

• libc++/libstdc++/MSVC runtime consistent with the compiler used
• librsqlite3 >= 3.7

11.4.2.13 Backward compatibility

At this stage, no backward compatibility issue is foreseen, as no existing functional C code has been modified to use the new capabilities

11.4.2.14 Future work

The work described in this RFC will be pursued in a number of directions. Non-exhaustively:

• Support for ESRI WKT1 dialect (PROJ currently ingest the ProjectedCRS in esri.sql in that dialect, but there is no mapping between it and EPSG operation and parameter names, so conversion to PROJ strings does not always work.
• closer integration with the existing code base. In particular, the +init=dict:code syntax should now go first to the database (then the epsg and IGNF files can be removed). Similarly proj_create_crs_to_crs() could use the new capabilities to find an appropriate coordinate transformation.
• and whatever else changes are needed to address GDAL and libgeotiff needs

11.4.2.15 Adoption status

The RFC has been adopted with support from PSC members Kurt Schwehr, Kristian Evers, Howard Butler and Even Rouault.

11.4.3 PROJ RFC 3: Dependency management

Author Kristian Evers
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Status Adopted
Last Updated 2019-01-16
11.4.3.1 Summary

This document defines a set of guidelines for dependency management in PROJ. With PROJ being a core component in many downstream software packages clearly stating which dependencies the library has is of great value. This document concern both programming language standards as well as minimum required versions of library dependencies and build tools.

It is proposed to adopt a rolling update scheme that ensures that PROJ is sufficiently accessible, even on older systems, as well as keeping up with the technological evolution. The scheme is divided in two parts, one concerning versions of used programming languages within PROJ and the other concerning software packages that PROJ depend on.

With adoption of this RFC, versions used for

1. programming languages will always be at least two revisions behind the most recent standard
2. software packages will always be at least two years old (patch releases are exempt)

A change in programming language standard can only be introduced with a new major version release of PROJ. Changes for software package dependencies can be introduced with minor version releases of PROJ. Changing the version requirements for a dependency needs to be approved by the PSC.

Following the above rule set will ensure that all but the most conservative users of PROJ will be able to build and use the most recent version of the library.

In the sections below details concerning programming languages and software dependencies are outlined. The RFC is concluded with a bootstrapping section that details the state of dependencies after the accept of the RFC.

11.4.3.2 Background

PROJ has traditionally been written in C89. Until recently, no formal requirements of e.g. build systems has been defined and formally accepted by the project. :ref:`RFC2 <rfc2>` formally introduces dependencies on C++11 and SQLite 3.7.

In this RFC a rolling update of version or standard requirements is described. The reasoning behind a rolling update scheme is that it has become increasingly evident that C89 is becoming outdated and creating a less than optimal development environment for contributors. It has been noted that the most commonly used compilers all now support more recent versions of C, so the strict usage of C89 is no longer as critical as it used to be.

Similarly, rolling updates to other tools and libraries that PROJ depend on will ensure that the code base can be kept modern and in line with the rest of the open source software ecosphere.

11.4.3.3 C and C++

Following RFC2 PROJ is written in both C and C++. At the time of writing the core library is C based and the code described in RFC2 is written in C++. While the core library is mostly written in C it is compiled as C++. Minor sections of PROJ, like the geodesic algorithms are still compiled as C since there is no apparent benefit of compiling with a C++ compiler. This may change in the future.

Both the C and C++ standards are updated with regular intervals. After an update of a standard it takes time for compiler manufacturers to implement the standards fully, which makes adaption of new standards potentially troublesome if done too soon. On the other hand, waiting too long to adopt new standards will eventually make the code base feel old and new contributors are more likely to stay away because they don’t want to work using tools of the past. With a rolling update scheme both concerns can be managed by always staying behind the most recent standard, but not so far away that potential contributors are scared away. Keeping a policy of always lagging behind be two iterations of the standard is thought to be the best comprise between the two concerns.

C comes in four ISO standardised varieties: C89, C99, C11, C18. In this document we refer to their informal names for ease of reading. C++ exists in five varieties: C++98, C++03, C++11, C++14, C++17. Before adoption of this
RFC PROJ uses C89 and C++11. For C, that means that the used standard is three iterations behind the most recent standard. C++ is two iterations behind. Following the rules in this RFC the required C standard used in PROJ is at allowed to be two iterations behind the most recent standard. That means that a change to C99 is possible, as long as the PROJ PSC acknowledges such a change.

When a new standard for either C or C++ is released PROJ should consider changing its requirement to the next standard in the line. For C++ that means a change in standard roughly every three years, for C the periods between standard updates is expected to be longer. Adaptation of new programming language standards should be coordinated with a major version release of PROJ.

11.4.3.4 Software dependencies

At the time of writing PROJ is dependent on very few external packages. In fact only one runtime dependency is present: SQLite. Building PROJ also requires one of two external dependencies for configuration: Autotools or CMake.

As with programming language standards it is preferable that software dependencies are a bit behind the most recent development. For this reason it is required that the minimum version supported in PROJ dependencies is at least two years old, preferably more. It is not a requirement that the minimum version of dependencies is always kept strictly two years behind current development, but it is allowed in case future development of PROJ warrants an update. Changes in minimum version requirements are allowed to happen with minor version releases of PROJ.

At the time of writing the minimum version required for SQLite it 3.7 which was released in 2010. CMake currently is required to be at least at version 2.8.3 which was also released in 2010.

11.4.3.5 Bootstrapping

This RFC comes with a set of guidelines for handling dependencies for PROJ in the future. Up until now dependencies hasn’t been handled consistently, with some dependencies not being approved formally by the projects governing body. Therefore minimum versions of PROJ dependencies is proposed so that at the acception of this RFC PROJ will have the following external requirements:

- C99 (was C89)
- C++11 (already approved in RFC2)
- SQLite 3.7 (already approved in RFC2)
- CMake 3.5 (was 2.8.3)

11.4.3.6 Adoption status

The RFC was adopted on 2018-01-19 with +1’s from the following PSC members

- Kristian Evers
- Even Rouault
- Thomas Knudsen
- Howard Butler
12.1 Which file formats does PROJ support?

The command line applications that come with PROJ only support text input and output (apart from proj which accepts a simple binary data stream as well). proj, cs2cs and cct expects text files with one coordinate per line with each coordinate dimension in a separate column.

Note: If your data is stored in a common geodata file format chances are that you can use GDAL as a frontend to PROJ and transform your data with the ogr2ogr application.

12.2 Can I transform from abc to xyz?

Probably. PROJ supports transformations between most coordinate reference systems registered in the EPSG registry, as well as a number of other coordinate reference systems. The best way to find out is to test it with the projinfo application. Here’s an example checking if there’s a transformation between ETRS89/UTM32N (EPSG:25832) and ETRS89/DKTM1 (EPSG:4093):

```
$ ./projinfo -s EPSG:25832 -t EPSG:4093 -o PROJ
Candidate operations found: 1
Operation n°1:
unknown id, Inverse of UTM zone 32N + DKTM1, 0 m, World
PROJ string:
+proj=pipeline +step +inv +proj=utm +zone=32 +ellps=GRS80
+step +proj=tmerc +lat_0=0 +lon_0=9 +k=0.99998 +x_0=200000 +y_0=-5000000 +ellps=GRS80
```

See the projinfo documentation for more info on how to use it.
12.3 Coordinate reference system xyz is not in the EPSG registry, what do I do?

Generally PROJ will accept coordinate reference system descriptions in the form of WKT, WKT2 and PROJ strings. If you are able to describe your desired CRS in either of those formats there’s a good chance that PROJ will be able to make sense of it.

If it is important to you that a given CRS is added to the EPSG registry, you should contact your local geodetic authority and ask them to submit the CRS for inclusion in the registry.

12.4 I found a bug in PROJ, how do I get it fixed?

Please report bugs that you find to the issue tracker on GitHub. Here's how.

If you know how to program you can also try to fix it yourself. You are welcome to ask for guidance on one of the communication channels used by the project.

12.5 How do I contribute to PROJ?

Any contributions from the PROJ community is welcome. See Contributing for more details.

12.6 How do I calculate distances/directions on the surface of the earth?

These are called geodesic calculations. There is a page about it here: Geodesic calculations.

12.7 What is the best format for describing coordinate reference systems?

A coordinate reference system (CRS) can in PROJ be described in several ways: As PROJ strings, Well-Known Text (WKT) and as spatial reference ID’s (such as EPSG codes). Generally, WKT or SRID’s are preferred over PROJ strings as they can contain more information about a given CRS. Conversions between WKT and PROJ strings will in most cases cause a loss of information, potentially leading to erroneous transformations.

For compatibility reasons PROJ supports several WKT dialects (see projinfo -o). If possible WKT2 should be used.
12.8 Why is the axis ordering in PROJ not consistent?

PROJ respects the axis ordering as it was defined by the authority in charge of a given coordinate reference system. This is in accordance to the ISO19111 standard [ISO19111]. Unfortunately most GIS software on the market doesn’t follow this standard. Before version 6, PROJ did not respect the standard either. This causes some problems while the rest of the industry conforms to the standard. PROJ intends to spearhead this effort, hopefully setting a good example for the rest of the geospatial industry.

Customarily in GIS the first component in a coordinate tuple has been aligned with the east/west direction and the second component with the north/south direction. For many coordinate reference systems this is also what is defined by the authority. There are however exceptions, especially when dealing with coordinate systems that don’t align with the cardinal directions of a compass. For example it is not obvious which coordinate component aligns to which axis in a skewed coordinate system with a 45 degrees angle against the north direction. Similarly, a geocentric cartesian coordinate system usually has the z-component aligned with the rotational axis of the earth and hence the axis points towards north. Both cases are incompatible with the convention of always having the x-component be the east/west axis, the y-component the north/south axis and the z-component the up/down axis.

In most cases coordinate reference systems with geodetic coordinates expect the input ordered as latitude/longitude (typically with the EPSG dataset), however, internally PROJ expects an longitude/latitude ordering for all projections. This is generally hidden for users but in a few cases it is exposed at the surface level of PROJ, most prominently in the proj utility which expects longitude/latitude ordering of input data (unless proj -r is used).

In case of doubt about the axis order of a specific CRS projinfo is able to provide an answer. Simply look up the CRS and examine the axis specification of the Well-Known Text output:

```plaintext
projinfo EPSG:4326
PROJ.4 string:
+proj=longlat +datum=WGS84 +no_defs +type=crs
WKT2_2018 string:
GEOGCRS["WGS 84",
  DATUM["World Geodetic System 1984",
    ELLIPSOID["WGS 84",6378137,298.257223563,
      LENGTHUNIT["metre",1]]],
  PRIMEM["Greenwich",0,
    ANGLEUNIT["degree",0.0174532925199433]],
  CS[ellipsoidal,2],
    AXIS["geodetic latitude (Lat)",north,
      ORDER[1],
      ANGLEUNIT["degree",0.0174532925199433]],
    AXIS["geodetic longitude (Lon)",east,
      ORDER[2],
      ANGLEUNIT["degree",0.0174532925199433]],
  USAGE[.Scope["unknown"],
    AREA["World"],
    BBOX[-90,-180,90,180],
    ID["EPSG",4326]]
```

12.8. Why is the axis ordering in PROJ not consistent? 507
Pseudocylindrical Projection  Pseudocylindrical projections have the mathematical characteristics of

\[ x = f(\lambda, \phi) \]
\[ y = g(\phi) \]

where the parallels of latitude are straight lines, like cylindrical projections, but the meridians are curved toward the center as they depart from the equator. This is an effort to minimize the distortion of the polar regions inherent in the cylindrical projections.

Pseudocylindrical projections are almost exclusively used for small scale global displays and, except for the Sinusoidal projection, only derived for a spherical Earth. Because of the basic definition none of the pseudocylindrical projections are conformal but many are equal area.

To further reduce distortion, pseudocylindrical are often presented in interrupted form that are made by joining several regions with appropriate central meridians and false easting and clipping boundaries. Interrupted Homolosine constructions are suited for showing respective global land and oceanic regions, for example. To reduce the lateral size of the map, some uses remove an irregular, North-South strip of the mid-Atlantic region so that the western tip of Africa is plotted north of the eastern tip of South America.


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